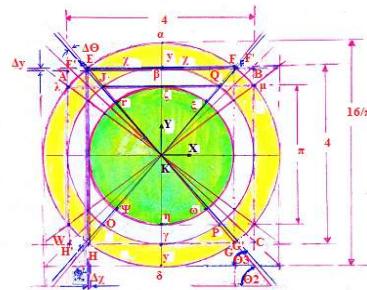


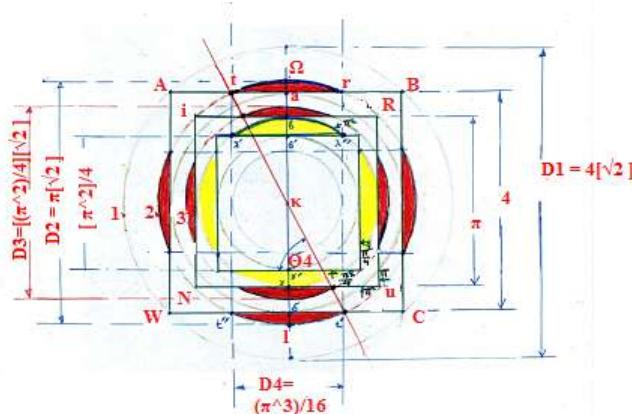


Treatise on Circle – Generator Polyhedron

Harmony and Disharmony



Condition of Three Concentric Circles in Common Ratio



By
Eur Ing Panagiotis Stefanides BSc(Eng)Lon(Hons)
MSc(Eng)NTUA CEng MIET
Chartered Engineer[UK]



Kifissia Athens April-May 2017

© Copyright 1985- 2017, Eur Ing Panagiotis Chr. Stefanides CEng MIET

ISBN 978 – 618 – 83169 – 0 - 4



Publisher Panagiotis Chr. Stefanides **Heliotropio Stefanides**

Author Panagiotis Chr. Stefanides

Published Athens, 04 – 05 - 2017

ISBN 978 – 618 – 83169 – 0 - 4

© Copyright 2017 by Panagiotis Ch. Stefanides

National Library of Greece, ISBN Number, Issued Date 04 – 05 - 2017

ISBN 978 – 618 – 83169 – 0 – 4

Cover Illustrations by Panagiotis Chr. Stefanides

Front Cover Page [1] : Concentric Circles

Back Cover Page [122] : Generator Polyhedron

Treatise on Circle – Generator Polyhedron

**Harmony and Disharmony
Condition of Three Concentric Circles
in Common Ratio**

ISBN 978 – 618 – 83169 – 0 - 4



© Copyright 04 – 05 - 2017 Panagiotis Ch. Stefanides

National Library of Greece

ISBN 978 – 618 – 83169 – 0 - 4

Panagiotis Stefanides
8, Alonion st.,
Kifissia,
Athens, 145 62
Greece

Treatise on Circle-Generator Polyhedron

**Harmony and Disharmony
Condition of Three Concentric Circles
in Common Ratio**

Published Athens April-May 2017 - Heliotropio Stefanides

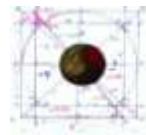


Generator Polyhedron By Panagiotis Stefanides- 03 April 2017



**To my Adorable and Beloved Ones,
my wife Mary and my Daughter Natalia's New Born Family
24 April 2017**

**Published Athens 2017 – Heliotropio Stefanides
© Copyright 1985-2017 Panagiotis Stefa**



In Anticipation

To the “*discussions*”, and “*navigation*” instructions, during lengthy sea and oceanic seafarer’s voyages, I received from my father, on the celestial bodies’ “*spirals*”, their “*temporal*” periodic “*cyclic*” motion “*frequencies*”, when clear guiding night or sunny day skies permitted, for stellar, lunar or solar “*timely measurements*”, and for the relevant “*calculations*” involved, of the vessel’s “*position*” in the sea with acceptable “*errors*” estimation, dependent on mathematics, “*astronomical data*” correctly applied, and with instrument “*sextant*” within acceptable “*functioning condition*” and “*calibration*”, for the “*reliable mile safety*” accuracy limit.



Astrolabe Structure by
Captain Mariner Christos P. Stefanides [1911-1999]

FOREWORD

Since 1985, I posed a *Conjecture* to myself, that there should be at least one reliable *Formula or Method* [possibly a ruler and compass one] with its proof for the *Value of π* [as there are many of the kind, but not leading to the same *Exact Value*].

The concept envisaged, should involve *Eucleidean Geometry* [as it bears reliable consequence, and should be easily examined for its *Truth or not*].

Amongst the various methods that I have come to, [and delivered to various Conferences and Exhibitions, nationally and internationally], for some classical problems' solutions, [as those additional ones presented here as contents of the book, which to me are very interesting and challenging], are *problems* with *theoretical geometric solutions and proofs, simply, by ruler and compass*, with purpose of performing, as far as possible, more analytic and more simplified presentations.

The work elaborated here concerns 3 Concentric Circles in Ratio to each other of $4/\pi$, analyzing and comparing the results, for evident conditions for found Symmetries or Dissymmetries and consequently conditions for Harmony or Disharmony.



Treatise on Circle

HARMONY and DISHARMONY

$$2y + 4 = 16/\pi$$

$$y[\{16/\pi\} - y] = [\pi/2]^2$$

$$\pi^4 - [2*\pi^2]*[(8/\pi) - 2]^3 + 48*\pi*[(8/\pi) - 2]^2 - 256*[(8/\pi) - 2] = 0$$

$$64/\pi^2 - 32/\pi + 4 - 128/\pi^2 + 32/\pi + \pi^2/4 = 0$$

$$\underline{\pi^4 + 16\pi^2 - 4^4 = 0}$$

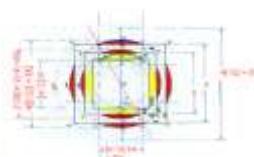
Condition of 3 Circles in Common Ratio

$$(16/\pi)y - y^2 = s^2$$

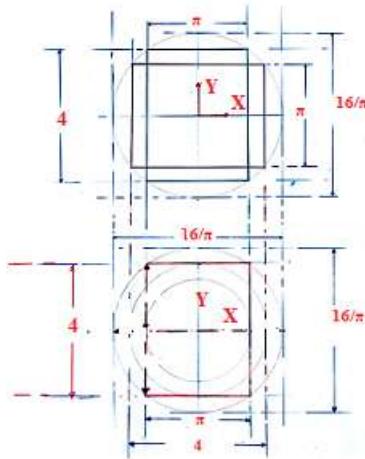
$$2y = (16/\pi) - 4$$

$$(16/\pi)x - x^2 = t^2$$

$$2x + \pi = 16/\pi$$



Treatise on Circle Harmony and Disharmony, Condition of 3 Circles in Common Ratio



Since 1985, I posed a *Conjecture* to myself, that there should be at least one reliable *Formula or Method* [possibly [a ruler and compass one](#)] with its proof for the *Value of π* [as there are many of the kind, but not leading to the same *Exact Value*].

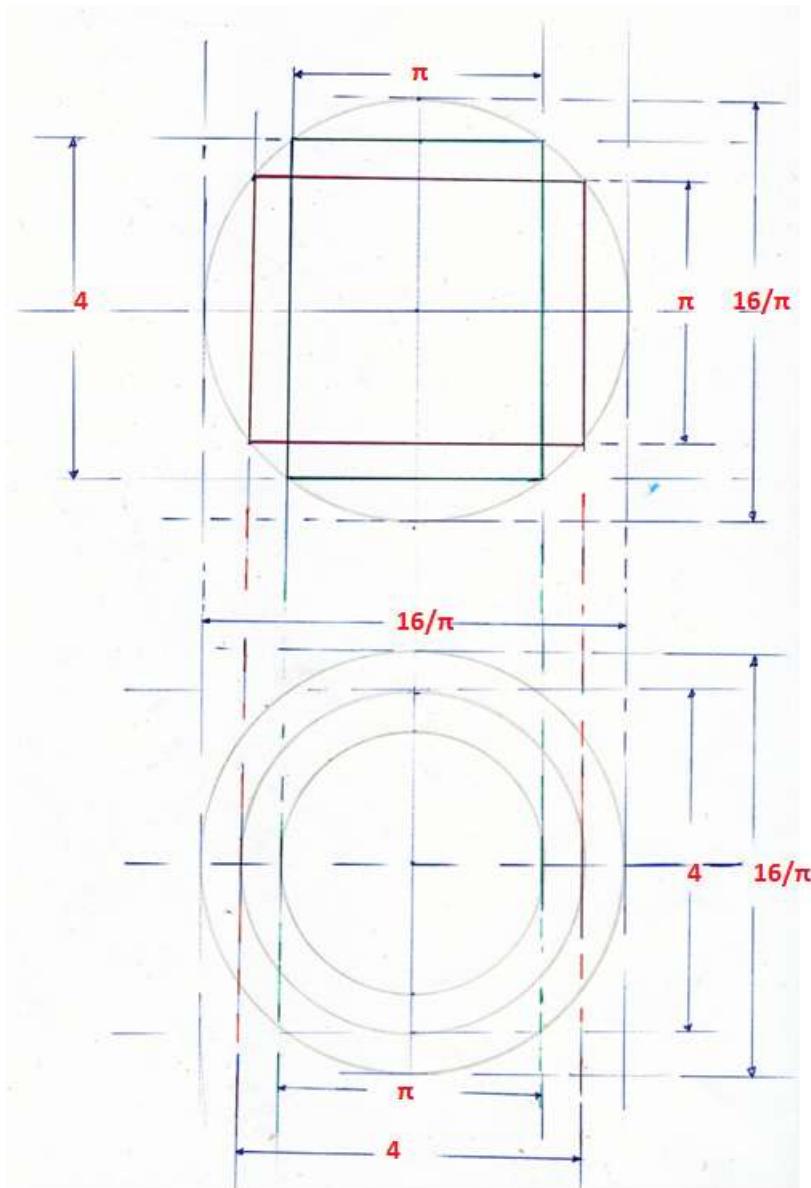
The concept envisaged, should involve *Eucleidean Geometry* [as it bears reliable consequence, and should be easily examined for its *Truth or not*].

Amongst the various methods that I have come to, [and delivered to various [Conferences and Exhibitions](#), nationally and [internationally](#)], for some classical problems' solutions, [as those additional ones presented here as contents of the book, which to me are very interesting and challenging], are *problems with theoretical geometric solutions and proofs, simply, by ruler and compass*, with purpose of performing, as far as possible, more analytic and more simplified presentations.

The work elaborated here concerns 3 Concentric Circles in Ratio to each other of $4/\pi$, analyzing and comparing the results, for evident conditions for found Symmetries or Dissymmetries and consequently conditions for Harmony or Disharmony.

Diameters D1, D2, D3

[*] **D1 = $16/\pi$, D2= 4, D3 = π and $D1/D2 = D2/D3$ or $[D1]*[D3] = [D2]^2$**



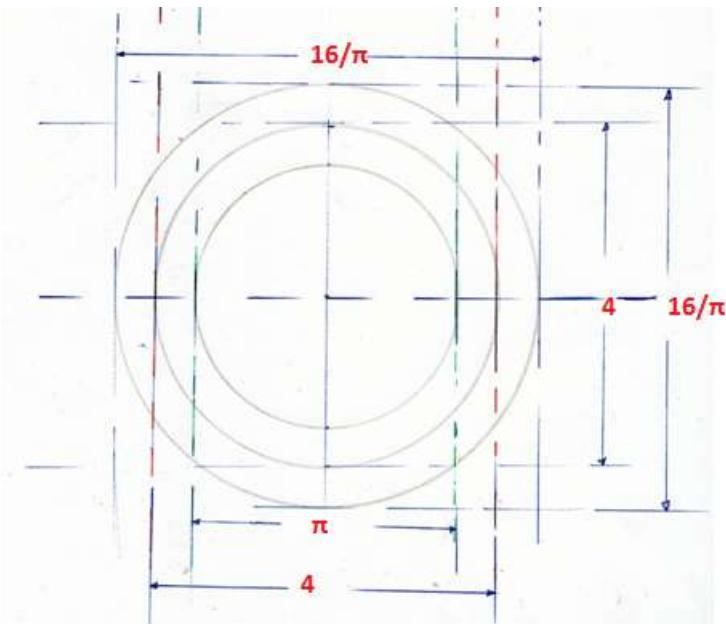
Conjectural Configuration

Projection of inner circles' diameters D2 and D3 fit as chords of outer circle of diameter D1.

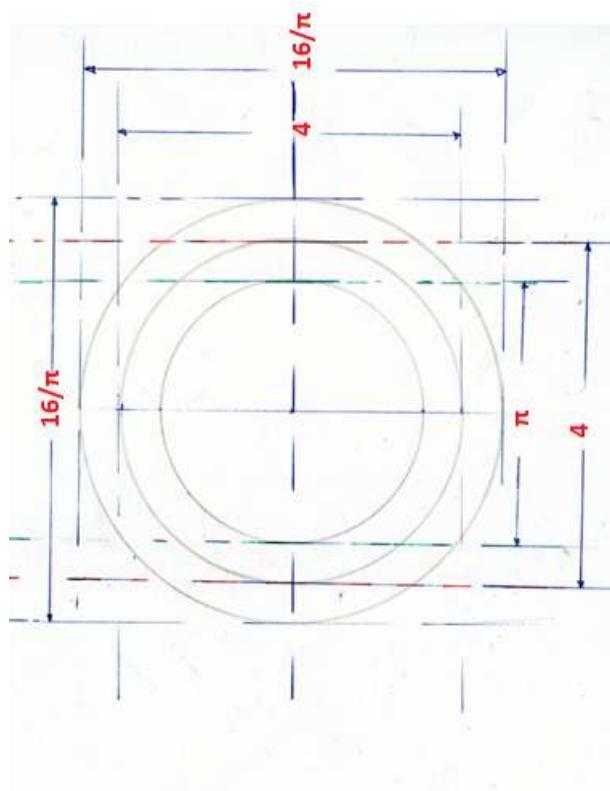
At first contemplation of the two configurations it appears that both comply to the dimensions quoted.

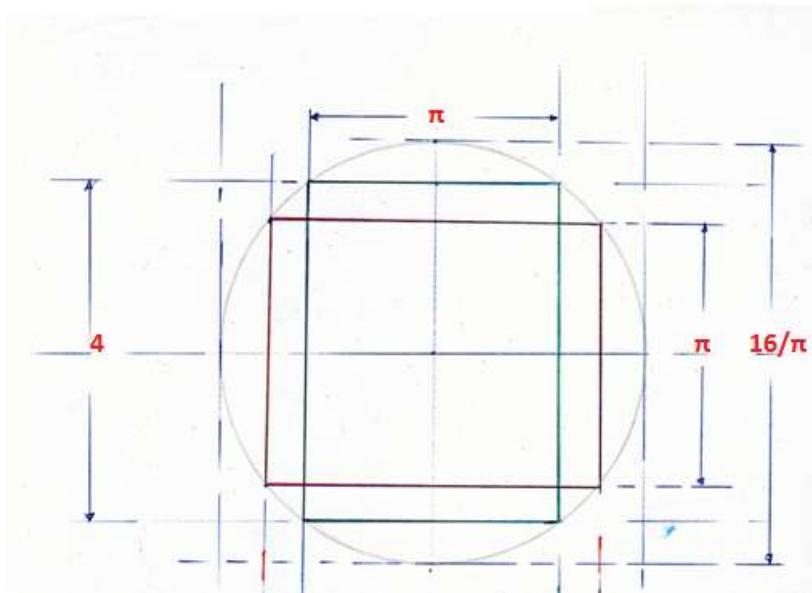
However logic requires that geometrical compliance should be examined according to valid theorems.

One such which shall apply here, is that of the “*Power of Point Theorem*”.

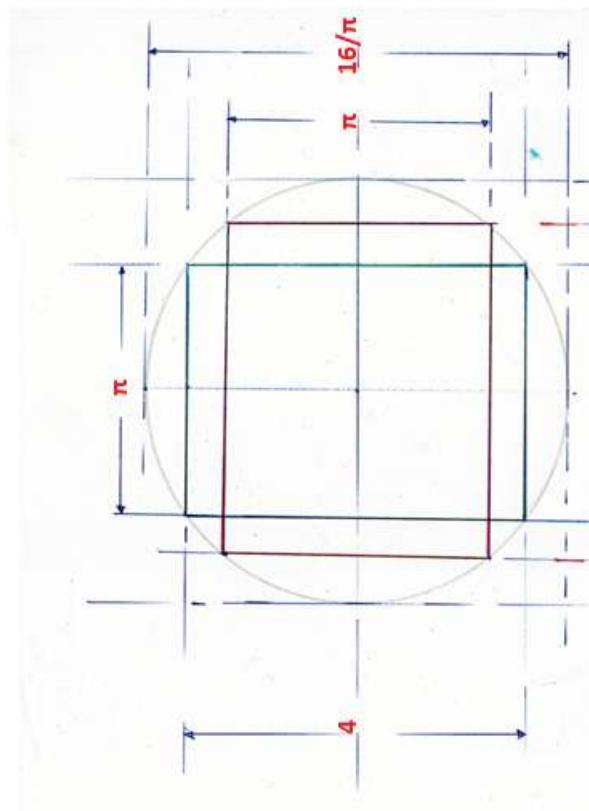


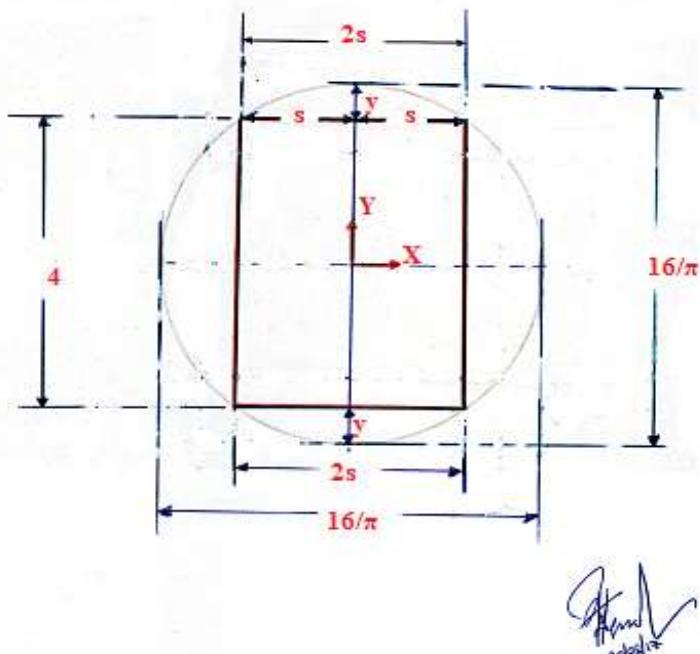
90 DEG. ROTATION OF CIRCLES, SYMMETRY DOES NOT CHANGE.





90 DEG. ROTATION OF PARALLELOGRAMMES [WITHIN CIRCLE: D = $16/\pi$],
SYMMETRY DOES NOT CHANGE.



A1

$$y[16/\pi - y] = s^2, \quad [\text{application of "Power of Point Theorem"}]$$

$$(16/\pi)y - y^2 = s^2$$

$$2y + 4 = 16/\pi, \quad 2y = (16/\pi) - 4$$

$$y = [(8/\pi) - 2] = 0.546479089$$

$$(16/\pi)y - y^2 = s^2$$

$$(16/3.141592654)(0.546479089) - (0.546479089)^2 = s^2$$

$$s^2 = 2.783195148 - 0.298639395 = 2.484555753$$

$$s^2 = 2.484555753, \quad s = 1.576247364$$

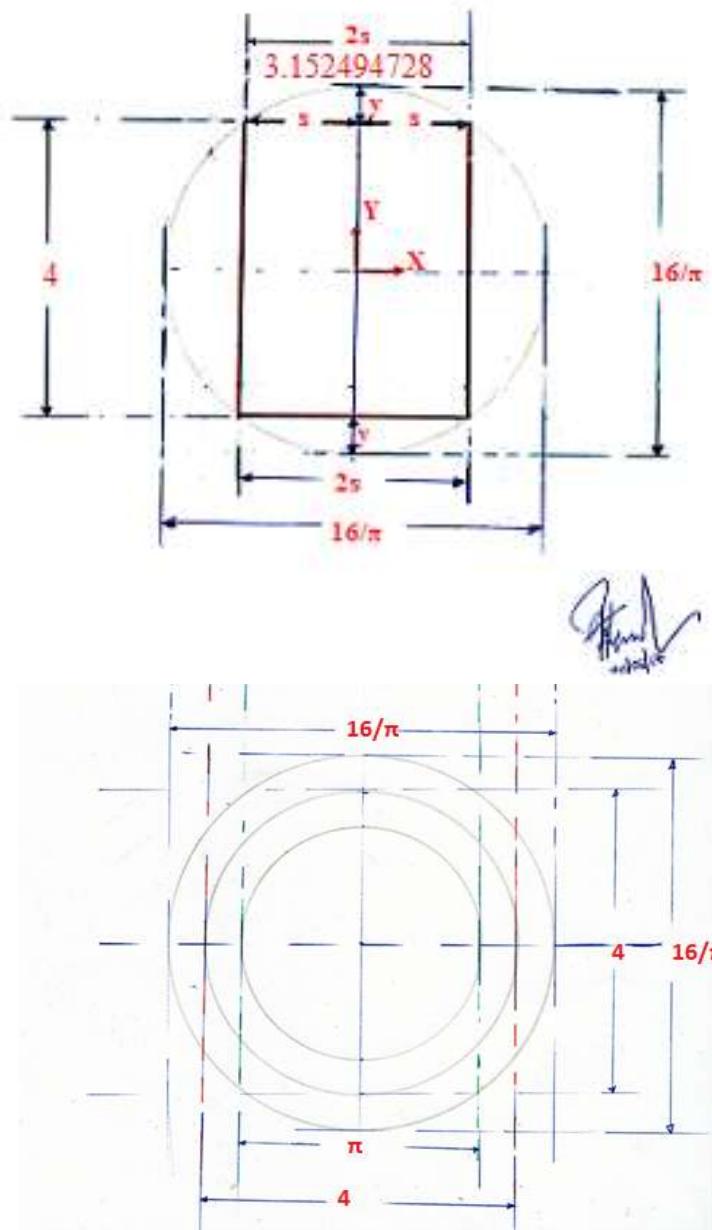
$$2s = 3.152494728$$

[https://www.wolframalpha.com/input/?i=\(16%2F3.141592654\)\(0.546479089\)++%E2%80%93+\(0.546479089\)%5E2++%3D+s%5E2](https://www.wolframalpha.com/input/?i=(16%2F3.141592654)(0.546479089)++%E2%80%93+(0.546479089)%5E2++%3D+s%5E2)

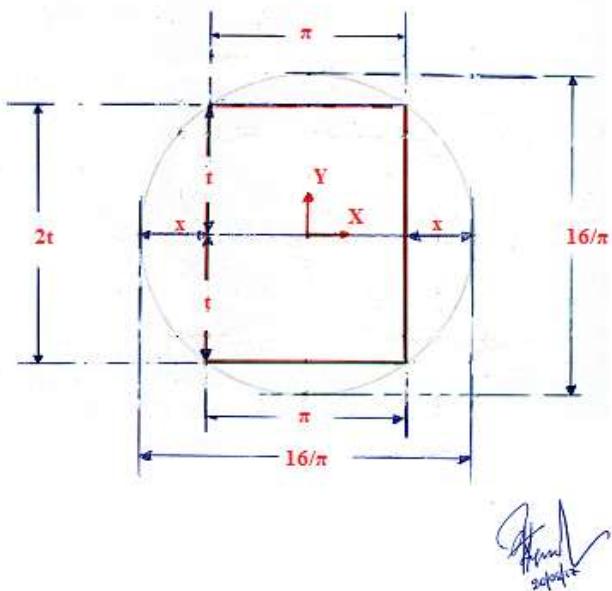
<https://www.wolframalpha.com/input/?i=2%7B+SQRT2.484555750864906111794479535347169168673514475311094867361%7D+%3D>

<https://www.wolframalpha.com/input/?i=2%7B+SORT2.484555750864906111794479535347169168673514475311094867361%7D+%3D>

A1a



A2



$$x[16/\pi - x] = t^2, \quad [\text{application of "Power of Point Theorem"}]$$

$$(16/\pi)x - x^2 = t^2$$

$$2x + \pi = 16/\pi, \quad 2x = [(16/\pi) - \pi] = 1.951365525$$

$$x = [(8/\pi) - (\pi/2)] = 0.975682763$$

$$(16/\pi)x - x^2 = t^2$$

$$(16/3.141592654)(0.975682763) - (0.975682763)^2 = t^2$$

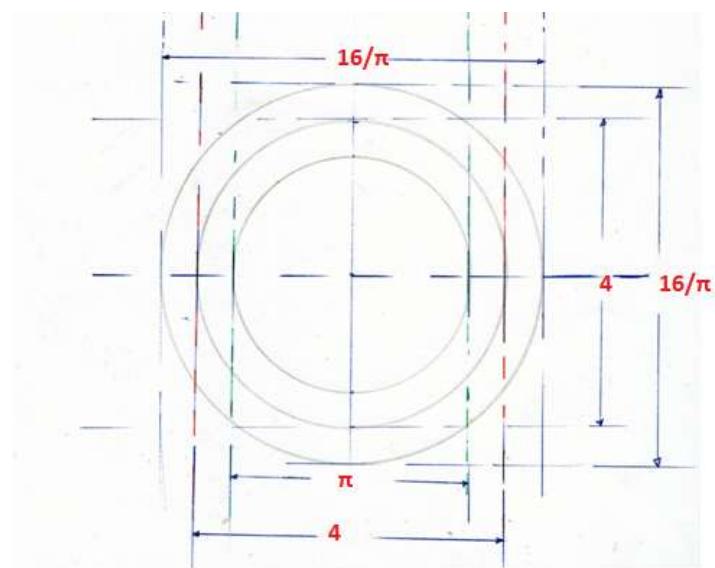
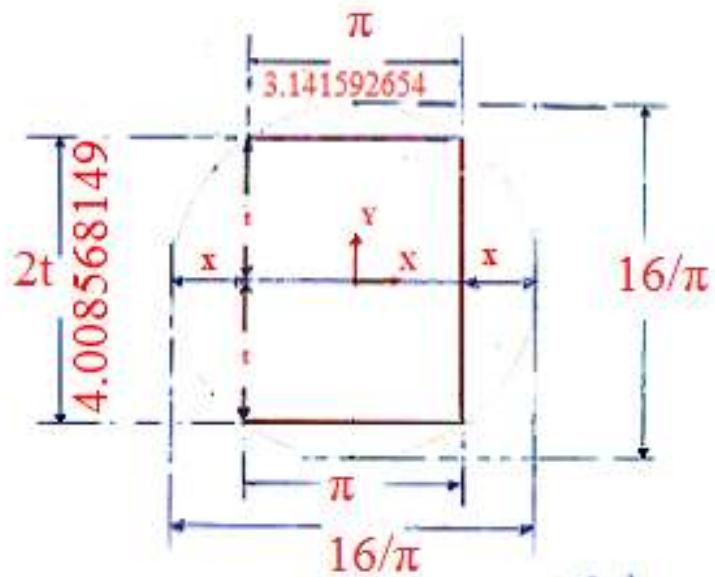
$$t^2 = 4.969111505 - 0.951956854 = 4.017154651$$

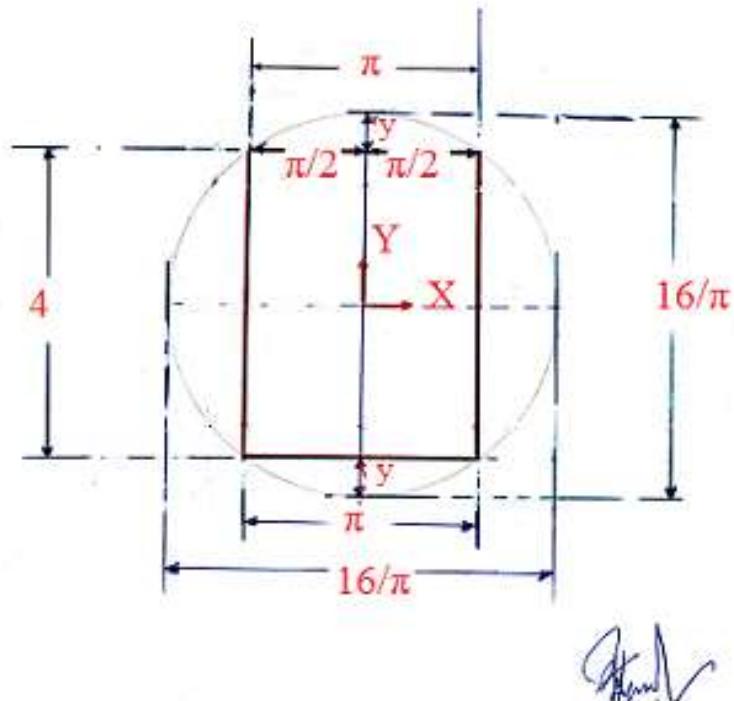
$$t^2 = 4.017154651, \quad t = 2.004284074$$

$$2t = 4.008568149$$

[https://www.wolframalpha.com/input/?i=\(16%2F3.141592654\)\(+0.975682763++\)++%E2%80%93+\(0.975682763\)%5E2+++%3D+t%5E2](https://www.wolframalpha.com/input/?i=(16%2F3.141592654)(+0.975682763++)++%E2%80%93+(0.975682763)%5E2+++%3D+t%5E2)

https://www.wolframalpha.com/input/?i=2*SQRT%7B4.0171546532081172237065860779796549396948010561524568678%7D%3D

A2a

B1

$$2y + 4 = 16/\pi$$

$$y = [8/\pi - 2]$$

$$y[(16/\pi) - y] = [\pi/2]^2, \quad [\text{application of "Power of Point Theorem"}]$$

$$y^2 - (16/\pi)y + (\pi^2)/4 = 0$$

$$[8/\pi - 2]^2 - (16/\pi)[8/\pi - 2] + (\pi^2)/4 = 0$$

$$[(8/\pi)^2 - 2 \cdot (8/\pi) \cdot 2 + 2^2] - (16/\pi)(8/\pi) + (16/\pi)(2) + [(\pi^2)/4] = 0$$

$$64/\pi^2 - 32/\pi + 4 - 128/\pi^2 + 32/\pi + \pi^2/4 = 0$$

$$\underline{64/K^2 - 32/K + 4 - 128/K^2 + 32/K + K^2/4 = 0}$$

For $\pi = K$ [compatible for Wolfram Alpha Solution]

Alternative Formulae:

$$\pi^4 + 16\pi^2 - 4^4 = 0$$

$$\pi^4 - [2*\pi^2]*[(8/\pi) - 2]^3 + 48*\pi*[(8/\pi) - 2]^2 - 256*[(8/\pi) - 2] = 0$$

For $\pi = L$ [compatible for Wolfram Alpha Solution]

$$L^4 - [2*L^2]*[(8/L) - 2]^3 + 48*L*[(8/L) - 2]^2 - 256*[(8/L) - 2] = 0$$

Real positive solution :

$$\frac{4}{\sqrt{\frac{1}{2}(\sqrt{5} + 1)}} \\ \underline{2 \sqrt{2} (-1 + \sqrt{5})} \quad [= \underline{\{4 / [\sqrt{\{\sqrt{5} + 1}\}}\}} =]$$

Note

$$[*] \quad D1 = 16/\pi, \quad D2 = 4, \quad D3 = \pi \quad \text{and} \quad D1/D2 = D2/D3 \quad \text{or} \quad [D1]*[D3] = [D2]^2$$

$$[16/\pi]: 4 = 4: [\pi]$$

$$[16/\pi]*[\pi] = 16$$

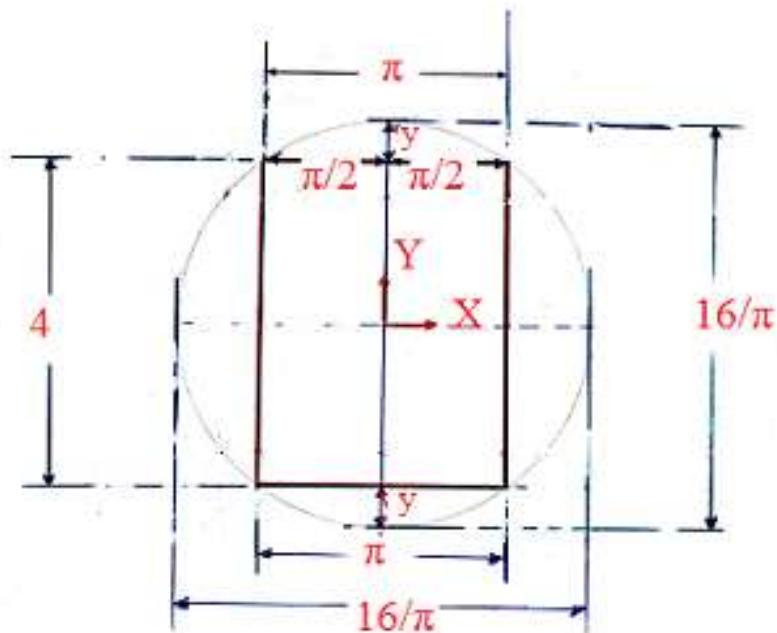
Triangular – Orthogonal- Relationship.

Ref. [Page 45]: http://www.stefanides.gr/pdf/BOOK_1997.pdf and

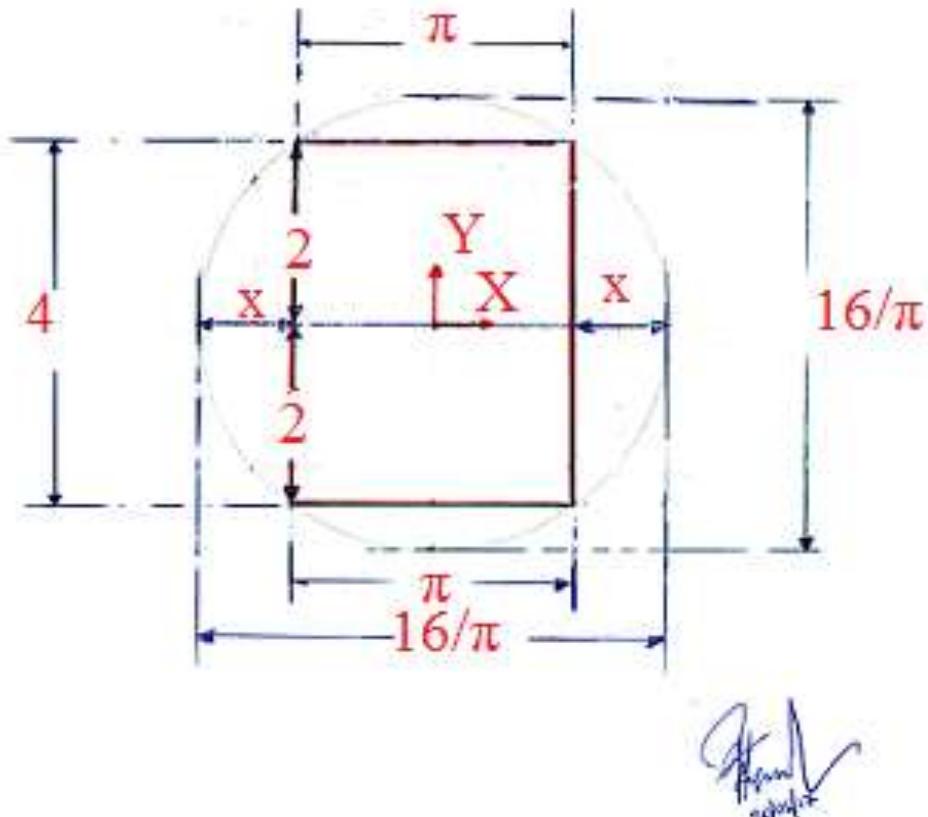
B1a

$$y = \sqrt{2(1 + \sqrt{5})} - 2$$

$$\pi = 4 / \left[\sqrt{\frac{1}{2}(\sqrt{5} + 1)} \right]$$



$$16/\pi = 4 * \left[\sqrt{\frac{1}{2}(\sqrt{5} + 1)} \right]$$

B2

$$2x + \pi = 16/\pi$$

$$x = [8/\pi - \pi/2]$$

$x[16/\pi] - x = [2]^2$, [application of “Power of Point Theorem”]

$$x^2 - (16/\pi)x + 4 = 0$$

$$[8/\pi - \pi/2]^2 - (16/\pi)[8/\pi - \pi/2] + 4 = 0$$

$$[(8/\pi)^2 - 2 \cdot (8/\pi) \cdot 2 + 2^2] - (16/\pi)(8/\pi) + (16/\pi)(2) + [(\pi^2)/4] = 0$$

$$64/\pi^2 - 32/\pi + 4 - 128/\pi^2 + 32/\pi + \pi^2/4 = 0$$

$$64/L^2 - 32/L + 4 - 128/L^2 + 32/L + L^2/4 = 0$$

For $\pi = L$ [compatible for Wolfram Alpha Solution]

<https://www.wolframalpha.com/input/?i=64%2FL%5E2++-+32%2FL+%2B4%+E2%80%93+128%2FL%5E2%+2B+32%2FL+%2BL+%5E2%2F4%+3D+0>

Alternative Formulae:

$$\pi^4 + 16\pi^2 - 4^4 = 0$$

$$\pi^4 - [2*\pi^2]*[(8/\pi) - 2]^3 + 48*\pi*[(8/\pi) - 2]^2 - 256*[(8/\pi) - 2] = 0$$

For $\pi = M$ [compatible for Wolfram Alpha Solution]

$$M^4 - [2*M^2]*[(8/M) - 2]^3 + 48*M*[(8/M) - 2]^2 - 256*[(8/M) - 2] = 0$$

Real positive solution :

$$\frac{4}{\sqrt{\frac{1}{2}(\sqrt{5} + 1)}} \\ \underline{2 \sqrt{2 (-1 + \sqrt{5})}} \quad \{ = \{ 4/\sqrt{\sqrt{5} + 1} \} \}$$

$$x = 2 \sqrt{\sqrt{5} - 2}$$

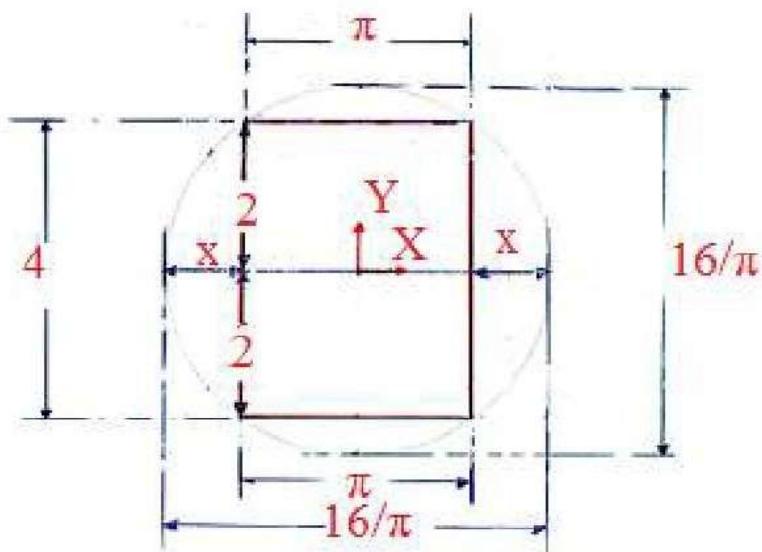
Computed by Wolfram|Alpha

B2a

$$x = 2\sqrt{\sqrt{5} - 2}$$

Computed by Wolfram|Alpha

$$\pi = 4/\left[\sqrt{\frac{1}{2}(\sqrt{5} + 1)}\right]$$



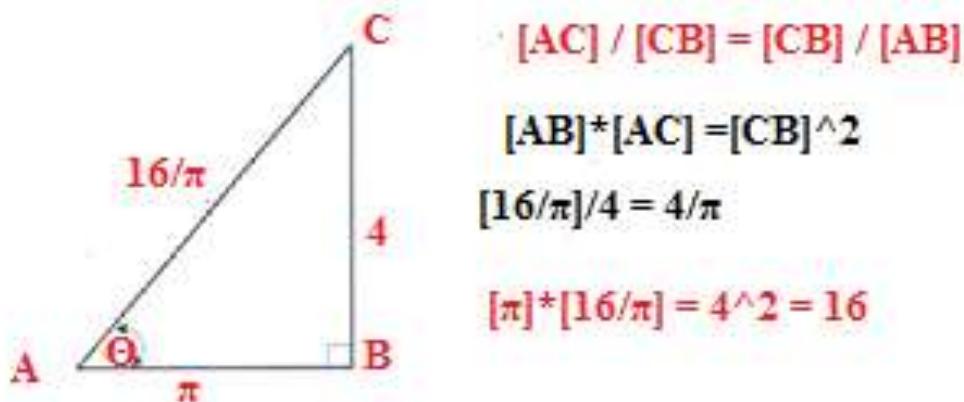
$$16/\pi = 4 * \left[\sqrt{\frac{1}{2}(\sqrt{5} + 1)} \right]$$

Note

[*] $D1 = 16/\pi$, $D2 = 4$, $D3 = \pi$ and $D1/D2 = D2/D3$ or $[D1]*[D3] = [D2]^2$

$$[16/\pi]: 4 = 4: [\pi]$$

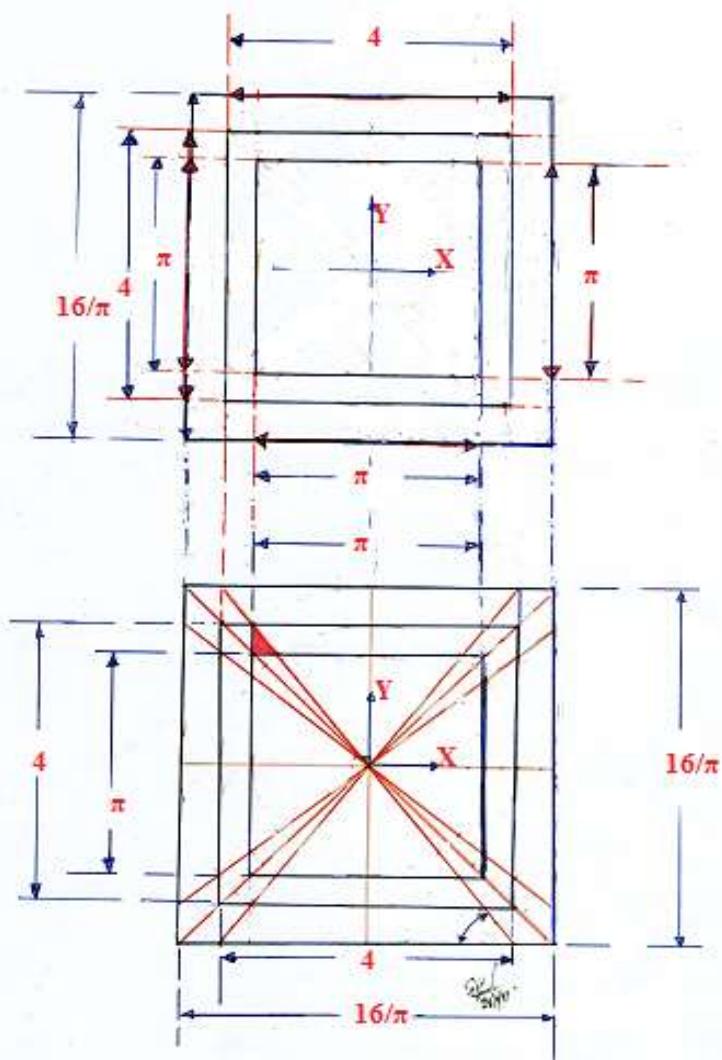
$$[16/\pi]*[\pi] = 16$$

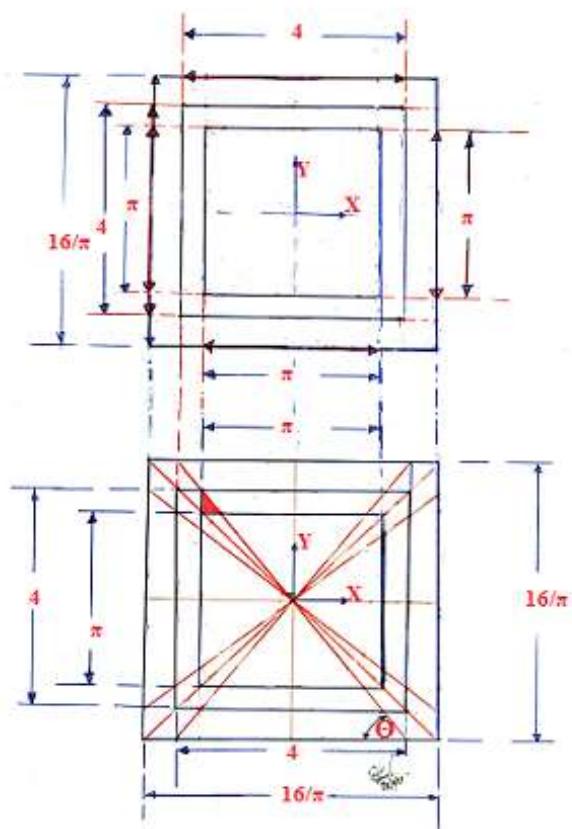


Triangular – Orthogonal- Relationship.

Ref: [Page 45]: http://www.stefanides.gr/pdf/BOOK_1997.pdf

Forms of Circles Related to Squares and



**RATIOS**

$$16/\pi : 4 = 4 : \pi = 4/\pi$$

$$[16/\pi]/[4] = [4]/[\pi]$$

$$[16/\pi]^*[\pi] = [4]^*[4] = 4^2 = 16$$

$$\tan(\Theta) = [16/\pi]/4 = 4/\pi$$

For $\pi = 3.141592654$,

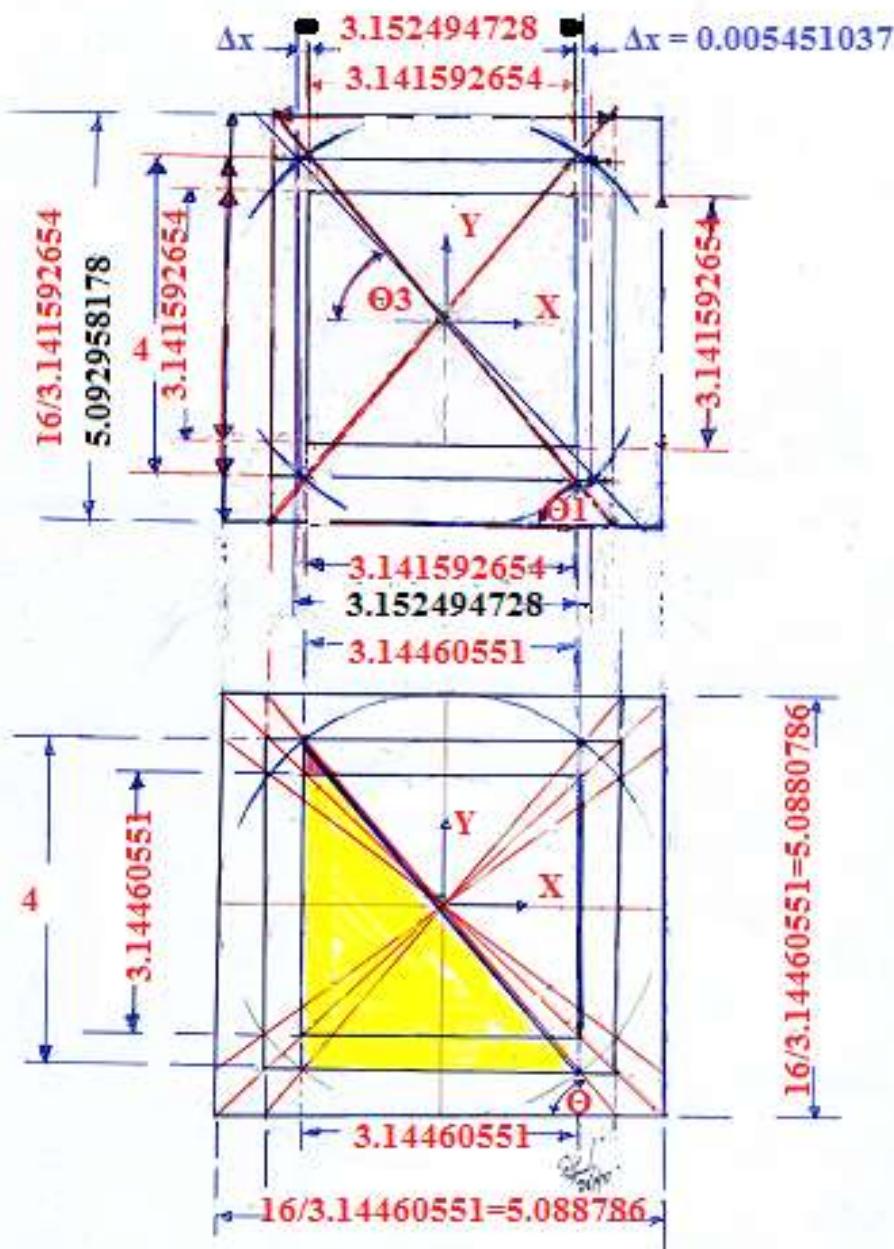
$$\tan(\Theta) = 4/3.141592654 = 1.273239545, \text{ and}$$

$$\Theta = 51.85397401 \text{ deg.}$$

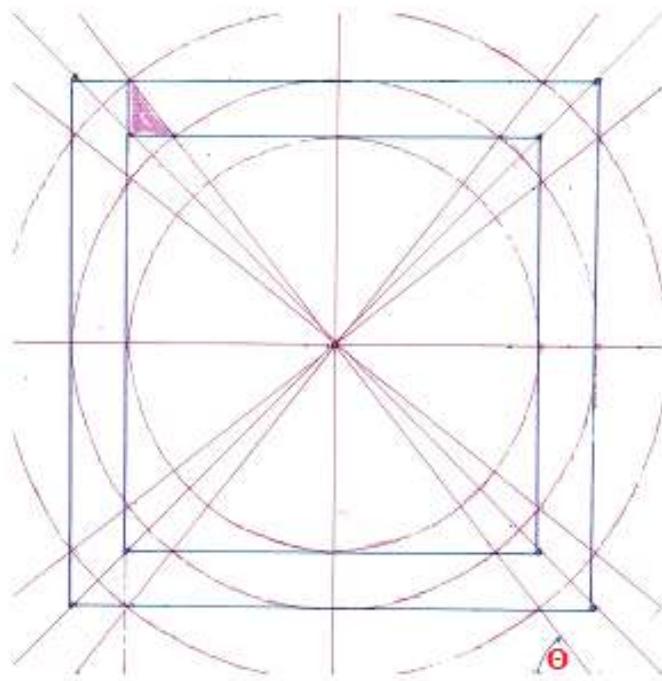
$$\text{For } \pi = 4/\sqrt{[5+2\sqrt{5}]}/2 = 3.14460551$$

$$\tan(\Theta) = 4/3.14460551 = 1.27201965, \text{ and}$$

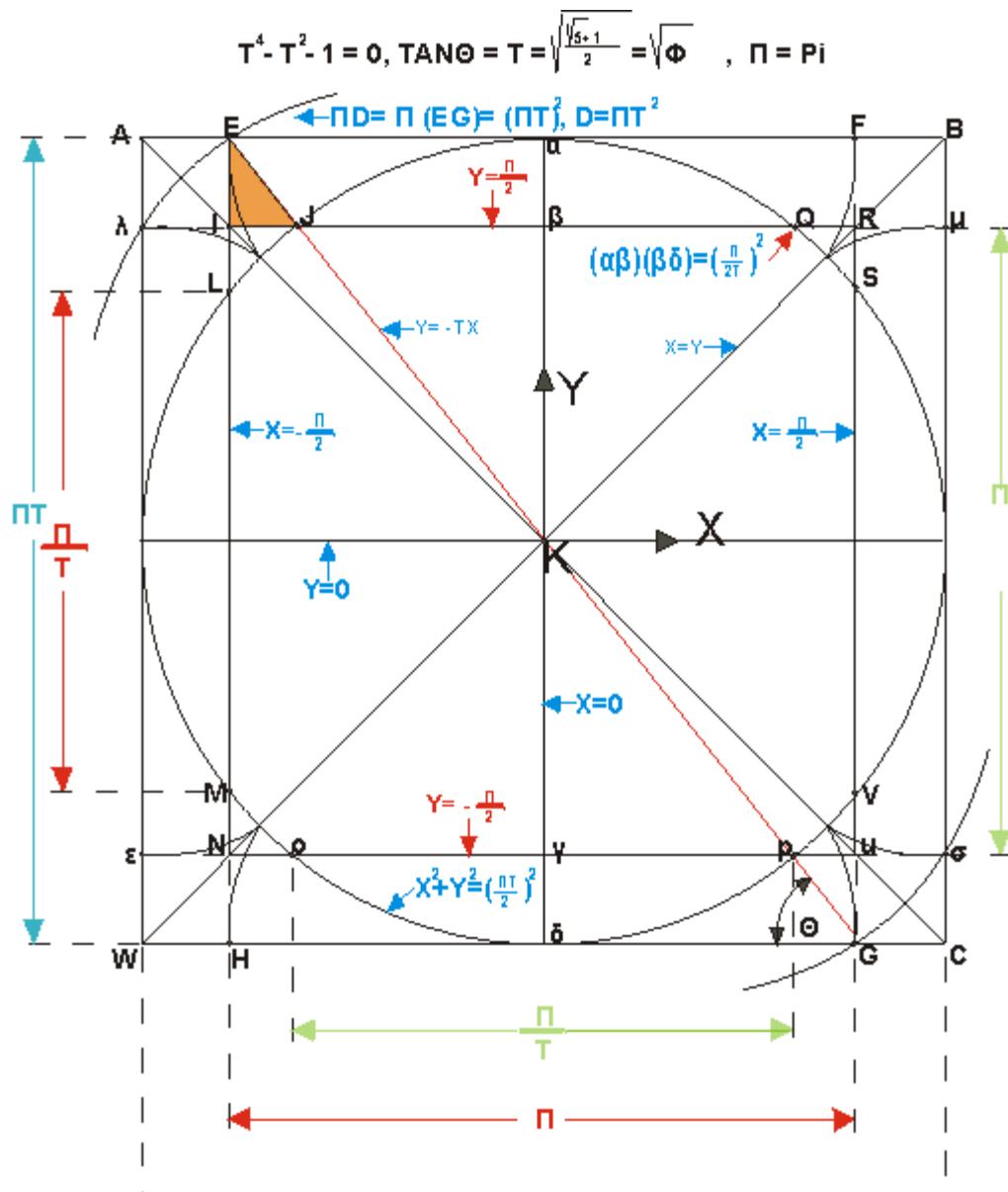
$$\Theta = 51.82729238 \text{ deg.}$$



$$4 / \left[\sqrt{\frac{1}{2}(\sqrt{5} + 1)} \right] = 3.14460551$$



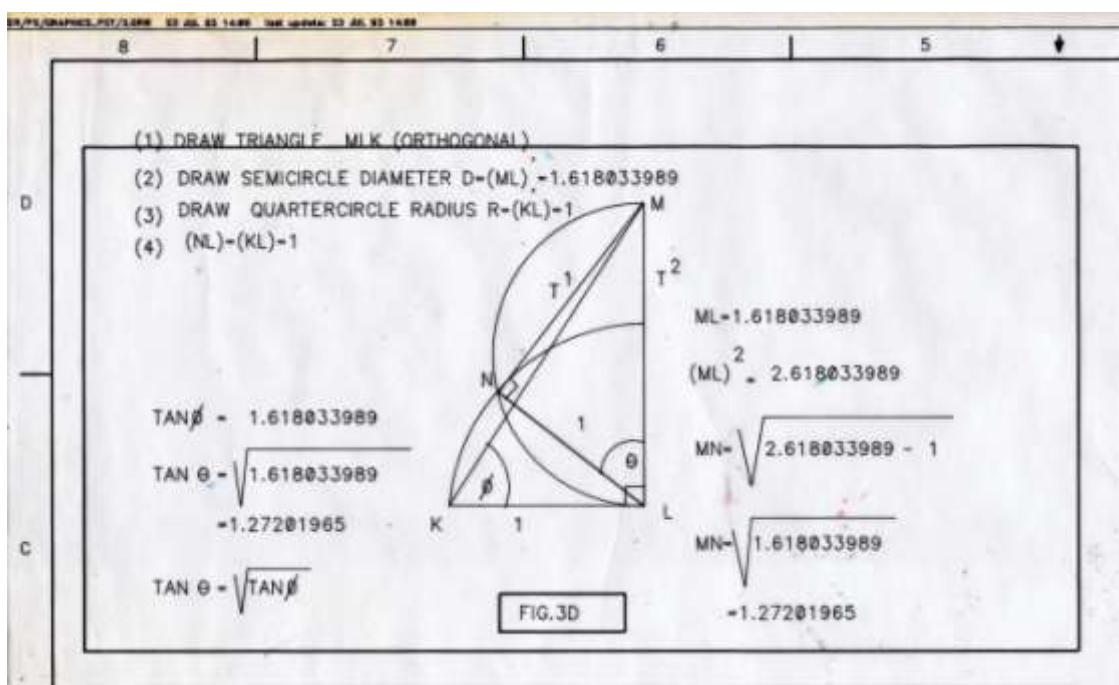
<http://www.stefanides.gr/Html/quad.html>



COPYRIGHT ©, SECUNDI MILLENNII FINIS, P.C. STEFANIDES

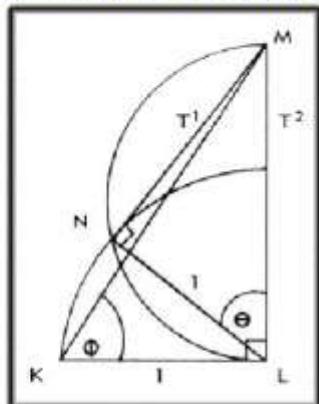
http://www.stefanides.gr/Html/theo_circle.html

RELEVANT PERFORMED WORK



http://www.stefanides.gr/pdf/BOOK_1997.pdf

Geometric Mean Ratio (T) by Ruler and Compass



- (1) DRAW TRIANGLE MLK (ORTHOGONAL)
- (2) DRAW SEMICIRCLE DIAMETER D = (ML) = 1.618033989
- (3) DRAW QUARTERCIRCLE RADIUS R = (KL) = 1
- (4) (NL) = (KL) = 1

$$\tan \Phi = 1.618033989$$

$$\tan \Theta = \sqrt{1.618033989}$$

$$= 1.27201965$$

$$\tan \Theta = \sqrt{\tan \Phi}$$

$$T^4 \cdot T^2 \cdot 1 = 0$$

$$ML = 1.618033989 = T^2$$

$$(ML)^2 = 2.618033989$$

$$MN = \sqrt{2.618033989 - 1}$$

$$MN = \sqrt{1.618033989} = T$$

$$T = 1.27201965$$

ΓΕΩΜΕΤΡΙΚΟΣ ΜΕΣΟΣ ΑΝΑΛΟΓΟΣ (T) ΜΕ ΚΑΝΟΝΑ ΚΑΙ ΔΙΑΒΗΤΗ

SQUARE ROOT OF THE GOLDEN NUMBER (BY THE USE OF RULER AND COMPASS)

Diagram illustrating the geometric construction of the square root of the golden ratio using a circle and a ruler.

Given a circle with center B, a horizontal chord AC is drawn. A vertical chord BD is drawn perpendicular to AC at point B. A second vertical chord BE is drawn from B to the right, intersecting the circle at E. Chords AD and CE are also drawn. The radius AB is labeled 1. The segments BC and BD are labeled $\frac{1}{T^2}$. The segments AD and AE are labeled $\frac{1}{T}$. The angle θ is shown at vertex B. The angle ϕ is shown at vertex E. Right angles are indicated at D and E.

Mathematical derivations:

$$T = \sqrt{\frac{\sqrt{5} + 1}{2}}$$

$$T^2 = \frac{\sqrt{5} + 1}{2}$$

$$T^4 - 1 - T^2$$

$$1 - \frac{1}{T^4} - \frac{1}{T^2}$$

$$\sqrt{1 - \frac{1}{T^4}} - \frac{1}{T}$$

$$AB = 1$$

$$BC = \frac{1}{T^2} = BD$$

$$AD = \frac{1}{T}$$

$$\tan \theta = T$$

$$T^4 - T^2 - 1 = 0$$

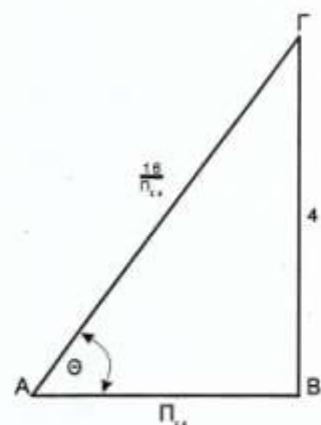
$$(BD) \cdot (AB) = (AD)^2$$

$$\tan \phi = T^2 (-1/(1/(T^2)))$$

FIG. 3A

FIG. 3B

FIG. 3C



$$\Pi_{\text{Ex}}^4 + 4^2 \cdot \Pi_{\text{Ex}}^2 - 4^4 = 0$$

$$\Pi_{\text{Ex}}^2 + 4^2 \cdot \frac{4^4}{\Pi_{\text{Ex}}^2} = 0$$

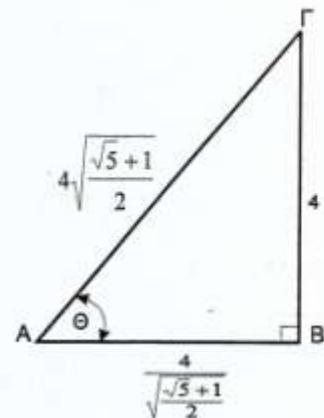
$$\Pi_{\text{Ex}}^2 + 4^2 = \frac{4^4}{\Pi_{\text{Ex}}^2}$$

$$\Pi_{\text{Ex}}^2 + 4^2 = \left(\frac{4^2}{\Pi_{\text{Ex}}}\right)^2$$

$$\tan \Theta = \frac{4}{\Pi_{\text{Ex}}}$$

$$\tan \Theta = \frac{4}{\sqrt{\frac{\sqrt{5}+1}{2}}}$$

$$\tan \Theta = \sqrt{\frac{\sqrt{5}+1}{2}}$$



$$\Delta IA \text{ (FOR)} 2\pi R = 4 = BG = K$$

$$R = \frac{4}{2\pi} \quad R = \frac{2}{\pi}$$

$$\Delta IA \text{ (FOR)} \pi = \Pi_{IX} = \frac{4}{\sqrt{\frac{\sqrt{5}+1}{2}}} = AB$$

$$4X\Pi_{IX} R^2 = 4X\Pi_{IX} \left(\frac{2}{\Pi_{IX}}\right)^2$$

$$4X\Pi_{IX} R^2 = \frac{16}{\Pi_{IX}} = \frac{16}{\frac{4}{\sqrt{\frac{\sqrt{5}+1}{2}}}} = 4\sqrt{\frac{\sqrt{5}+1}{2}} = AG$$

$$\tan \theta = \sqrt{\frac{\sqrt{5}+1}{2}} = 1.27201965$$

$$\Delta IA \text{ (FOR)} 2\pi R = 3.996167588 = BG = K$$

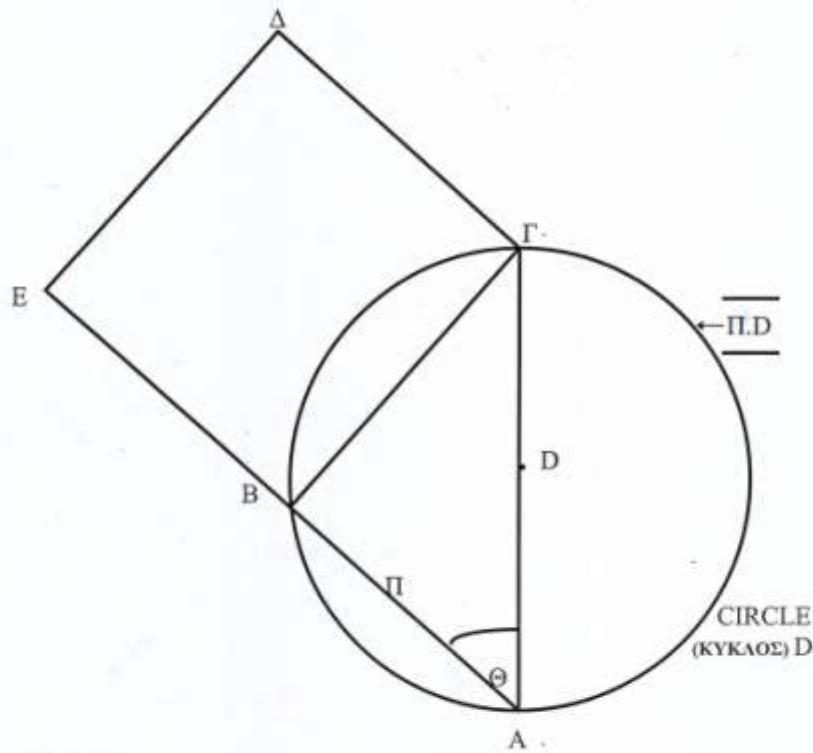
$$\pi = 3.141592654 = AB$$

$$AG = 5.083203694$$

$$\tan \theta = 1.27201965$$

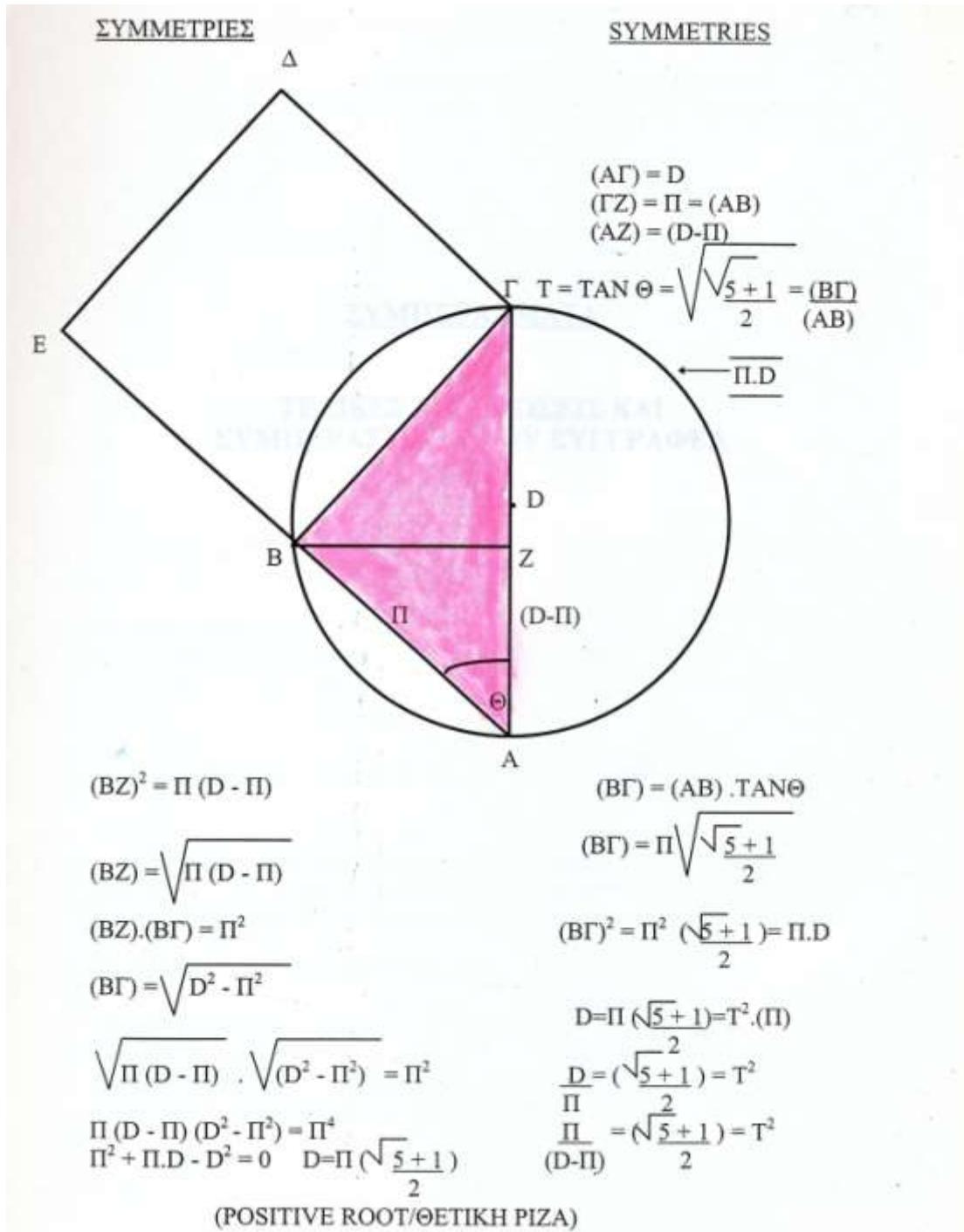
$$\tan \Theta = T = \sqrt{\frac{\sqrt{5} + 1}{2}}$$

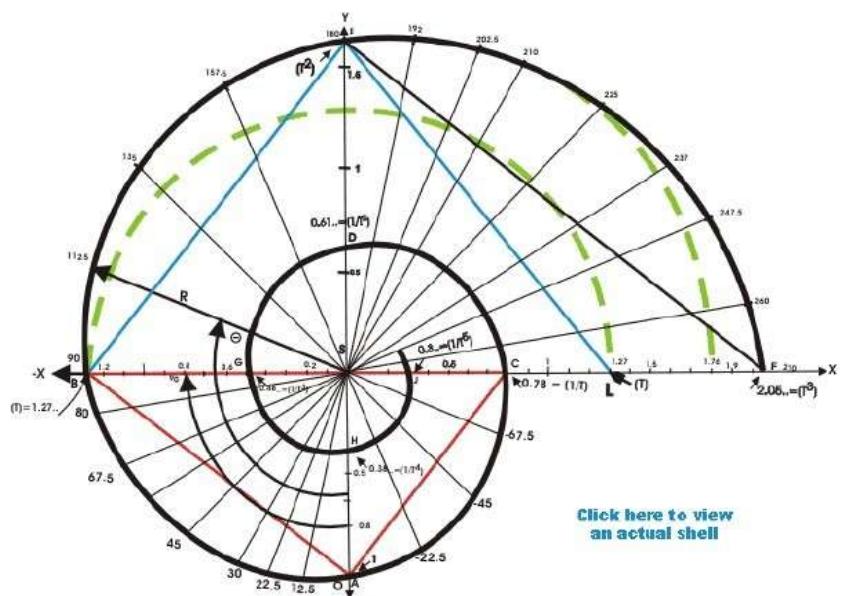
$(BG) = (\Gamma\Delta) = (\Delta E) = (EB)$
 (SQUARE / ΤΕΤΡΑΓΩΝΟ ΒΓΔΕΒ)



$(AB) = \Pi$
 $(AD) = D$
 $(AB) \cdot (AD) = \Pi \cdot D = (BG) \cdot (\Gamma\Delta) = (BG)^2$
 $\Pi \cdot D = \text{ΠΕΡΙΦΕΡΕΙΑ ΚΥΚΛΟΥ}$
 = CIRCLE CIRCUMFERENCE
 $(BG) \cdot (\Gamma\Delta) = \text{ΕΜΒΑΔΟΝ (ΒΓΔΕΒ) ΤΕΤΡΑΓΩΝΟΥ}$
 = AREA OF (ΒΓΔΕΒ) SQUARE

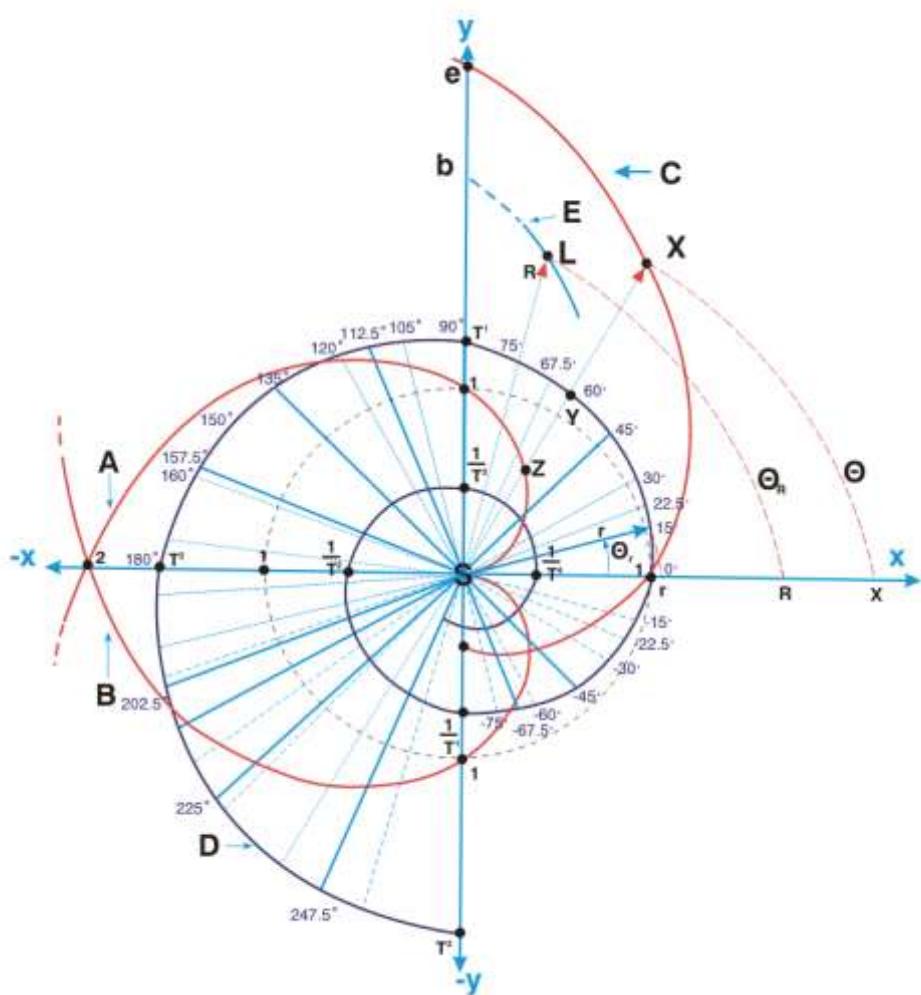
http://www.stefanides.gr/pdf/BOOK_1997.pdf



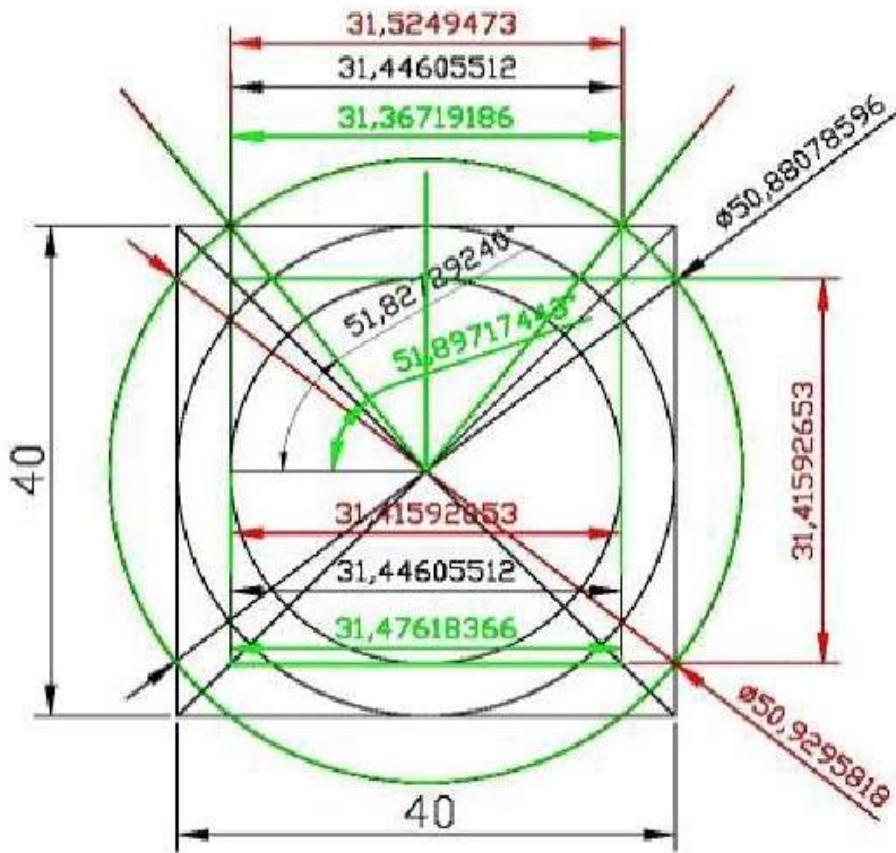


<http://www.stefanides.gr/Html/Nautilus.html>

http://www.stefanides.gr/Html/why_logarithm.html



http://www.stefanides.gr/pdf/BOOK%20_GRSOGF.pdf



QUADRATURE OF CIRCLE

MICROCOSMOS Geometrically Related to the MACROCOSMOS

“Nested Circles, Squares, Triangles”

Quadrature of the Circle, Compass and Ruler - NOVEL CONCEPT - via “The Quadrature Triangle”

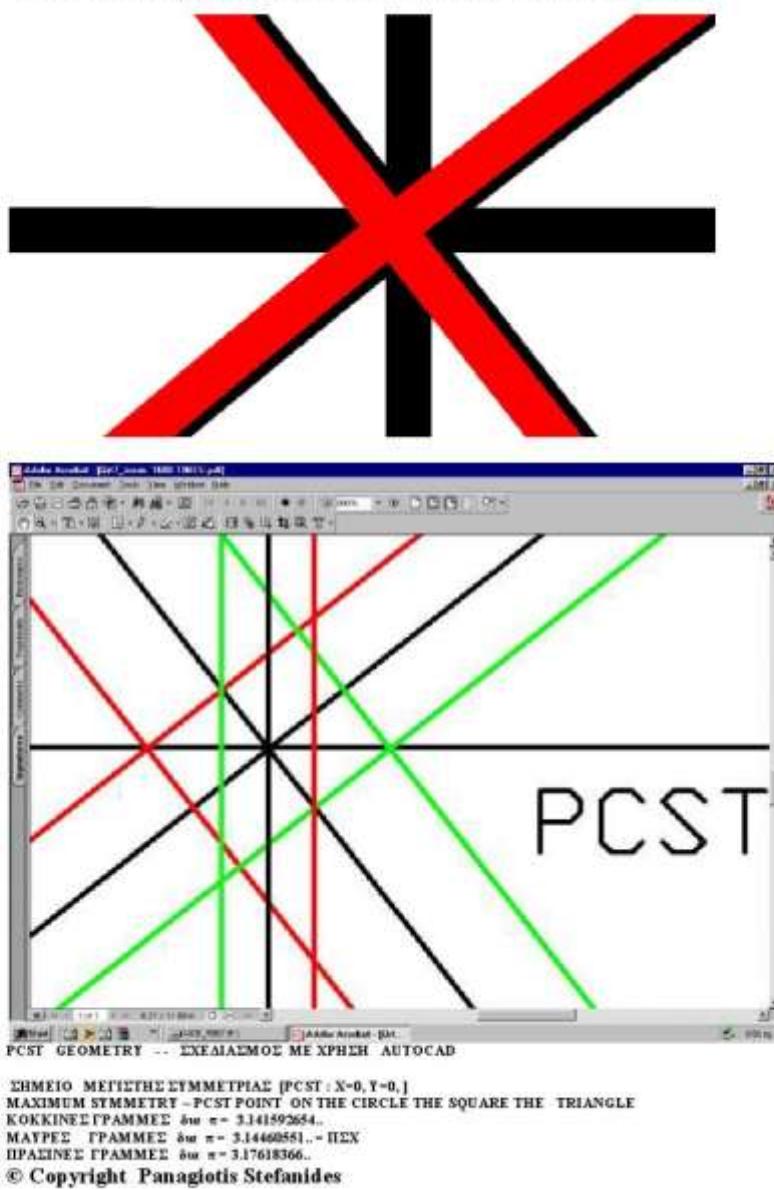
CONFIGURATION EXHIBITING MAXIMUM SYMMETRY

For Value of $\pi = 4 / \sqrt{\varphi}$ [= 3.14460551..]

Circumference of Circle [$D = 40 * \sqrt{\varphi} = 50.88078596..$] = Square [Side 40] Perimeter, and
Product $40 * D$ = Area of this Circle = A Square area of Side 45.11353941..

Geometry Design and Vector Definition of Coordinates by P.Stefanides, <http://www.stefanides.gr>
AutoCad Computerized Drawing by Dr. J. Kandylas

PCST GEOMETRY Copyright © 1986-2012 Eur Ing P.Stefanides CEng MIET - AUTOCAD DRAWING

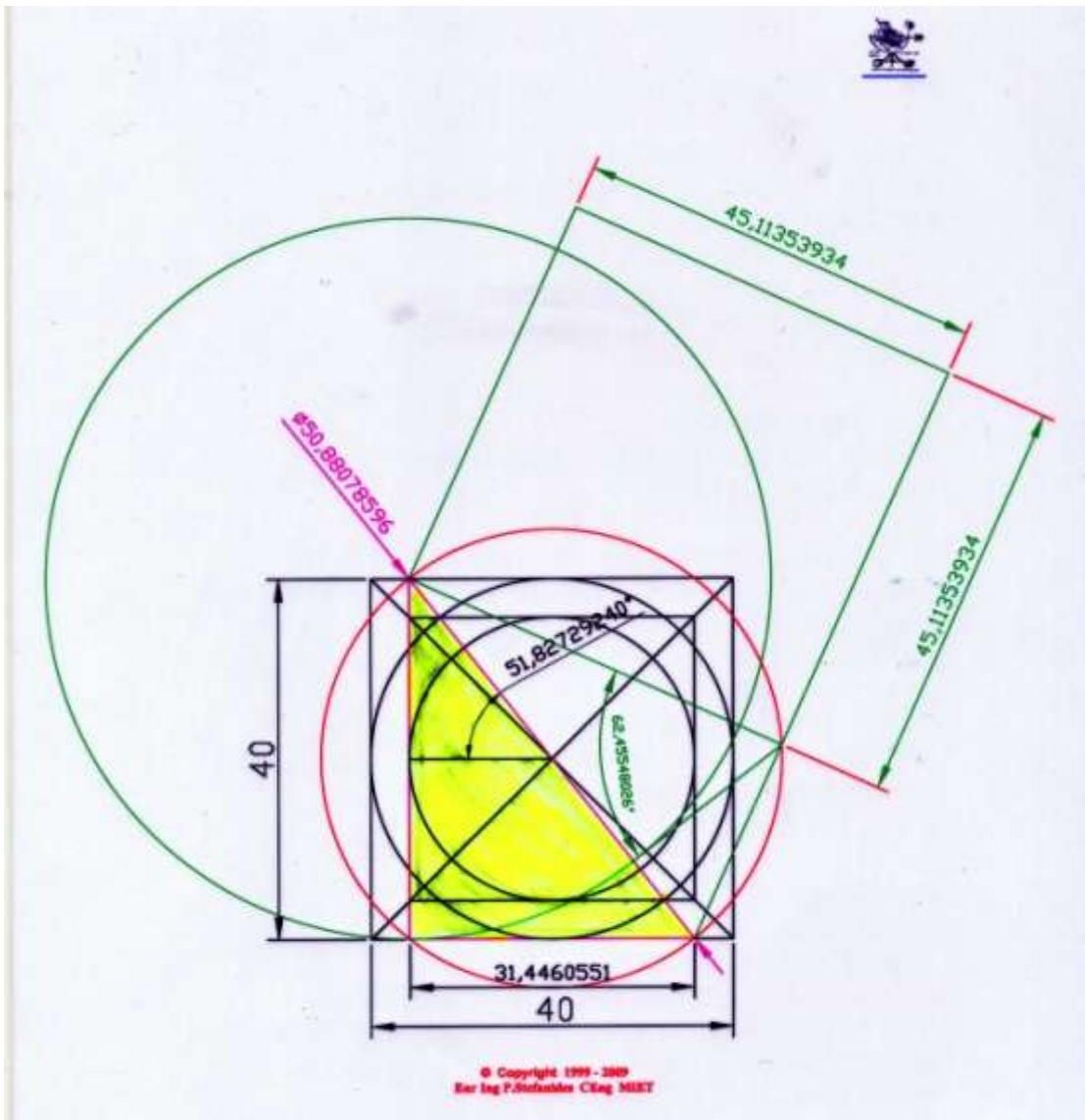


http://www.stefanides.gr/pdf/2012_Oct/PHOTO_09_PCST_GEOMETRY.pdf

<https://www.linkedin.com/pulse/microcosmos-geometrically-related-macrocosmos-panagiotis-stefanides>

https://www.researchgate.net/publication/295387242_O3

https://www.researchgate.net/publication/314626390_Triangular_and_Circular_Relationships



$$\text{For: } \pi = 4 / \sqrt{\varphi}$$

Quadrature of the Circle, Compass and Ruler - NOVEL CONCEPT - via "The Quadrature Triangle"

$$D = 40 * \sqrt{\varphi} = 50.8807859.., \quad \pi^* D = 4 * 40 = 160 = \text{Square [Side 40] Perimeter} =$$

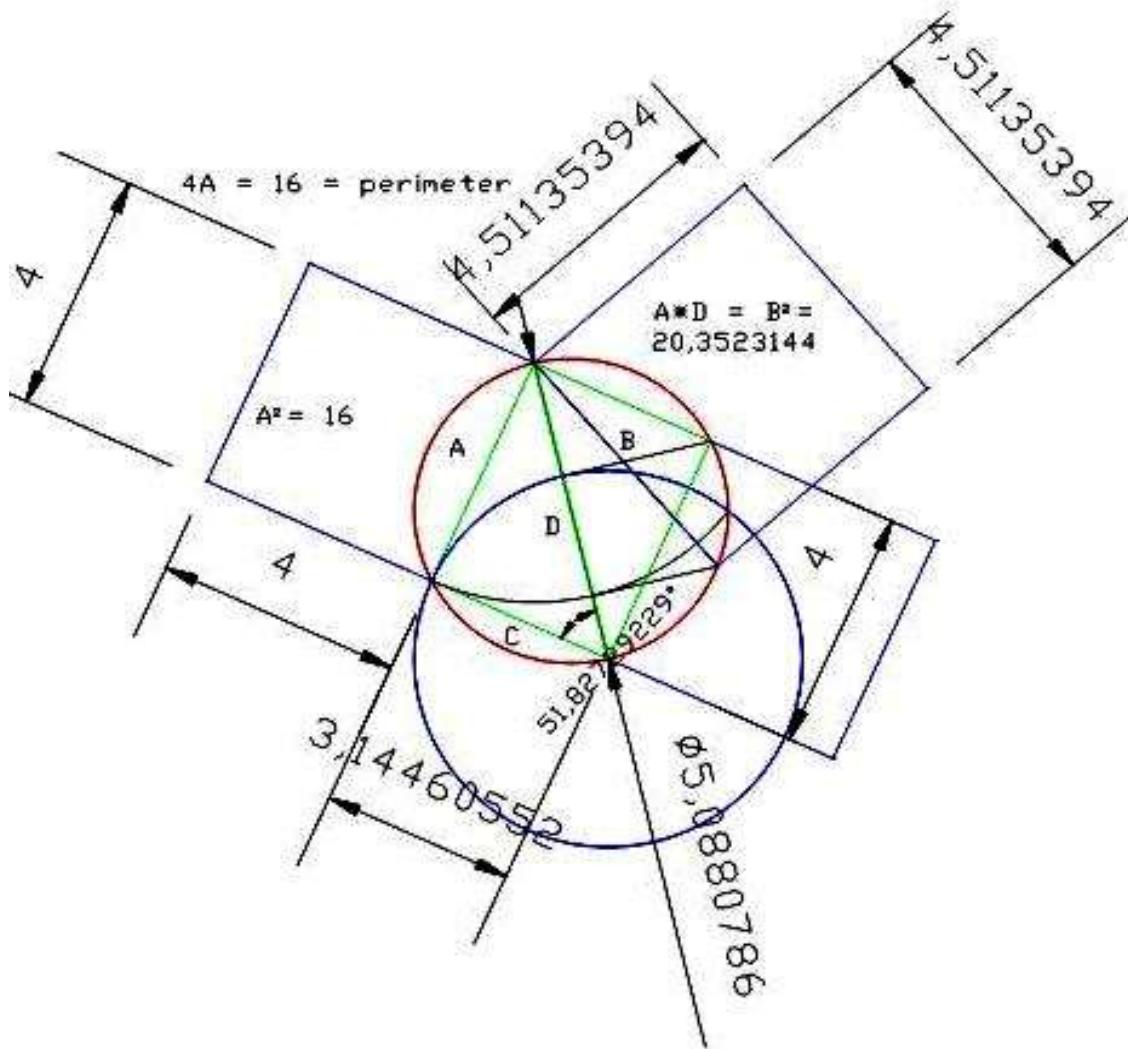
$$= \text{Circle [Red] Circumference}, [\pi/4]^* D^2 = 1600 * \sqrt{\varphi} = [45.113539..]^2 = \text{Circle [Red] Area} = \\ = \text{Square [Side 45.113539..] Area} = 2035.2314..$$

Geometry Design and Vector Definition of Coordinates by P. Stefanides, <http://www.stefanides.gr>

Auto Cad Computerized Drawing by Dr. J. Kandylas

© Copyright 1987 - 2014 Eur Ing Panagiotis Chr. Stefanides CEng MIET

<https://www.linkedin.com/pulse/exposed-mathematical-art-panagiotis-stefanides-2016-stefanides>



© Copyright 1986, 1999, 2010
Eur Ing P.Stefanides CEng MIET
11 June 2010
11 Years after the Spiroïd Definition of Logarithm

$$\text{For: } \pi = 4/\sqrt{\varphi}$$

Quadrature of the Circle, Compass and Ruler - NOVEL CONCEPT - via "The Quadrature Triangle"

$$D = 4 * \sqrt{\varphi} = 5.0880786\ldots, [\text{Red Circle}], \pi^* D = 4 * 4 = 16 = \text{Square [Side 4] Perimeter} = \text{Circle [Red]}$$

$$\begin{aligned} \text{Circumference, } [\pi/4]^* D^2 &= 16 * \sqrt{\varphi} = [4.51135394\ldots]^2 = \text{Circle [Red] Area} = \\ &= \text{Square [Side 4.51135394\ldots] Area} = 20.3523144.. \end{aligned}$$

Geometry Design and Vector Definition of Coordinates by P.Stefanides, <http://www.stefanides.gr>

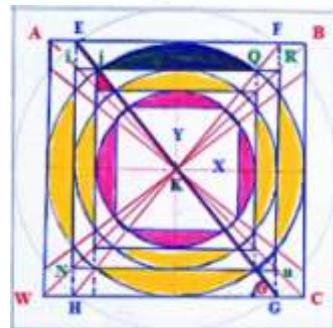
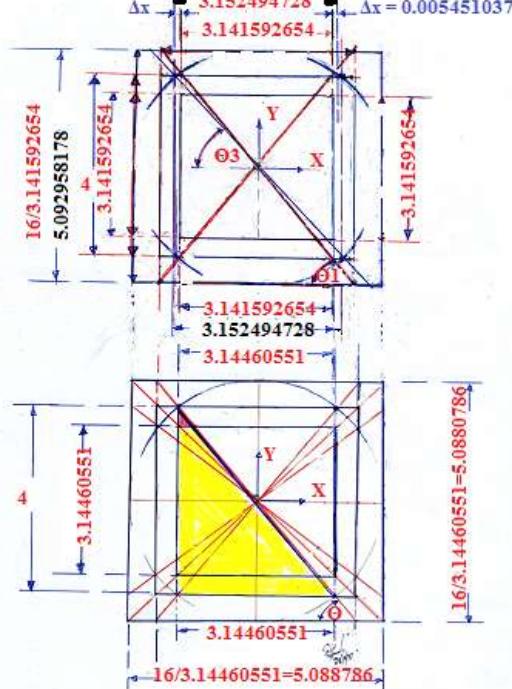
AutoCad Computerized Drawing by Dr. J. Kandylas

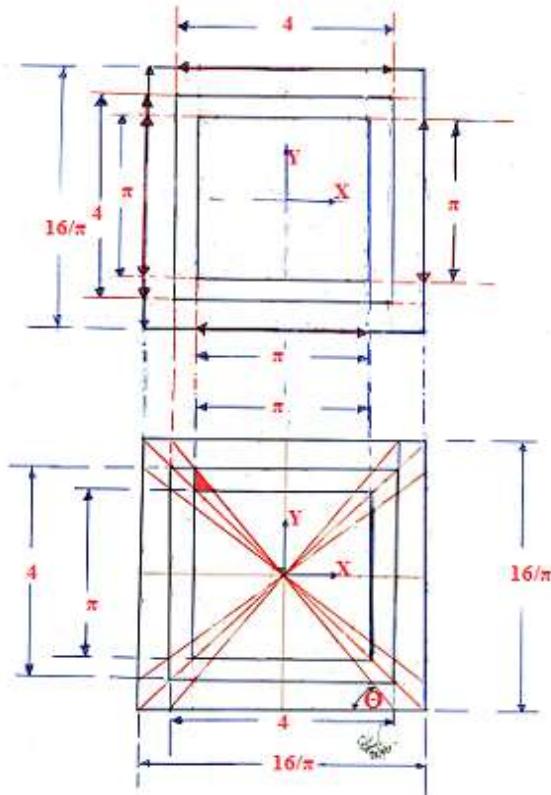
© Copyright 1987 - 2014 Eur Ing Panagiotis Chr. Stefanides CEng MIET

<https://www.linkedin.com/pulse/bridges-2014-pstefanides-exhibits-panagiotis-stefanides/>



Three Concentric Squares In Common Ratio With Circles and Triangles Compass and Ruler Interstructures





RATIOS

$$16/\pi : 4 = 4:\pi = 4/\pi$$

$$[16/\pi]/[4] = [4]/[\pi]$$

$$[16/\pi]*[\pi] = [4]*[4] = 4^2 = 16$$

$$\tan(\Theta) = [16/\pi]/4 = 4/\pi$$

$$\text{For } \pi = 3.141592654,$$

$$\tan(\Theta) = 4/3.141592654 = 1.273239545, \text{ and}$$

$$\Theta = 51.85397401 \text{ deg.}$$

$$\text{For } \pi = 4/\sqrt{[5+2\sqrt{5}]/2} = 3.14460551$$

$$\tan(\Theta) = 4/3.14460551 = 1.27201965, \text{ and}$$

$$\Theta = 51.82729238 \text{ deg.}$$

Squares' Sides : $S_1 = [16/\pi]$, $S_2 = [4]$, $S_3 = [\pi]$

Squares' Sides' Ratios : $[16/\pi]:[4]=[4]:[\pi]=[4/\pi]$

$$[S_1]/[S_2] = [S_2]/[S_3]$$

$$[S_1]*[S_3] = [S_2]^2$$

$$[S_2]^2 + [S_3]^2 = [S_1]^2$$

$$[4]^2 + [\pi]^2 = [16/\pi]^2$$

$$[4^2]*[\pi^2] + [\pi]^4 = [16]^2$$

$\pi^4 + 16\pi^2 - 256 = 0$ For $x = \pi$ [for WolframAlpha solution]:

$$x^4 + 16x^2 - 256 = 0$$

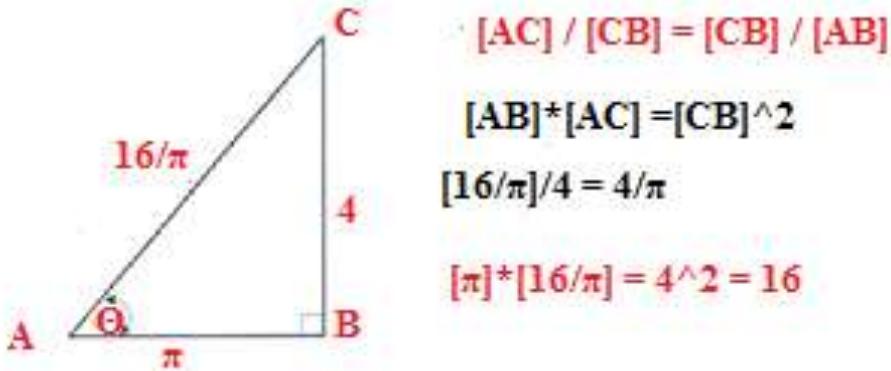
<https://www.wolframalpha.com/input/?i=x%5E4+%2B16x%5E2+-256+%3D0>

$$x = 2 \sqrt{2(\sqrt{5} - 1)}$$

Computed by Wolfram|Alpha

$$= 3.14460551\dots$$

$$= 4 / \left[\sqrt{\frac{1}{2}(\sqrt{5} + 1)} \right]$$



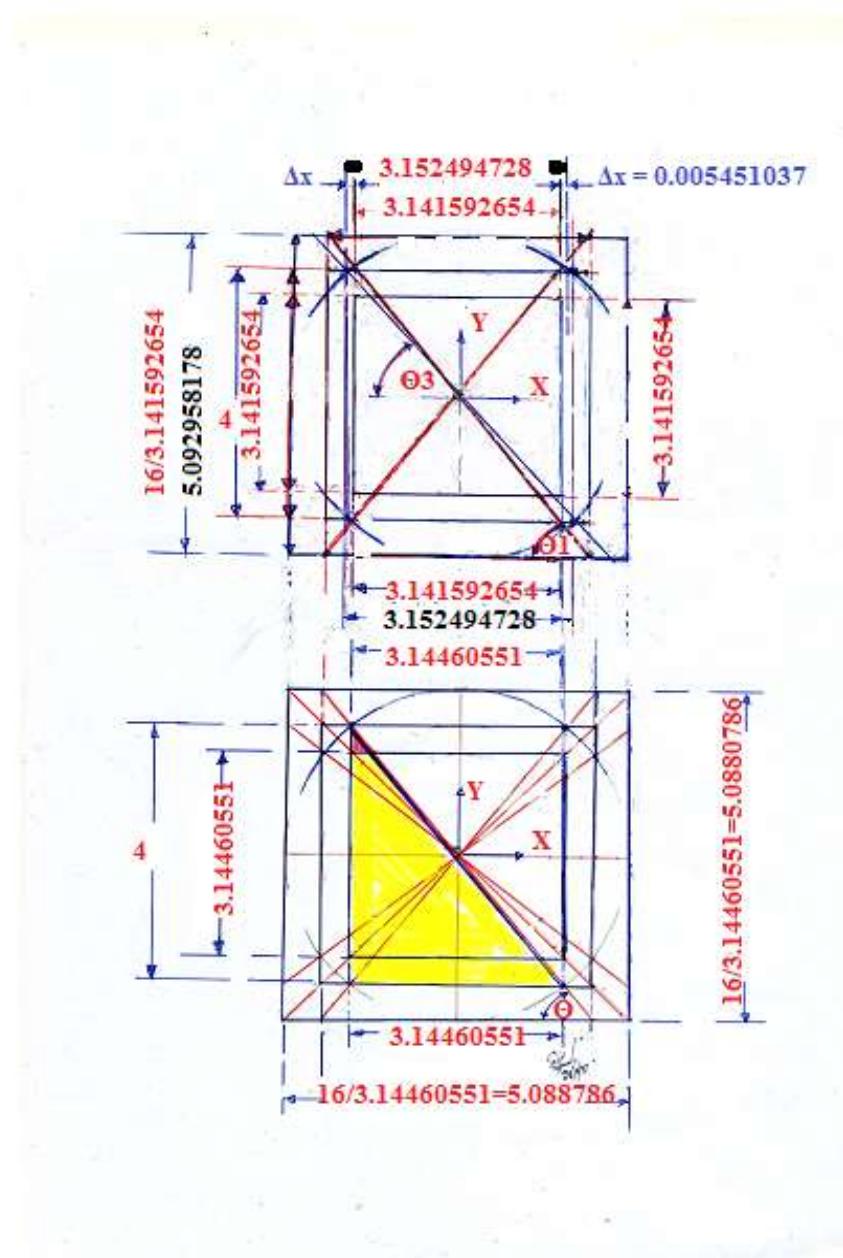
$$\tan[\Theta] = [4/3.14460551] = \sqrt{\frac{1}{2}(\sqrt{5} + 1)} = 1.27201965$$

$$\Theta = \text{ArcTan}\left[\sqrt{\frac{1}{2}(\sqrt{5} + 1)}\right]$$

$$\Theta = 51.82729238 \dots \text{ Deg}$$



Triangular and Circular Relationships



[16/3.14460551]=5.0880786 {= Circle circumference [16] diameter crossing parallel sides of square perimeter [16] - for $\pi = 3.14460551$ }

[16/3.141592654]= 5.092958178 {Circle circumference [16] diameter crossing parallel sides of square perimeter [16] - for $\pi = 3.141592654$ }

From Pythagoras Theorem

$$\text{SQRT}\{[5.092958178]^2 - [4]^2\} = 3.152494728$$

$$\begin{aligned} \text{SQRT}\{[5.0880786]^2 - [4]^2\} &= 3.14460551 \\ 3.152494728 - 3.141592654 &= 0.010902074 = 2\Delta x \end{aligned}$$

$$\Delta x = 0.005451037$$

Trigonometrically

$$5.092958178[\cos(\Theta_3)] - 3.141592654 = 2\Delta x$$

$$\sin(\Theta_3) = 4/[5.092958178] = 0.785398164$$

$$\Theta_3 = \text{ArcSin}[0.785398164] = 51.75751853.. \text{ Deg}$$

$$[\cos(\Theta_3)] = [\cos(51.75751853)] = 0.618990892$$

$$5.092958178[0.618990892] = 3.152494728$$

$$3.152494728 - 3.141592654 = 2\Delta x = 0.010902074$$

$$\Delta x = 0.005451037$$

https://www.researchgate.net/publication/311156470_No_Detection_of Imperfection_of_Circle_Challenges_the_Transcendence_of_pi_By_Panagiotis_Stefanides

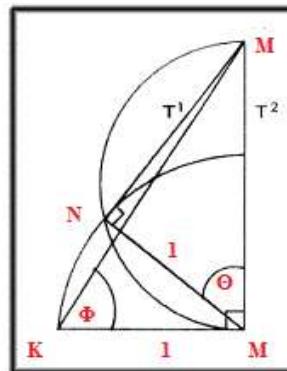
<https://www.linkedin.com/pulse/detection-imperfection-circle-challenges-%CF%80-panagiotis-stefanides>

<https://www.linkedin.com/pulse/chords-sectors-squares-circumscribed-subscribed-%CF%80-value-stefanides>

Drawing of Concentric Squares and Fitting Trianglularly Concentric Circles

Drawing by “ruler and compass” the Orthogonal Triangle Angle Θ , of Tangent [T]:

$$T = \sqrt{\frac{1}{2}(\sqrt{5} + 1)} = \sqrt{\Phi}$$



$$\tan \Phi = 1.618033989$$

$$\tan \Theta = \sqrt{1.618033989}$$

$$= 1.27201965$$

$$\tan \Theta = \sqrt{\tan \Phi}$$

$$T^4 - T^2 - 1 = 0$$

$$ML = 1.618033989 = T^2$$

$$(ML)^2 = 2.618033989$$

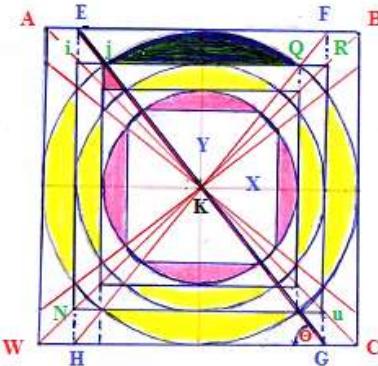
$$MN = \sqrt{2.618033989 - 1}$$

$$MN = \sqrt{1.618033989} = T$$

$$T = 1.27201965$$

$$T = \sqrt{\frac{1}{2}(\sqrt{5} + 1)} = \sqrt{\Phi}$$

<http://www.stefanides.gr/Html/gmr.html>



http://www.stefanides.gr/Html/theo_circle.html

RULER and COMPASS constructions

1. A Square [ABCW] of Perimeter [16] units, Side Length [4] units is drawn.
2. Diagonals [AC] and [BW] are drawn fixing its Center point K [x=0, y=0], on X,Y axes [drawn for reference].
3. A Square Inscribed Circle of Diameter [4] and Circumference $[4\pi]$ is drawn.
4. Line [EG] is drawn, passing Center point K, with Slope $\sqrt{\frac{1}{2}(\sqrt{5} + 1)}$.
Slope = Tan [Θ] = $\sqrt{\frac{1}{2}(\sqrt{5} + 1)}$ [= 1.27201965].

Similarly Line [FH] drawn .

$$[EF]=[HG] = [EH]/\tan[\Theta] = 4/\left[\sqrt{\frac{1}{2}(\sqrt{5} + 1)}\right] = \pi \quad [\text{for } \pi = 3.14460551].$$

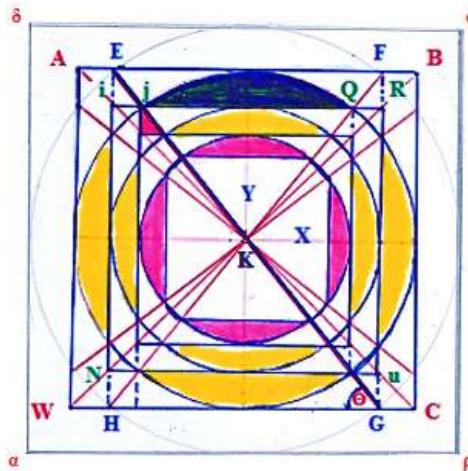
$$[EG]^2 = [EH]^2 + [HG]^2 = [4]^2 + \{4/\left[\sqrt{\frac{1}{2}(\sqrt{5} + 1)}\right]\}^2$$

$$[EG] = \sqrt{([4]^2 + \{4/\left[\sqrt{\frac{1}{2}(\sqrt{5} + 1)}\right]\}^2)} = 5.088078598$$

5. Circle drawn with [EG] Diameter, is of Circumference $\pi[EG]$,

$$\pi[EG] = \{4/\sqrt{\frac{1}{2}(\sqrt{5} + 1)}\} * \{\sqrt{([4]^2 + \{4/\left[\sqrt{\frac{1}{2}(\sqrt{5} + 1)}\right]\}^2)}\} = 16,$$

which is Equal to the Perimeter of Square [ABCW], [16].



This **Circle** defines the Construction by “*ruler and compass*” of its Circumscribed Square [**δωρα** having Perimeter defined by the product $[16]*[4/\pi] = 64/\pi$, with **Square Side** $16/\pi$.

Noting also here, that the **Parallelogramme** [EFGH] has an Area, equal to $[EH]*[HG] = [4\pi]$, which is Equal to the **Circumference** of the Circle with Diameter [4].

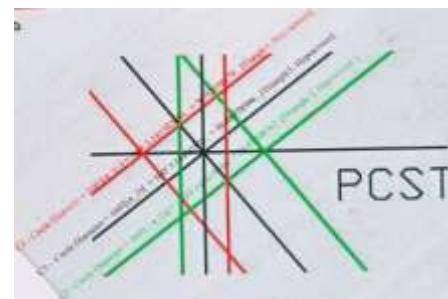
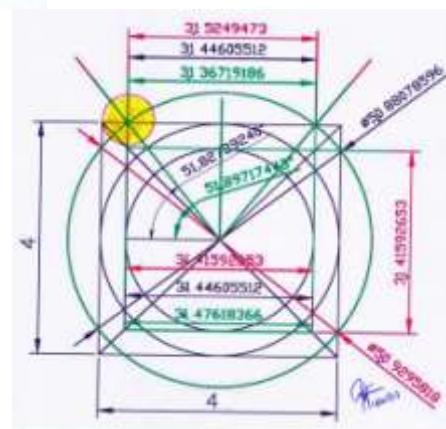
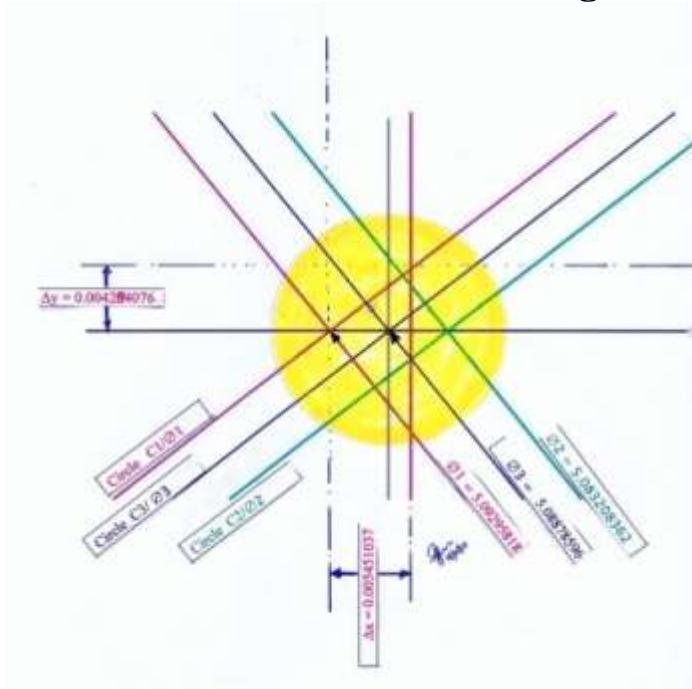
6. Joining Line [jQ] and extending it to [ji] crossing [EH] drawn, at [i] and similarly, [QR] crossing [FG] drawn at [R], the Square [iRuN] is being drawn with Sides equal to [EF],

$$\text{Equal to } \pi = 4 / \left[\sqrt{\frac{1}{2}(\sqrt{5} + 1)} \right] = [4/T] = 3.14460551 \quad [\pi^*T=4] \\ \text{with Perimeter Equal to } [4\pi]$$

Under which is being drawn, the **Inscribed Circle** of Circumference $[4\pi]*[\pi/4] = [\pi^2]$



Analysis of the PCST [Point on the Circle The Square the Triangle]

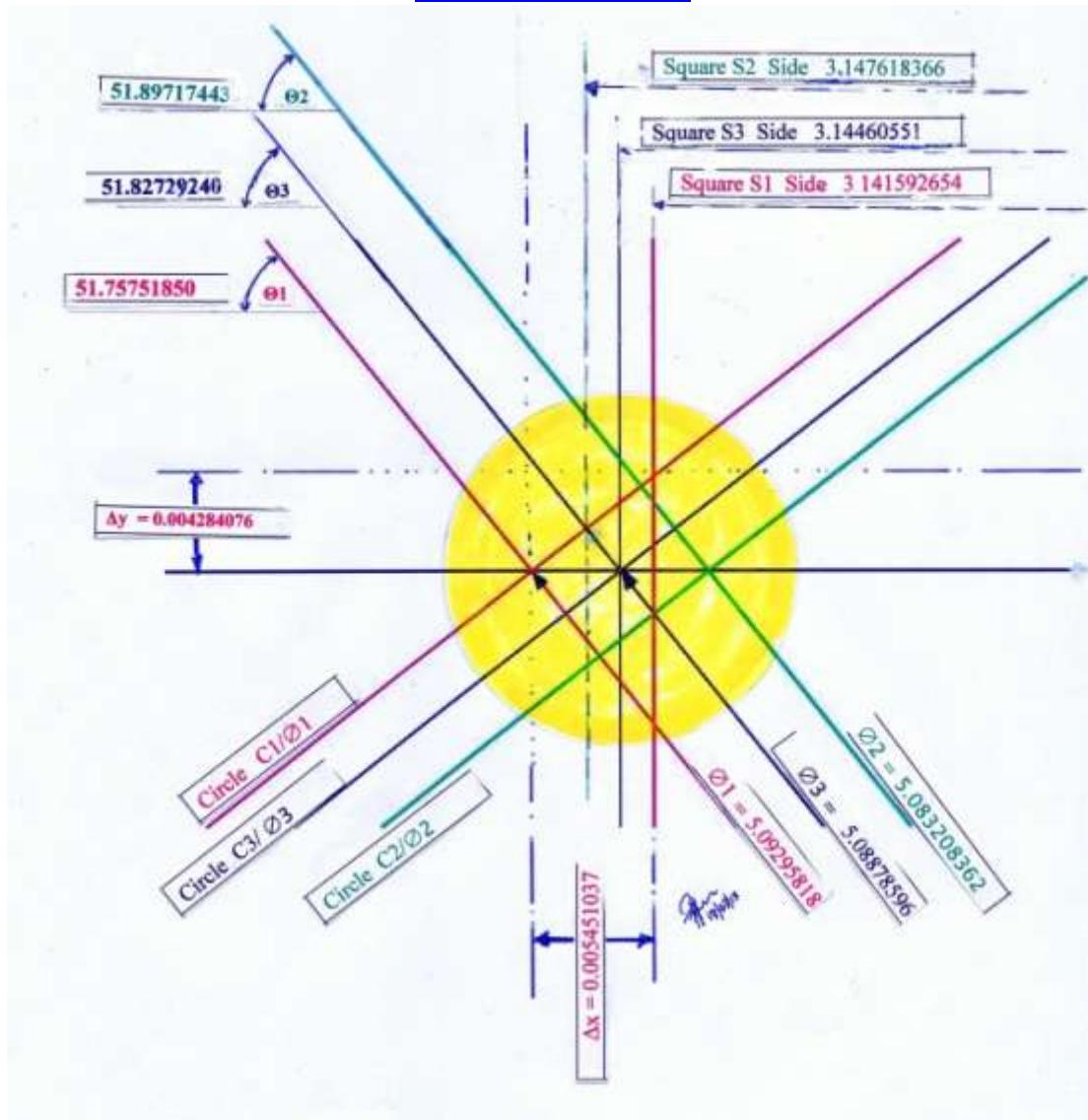


AutoCad Schematics

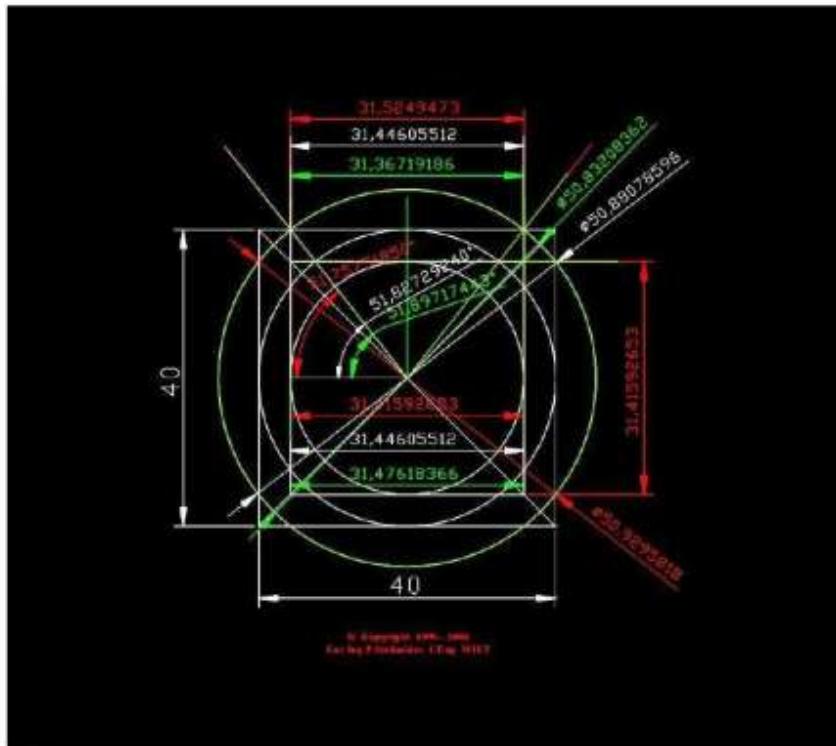


Complementary Notes added to the Analysis of the AutoCad** Schematics *

<https://www.linkedin.com/pulse/complementary-notes-added-analysis-autocad-schematics-stefanides>



* Geometry Design and 2D Vectors' Definition for AutoCad Computing by Panagiotis Stefanides.
** AutoCad Computerized Drawing by Dr. Giannis Kandylas.

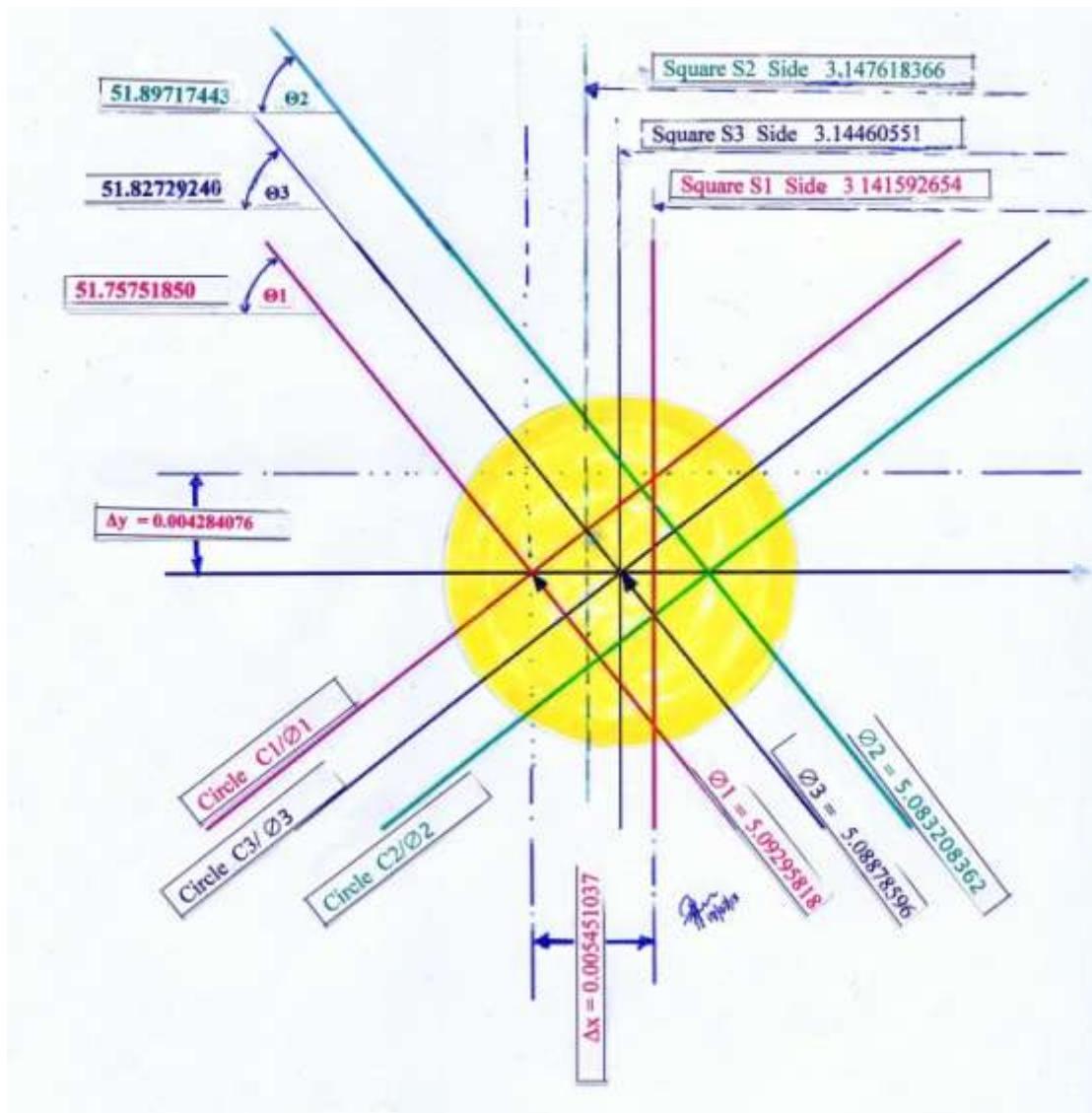


MICROCOSMOS Geometrically Related to the MACROCOSMOS
 "Nested Circles, Squares, Triangles"
Quadrature of the Circle, Compass and Ruler - NOVEL CONCEPT - via "The Quadrature Triangle"
 CONFIGURATION EXHIBITING MAXIMUM SYMMETRY
 For Value of $\pi = 4 / \sqrt{2} = 3.144605512$
 Circumference of Circle $J = 40 \cdot \sqrt{2} = 56.56878596$. $J = \text{Square } I \text{ Side } 40 \text{ J Perimeter, and}$
 $\text{Product } 40^2 D = \text{Area of this Circle} = A \text{ Square area of Side } 45.1135941.$
Geometry Design and Vector Definition of Coordinates by P. Stefanides, <http://www.stefanides.gr>
Auto Cad Computerized Drawing by Dr. J. Kandylas
© Copyright 1987 - 2014 Eur Ing Panagiotis Chr. Stefanides CEng MIET

<https://www.linkedin.com/pulse/interpreting-magnified-figures-nested-circles-squares-stefanides>



Complementary Notes added to the Analysis of the AutoCad** Schematics *

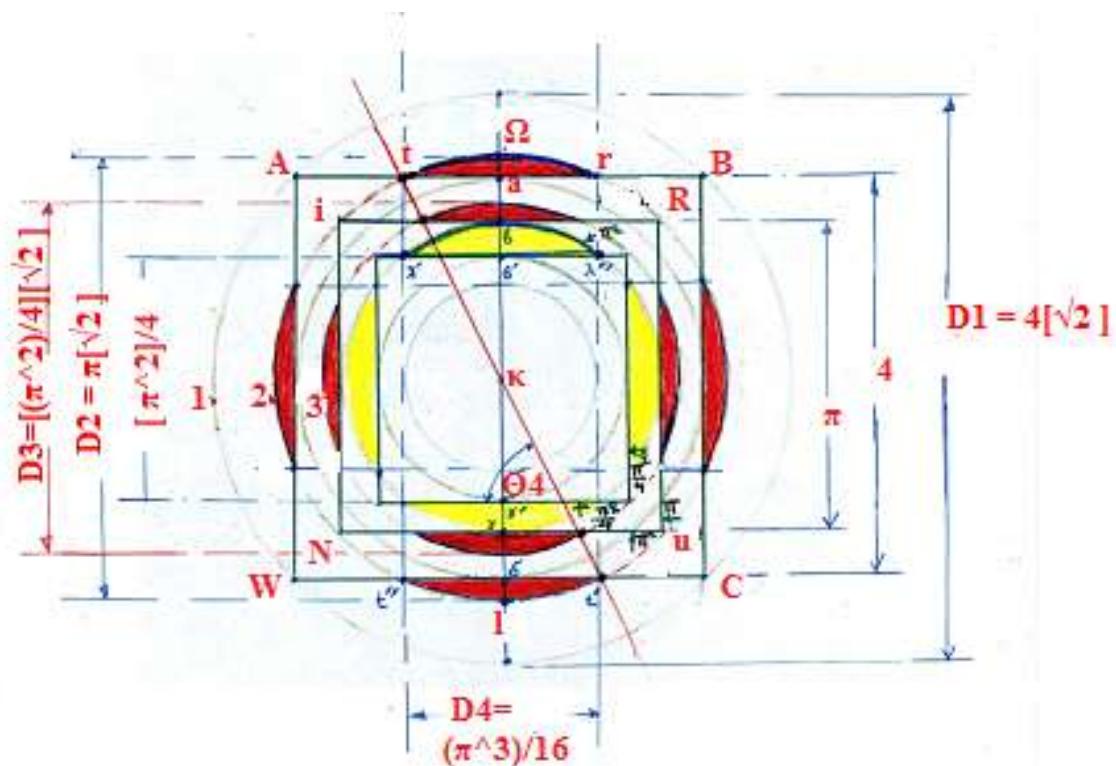


<https://www.linkedin.com/pulse/complementary-notes-added-analysis-autocad-schematics-stefanides>

* Geometry Design and 2D Vectors' Definition for AutoCad Computing by Panagiotis Stefanides.
** AutoCad Computerized Drawing by Dr. Giannis Kandylas.



Chords of Sectors of Squares' Circumscribed and Subscribed Circles', evaluated for SYMMETRIES-ASSYMETRIES, dependent on the Trancendental π Value



CIRCLES 1, 2, 3, - DIAMETERS D1, D2, D3

$D1 = 4[\sqrt{2}]$ = Diagonal of SQUARE with SideLength [4]

$D2 = \pi[\sqrt{2}]$ = Diagonal of SQUARE with SideLength [π]

$D3 = [(\pi^2)/4][\sqrt{2}]$ = Diagonal of SQUARE with SideLength [$(\pi^2)/4$]

CIRCLE with Diameter [$a\delta$] Subscribed to SQUARE [ABCW]

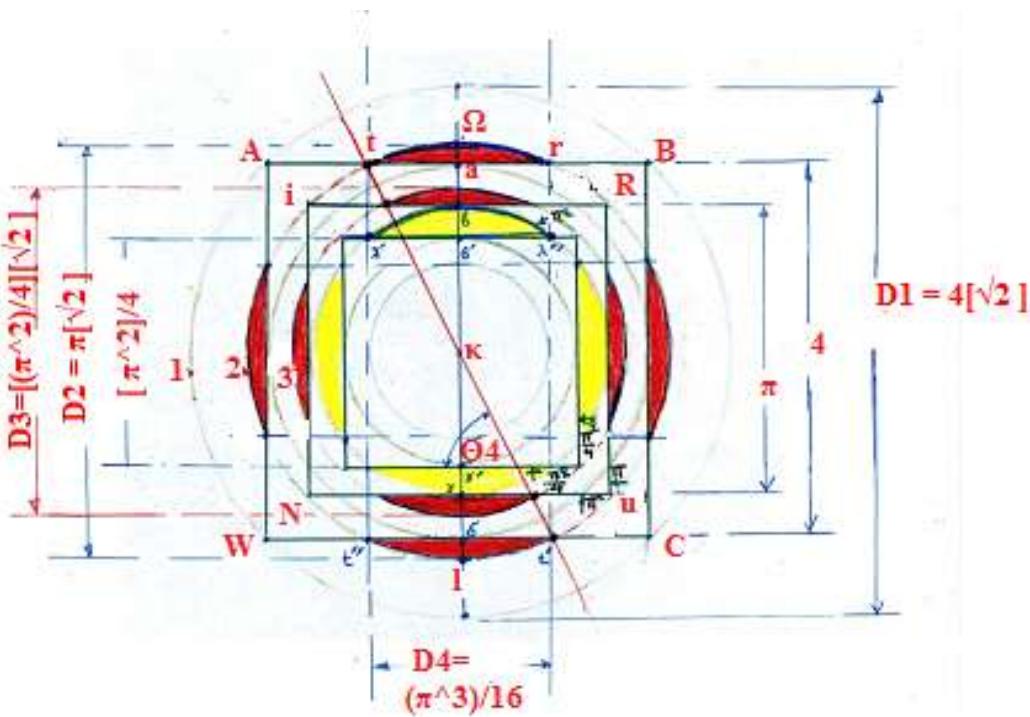
CIRCLE with Diameter [$\beta\gamma$] Subscribed to SQUARE [iRuN]

CIRCLE with Diameter [$\beta'\gamma'$], Subscribed to SQUARE with SideLength $(\pi^2)/4$

CIRCLE of Diameter $D4 = (\pi^3)/16$, Subscribed to SQUARE with SideLength $(\pi^3)/16$

SQUARE [iRuN] with SideLength π

SQUARE [ABCW] with SideLength 4



Find Chord Length $[\lambda'\lambda'']$

POWER OF POINT THEOREM APPLICATION

$$[\lambda'\beta'] = [\beta'\lambda'']$$

$$[\beta\beta'] = [\gamma\gamma']$$

$$[\beta\beta'] + [(\pi^2)/4] + [\gamma\gamma'] = \pi = 2[\beta\beta'] + [(\pi^2)/4],$$

$$2[\beta\beta'] = \pi - [(\pi^2)/4] \text{ or}$$

$$[\beta\beta'] = \pi/2 - [(\pi^2)/8] = 0.337095777..$$

$$[\beta\beta'] * [(\pi^2)/4 + \beta\beta'] = [\lambda'\beta'] * [\beta'\lambda''] = [\lambda'\beta']^2 \text{ or}$$

$$[\beta\beta'] * [(\pi^2)/4 + \beta\beta'] = [\lambda'\beta']^2 \text{ or}$$

$$[\lambda'\beta']^2 = [0.337095777..] * [2.4674011 + 0.337095777..] =$$

$$= 0.95384053.., \text{ or}$$

$$[\lambda'\beta'] = 0.97230862.. \text{ and}$$

$$2[\lambda'\beta'] = [\lambda'\lambda'']$$

$$[\lambda'\lambda''] = 1.94461724..$$

[Compare with $(\pi^3)/16 = 1.937892293.. < 1.94461724..]$
 [ratio error = 1.003470238]

NOTE: For $\pi = \Pi\sigma\chi = 4/\sqrt{[5+1]/2} = 3.14460551..$

$$\pi = 2[\beta\beta'] + [(\pi^2)/4],$$

$$2[\beta\beta'] = \pi - [(\pi^2)/4] = 0.672469557.. \text{ or}$$

$$[\beta\beta'] = \pi/2 - [(\pi^2)/8] =$$

[$\beta\beta'$] = 0.336234778.. [< 0.337095777.. .. using $\pi = 3.141592654..$]

$$[\beta\beta'] * [(\pi^2)/4 + \beta\beta'] = [\lambda'\beta'] * [\beta'\lambda''] = [\lambda'\beta']^2 \text{ or}$$

$$[\beta\beta'] * [(\pi^2)/4 + \beta\beta'] = [\lambda'\beta']^2$$

$$[\lambda'\beta']^2 = [\beta\beta'] * [(\pi^2)/4 + \beta\beta'] \text{ or}$$

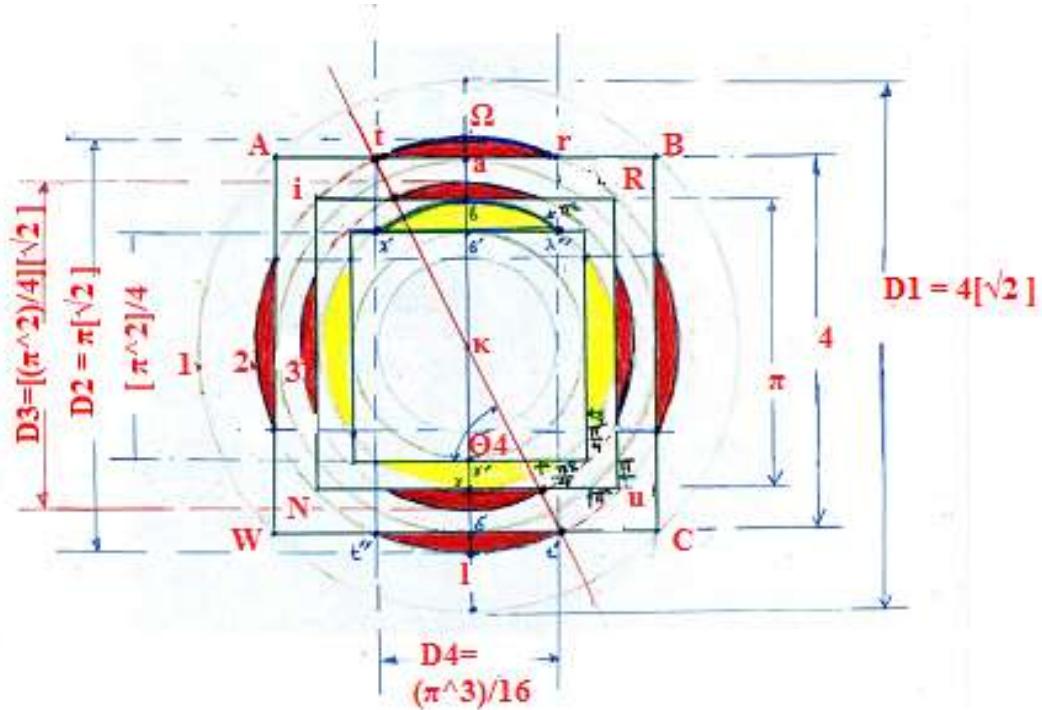
$$\begin{aligned} [\lambda'\beta']^2 &= [\textcolor{red}{0.336234778..}] * [(\pi^2)/4 + \textcolor{red}{0.336234778..}] = \\ &= 0.94427191.. \end{aligned}$$

$$[\lambda'\beta'] = 0.971736544.., \text{ and } 2[\lambda'\beta'] = 1.943473087..$$

$$2[\lambda'\beta'] = \textcolor{red}{[\lambda'\lambda'']}$$

[$\lambda'\lambda''$] = 1.943473087.. [< 1.94461724.. using $\pi = 3.141592654..$]

[Compare with $(\pi^3)/16 = 1.943473087..$ i.e equal]



© Copyright 1985- 2016, Eur Ing Panagiotis Chr. Stefanides CEng MIET

SIMILARLY

Find Chord Length [tr]

POWER OF POINT THEOREM APPLICATION

$$[\Omega a]^* [al] = [ta]^* [ar] = [(tr)/2]^2 = [ta]^2$$

$$[\Omega a] = [\delta\lambda], \quad [ta] = [ar], \quad [\Omega l] = [\Omega a] + [a\delta] + [\delta l]$$

$$[\Omega a]^* [al] = [ta]^2$$

$$[\Omega a]^* [a\delta + \delta l] = [\Omega a]^* [4 + \delta l] = [\Omega a]^* [4 + \Omega a], \text{ or}$$

$$[ta]^2 = [\Omega a]^* [4 + \Omega a] ..$$

$$\{4 + [\Omega a + \delta\lambda]\} = \{4 + 2[\Omega a]\} = D2 = \pi[\sqrt{2}], \quad \text{or} \quad [\Omega a] = \{\pi[\sqrt{2}] - 4\} / 2$$

$$[\Omega a] = 0.221441469..$$

$$\{ [ta]^2 = [\Omega a]^* [4 + \Omega a] \}$$

$$[ta]^2 = [\{\pi[\sqrt{2}] - 4\} / 2] * [4 + \{\pi[\sqrt{2}] - 4\} / 2] = 0.934802201..$$

$$[ta] = \sqrt{[\{\pi[\sqrt{2}] - 4\} / 2] * [4 + \{\pi[\sqrt{2}] - 4\} / 2]} = 0.966851695..$$

and

$$2[ta] = [tr] = 2(\sqrt{[\{\pi[\sqrt{2}] - 4\} / 2] * [4 + \{\pi[\sqrt{2}] - 4\} / 2]}) = [tr]$$

$$[tr] = 1.93370339..$$

[Compare with $(\pi^3)/16 = 1.937892293.. > 1.93370339..$, ,

ratio error 1.002166259]

$$\tan(\Theta_4) = [Ka]/[ta] =$$

$$= (4/2) / \sqrt{[\{\pi[\sqrt{2}] - 4\} / 2] * [4 + \{\pi[\sqrt{2}] - 4\} / 2]} =$$

$$= 2/0.966851695.. = 2.068568998.., \quad \Theta_4 = 64.19967679.. \text{ deg.}$$

NOTE: For $\pi = \Pi \sigma \chi = 4/\sqrt{[5 + 1]/2} = 3.14460551..$

$$[\Omega a] = 0.22357188.. [> 0.221441469.. \text{ using } \pi = 3.141592654..]$$

$$[ta] = 0.971736544.., \quad 2[ta] = [tr]$$

$$[tr] = 1.943473087.. [> 1.93370339.. \text{ using } \pi = 3.141592654..]$$

[Compare with $(\pi^3)/16 = 1.943473087..$, i.e equal]

$$\tan(\Theta_4) = 2/[ta] = 2.058171027.., \quad 1/2.058171027.. = 0.485868272..$$

$$\Theta_4 = 64.08635381.. \text{ deg.}$$

$$1/\tan(\Theta_4) = 0.485868272..,$$

$$[1/\tan(\Theta_4)]^2 = 0.236067978.. = 2\Phi - 3, \quad [\Phi = \{\sqrt{5} - 1\}/2]$$

$$0.236067978.. + 4 = 1/0.236067978.. = 4.236067978..$$

$$\sqrt{4.236067978..} = 2.058171027.., \quad 1/2.058171027.. \\ = 0.485868272..$$

SUMMARY OF RESULTS

A

Calculations Based on : $\Pi\sigma\chi = 4/\sqrt{[\sqrt{5} + 1]/2}$
 $[= 3.14460551..]$

Chord Length $[\lambda\lambda''] = 1.943473087..$

**[Value Equals to Circle Diameter D4 =
 $([\Pi\sigma\chi]^3)/16 = [(4/\sqrt{[\sqrt{5} + 1]/2})^3]/16 = 1.943473087..]$**

Chord Length $[tr] = 1.943473087..$

**[Value Equals to Circle Diameter D4 =
 $([\Pi\sigma\chi]^3)/16 = [(4/\sqrt{[\sqrt{5} + 1]/2})^3]/16 = 1.943473087..]$**

THESE DEMONSTRATE EVIDENT SYMMETRIES

B

Calculations Based on : $\pi = 3.141592654..$

Chord Length $[\lambda\lambda''] = 1.94461724.. [> (\pi^3)/16 = 1.937892293..]$

**[Value Bigger than Circle Diameter D4 =
 $= (\pi^3)/16 = \{(3.141592654..)^3\}/16 = 1.937892293..]$**

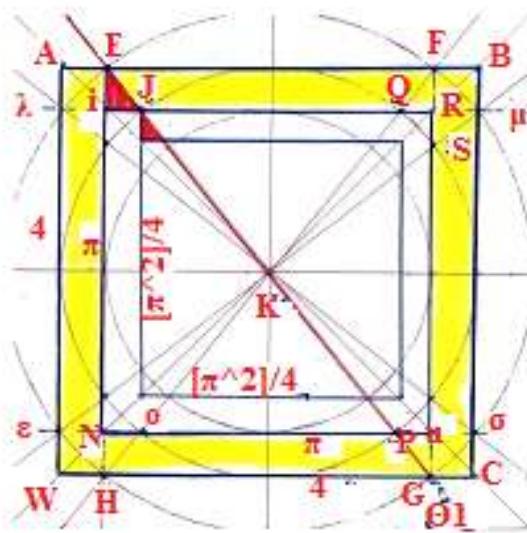
Chord Length $[tr] = 1.93370339.. [< (\pi^3)/16 = 1.937892293..]$

**[Value Smaller than Circle Diameter D4 =
 $= (\pi^3)/16 = \{(3.141592654..)^3\}/16 = 1.937892293..]$**

THESE DEMONSTRATE EVIDENT ASYMMETRIES

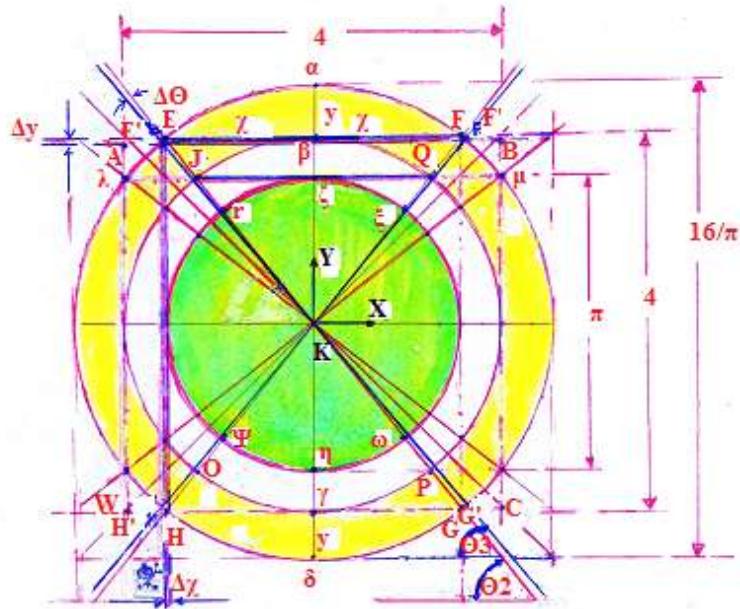


No Detection of Imperfection of Circle, Challenges the Transcendence of π



SQUARES in RATIOS of $4/\pi$

<https://www.linkedin.com/pulse/detection-imperfection-circle-challenges-%CF%80-panagiotis-stefanides?trk=prof-post>



CIRCLES in RATIOS of $4/\pi$ [as SQUARES in same RATIOS]

Power of Point Theorem Application

$$[a\beta].[b\delta] = \chi^2$$

$$[y].[(\beta\gamma) + (y)] = \chi^2$$

$$[y].[(JP) + (y)] = \chi^2$$

$$[y].[(4) + (y)] = \chi'^2$$

$$y^2 + 4y - \chi^2 = 0, \quad y = a\beta = \gamma\delta = [D_1 - D_2] / 2 = y = 0.54647909..$$

$$[0.54647909..]^2 + 4[0.54647909..] = 2.484555753.. = \chi^2$$

$$\chi = 1.576247364.., \quad 2\chi = 3.152494728.. = [E'F']$$

$$D_1 = EG = a\delta = 16/\pi = 5.092958179.., \quad \text{Circumference} = 16$$

$$D_2 = JP = \beta\gamma = 4, \quad \text{Circumference} = 4\pi$$

$$D3 = \zeta\eta = \tau\omega = \pi,$$

Circumference = π^2

$$D1/D2 = a\delta / \beta\gamma = [16/\pi]/4 = 4/\pi$$

$$D2/D3 = \beta\gamma / \zeta\eta = 4/\pi = D1/D2$$

$$D1-D2 = 5.092958179.. - 4 = 1.092958179.. = a\beta = \gamma\delta = 2y, y = 0.54647909..$$

$$2\chi = 3.152494728.. = [E'F']$$

Ratios:

$$[E'H']/[\zeta\eta] = 4/\pi = 1.273239545.. \quad [\Theta = 51.85397401... \text{Deg}]$$

$$[EH]/[\zeta\eta] = [EH]/[HG] = [4 + 2\Delta y]/\pi > 4/\pi$$

$$[\Delta y = 0.004284076 ..]$$

Ref : <https://www.linkedin.com/pulse/detection-imperfection-circle-challenges-%CF%80-panagiotis-stefanides?trk=prof-post>

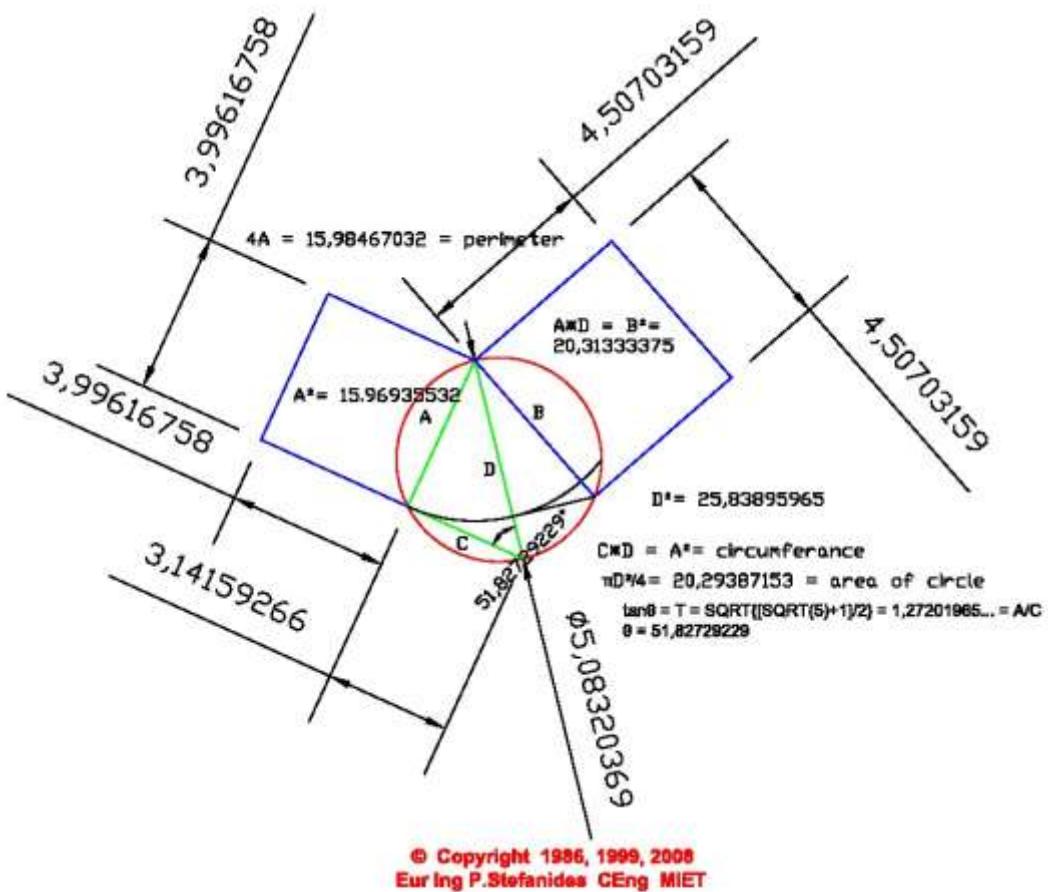
$$[EH]/[\zeta\eta] = [EH]/[HG] = [4 + 2\Delta y]/\pi = 1.275966872$$

Corresponding to slope of angle 51.91351208..Deg. = Θ_2

$$[E'H']/[H'G'] = 4/[E'F'] = 4/3.152494728.. = 1.26883638..$$

Corresponding $\Theta_3 = 51.75751853.. \text{Deg.}$

TRANSCENDENTAL π [= 3.141592654..] does not Square the Circle



NOTE: For $\pi = \Pi\sigma\chi = 4/\sqrt{[\{ \sqrt{5} + 1 \} / 2]} = 3.14460551..$

$\Delta\chi = 0$, $\Delta y = 0$ and $\Delta\theta = 0$, [E'F'] = [EF] and [EH] = [E'H']

$$\tan \theta = T = \text{SQRT}(\{\text{SQRT}(5)+1\}/2) = 1.27201965... = A/C$$

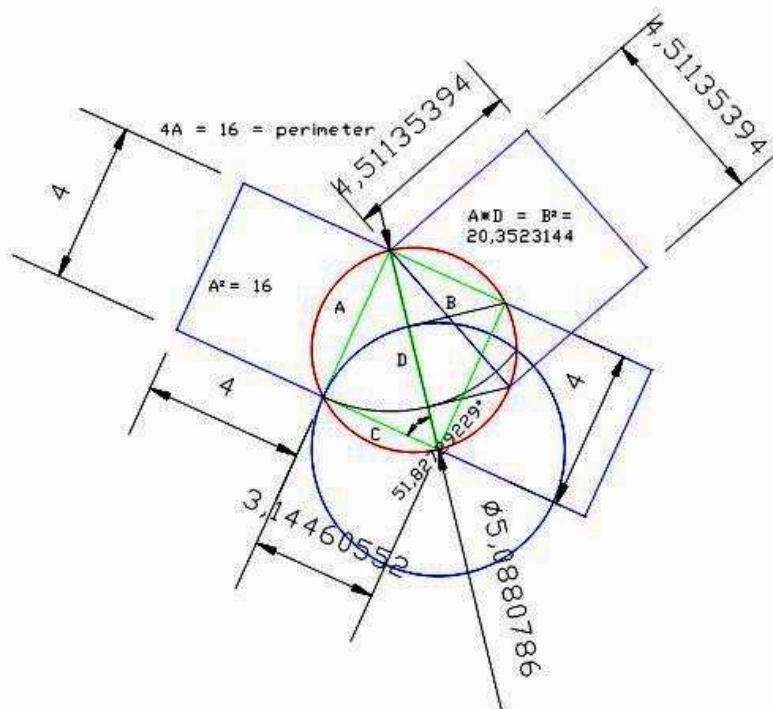
$$\theta = 51.82729229^\circ$$

$$D^2 = 25.88854384$$

$C \cdot D = A^2 = \text{circumference}$

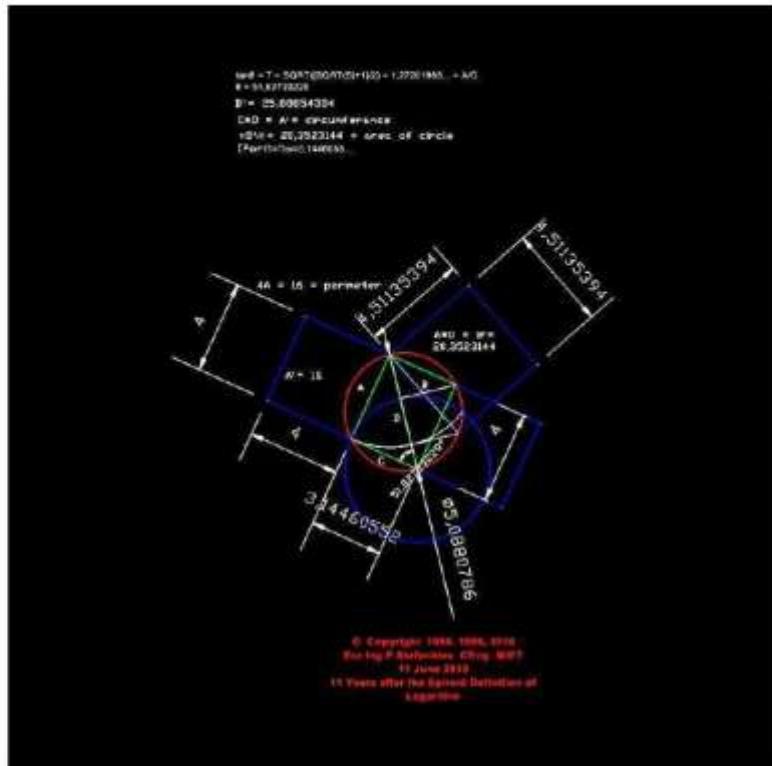
$$\pi D^2/4 = 20.3523144 = \text{area of circle}$$

[for $\Pi = \Pi_{\text{ex}} = 3.1446055...$]



© Copyright 1986, 1989, 2010
Eur Ing P.Stefanides CEng MIET
11 June 2010

11 Years after the Spiroid Definition of
Logarithm



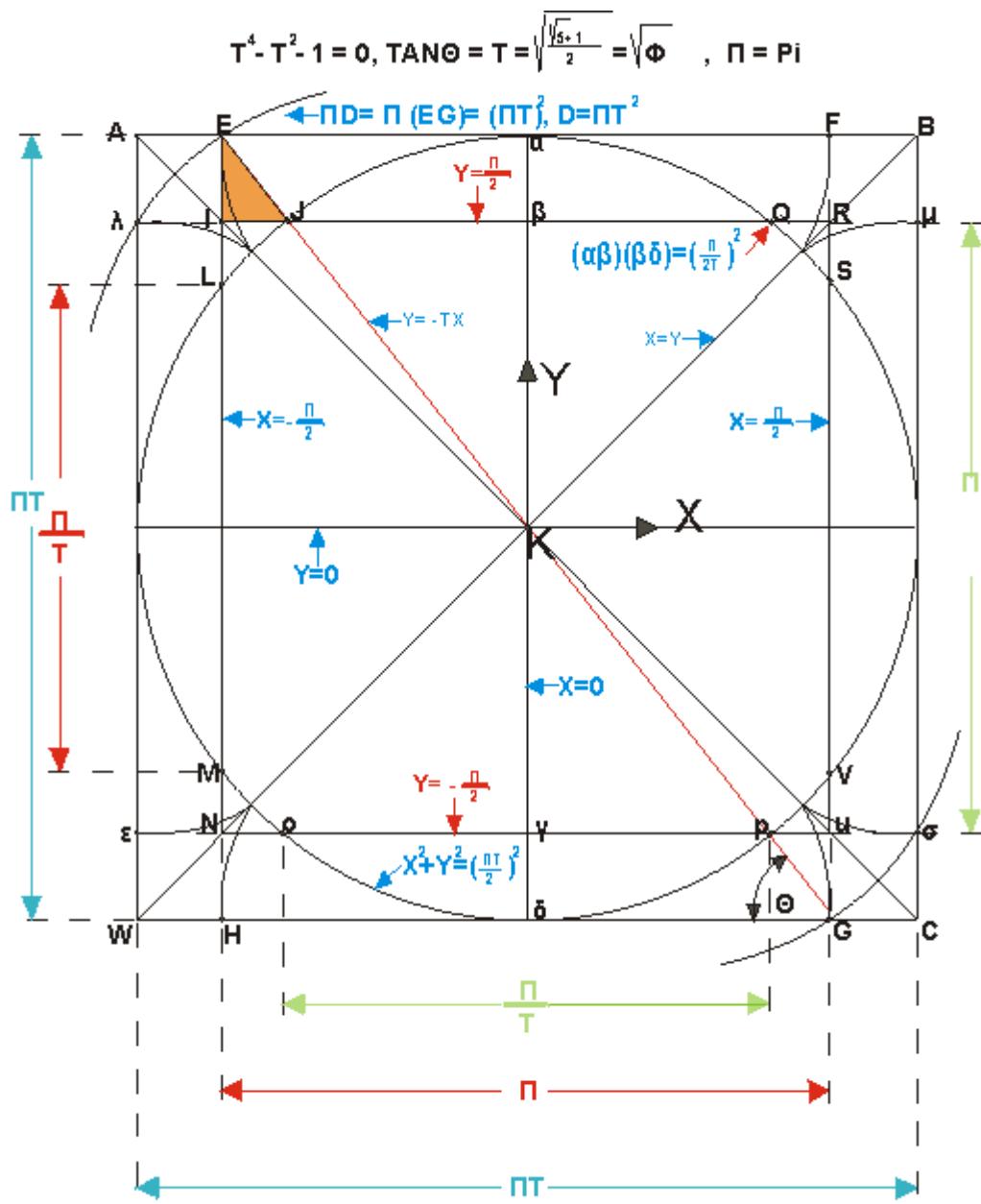
For: $\pi = 4/\sqrt{\varphi}$

Quadrature of the Circle, Compass and Ruler - NOVEL CONCEPT - via "The Quadrature Triangle"

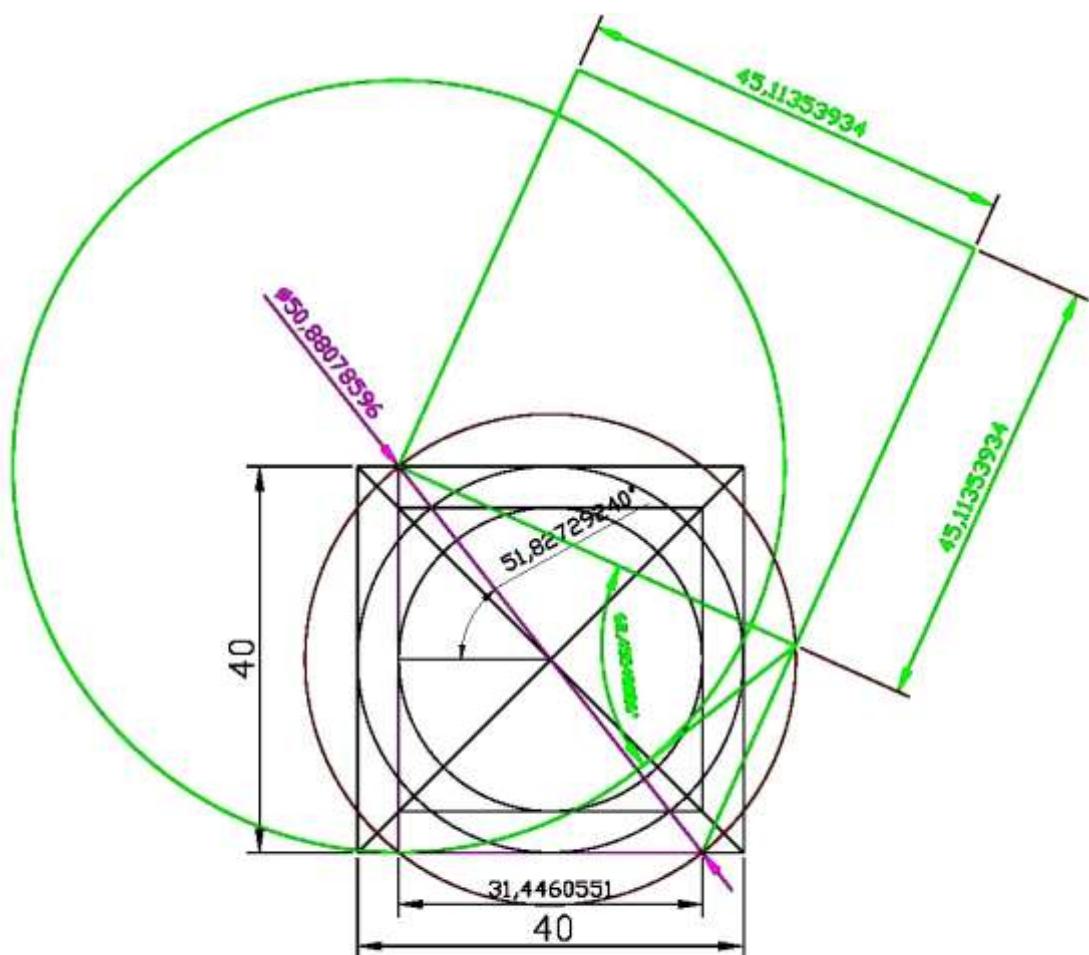
$D = 4\sqrt{\varphi} = 5.0880786...$ [Red Circle], $\pi^2 D = 4^2 = 16 = \text{Square}$ [Side 4] Perimeter = Circle[Red]

Circumference , $[\pi/4]^2 D^2 = 16 + \sqrt{\varphi} = 4.51135394..]^2 = \text{Circle}[Red] \text{ Area} =$
 $= \text{Square} [\text{Side } 4.51135394..] \text{ Area} = 20.3523144..$

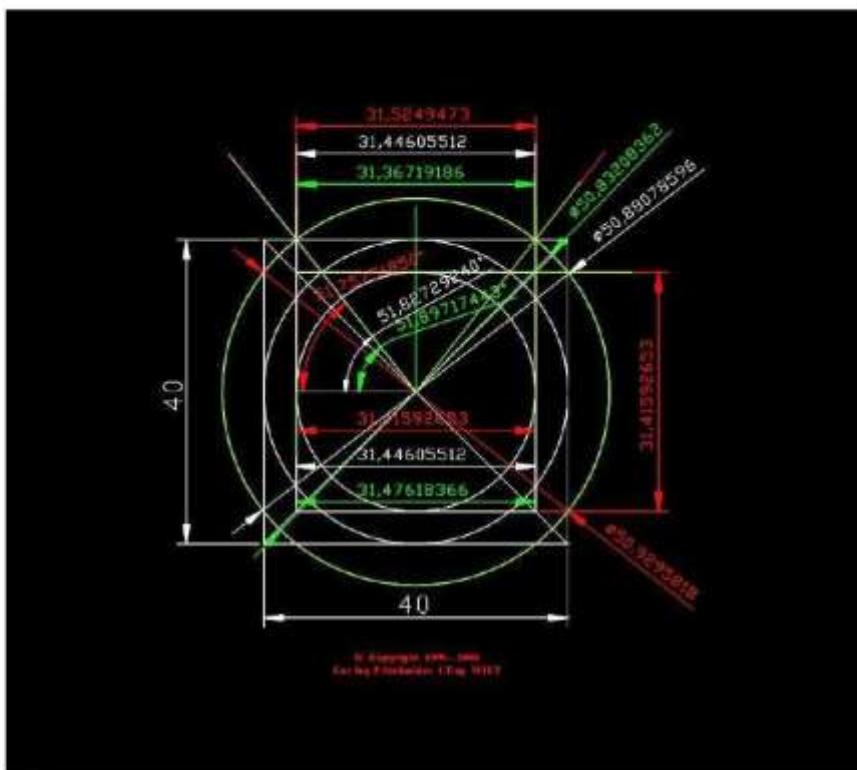
Geometry Design and Vector Definition of Coordinates by P.Stefanides, <http://www.stefanides.gr>
AutoCad Computerized Drawing by Dr. J. Kandylas
©Copyright 1987 - 2014 Eur Ing Panagiotis Chr. Stefanides CEng MIET



COPYRIGHT ©, SECUNDI MILLENNII FINIS, P.C. STEFANIDES



© Copyright 1985 - 2017
Eur Ing P.Stefanides CEng MIET



MICROCOSMOS Geometrically Related to the MACROCOSMOS
"Nested Circles, Squares, Triangles"
Quadrature of the Circle, Compass and Ruler - NOVEL CONCEPT - via "The Quadrature Triangle"
CONFIGURATION EXHIBITING MAXIMUM SYMMETRY

For Value of $\pi = 4 / \sqrt{\varphi} [- 3.14460551..]$

Circumference of Circle [D = 40] $= 80.80078596..$ - Square [Side 40] Perimeter, and
Product 40² - Area of this Circle - A Square area of Side 45.1135941..

Geometry Design and Vector Definition of Coordinates by P. Stefanides, <http://www.stefanides.gr>
Auto Cad Computerized Drawing by Dr. J. Kandylas
© Copyright 1987 - 2014 Eur Ing Panagiotis Chr. Stefanides CEng MIET

Page_101_ from_JMM_2016_Cat_Full

[Bridges Seoul Korea AUG 2014
2016](#)

[Bridges Mathematical Art Galleries](#)

[Bridges Washington Seattle Jan](#)

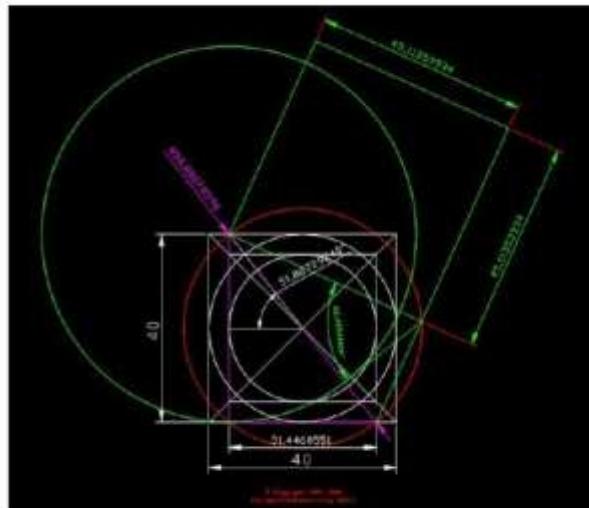
WASHINGTON SEATTLE JOINT MATHEMATICAL MEETING
JMM * AMERICAN MATHEMATICAL SOCIETY*MATHEMATICAL ASSOCIATION OF AMERICA JAN
2016

[Athens Energy 2015 European Cente](#)

Panagiotis Stefanides

Chartered Engineer [UK]
Hellenic Aerospace Industry [ex]
Athens, Greece

"This work, presented to various conferences, is a proposed interpretation of Plato's Timaeus Scalene Orthogonal Triangle by Panagiotis Stefanides. It is noted here that, a similar, constituent part of this triangle but not the same, is the Kepler triangle discovered by Magirus. Quadrature of the circle by compass and ruler is achieved based on the special quality of this triangle [a quadrature triangle] and its relationship with circle, the parallelogramms and the square."



CIRCLE'S QUADRATURE

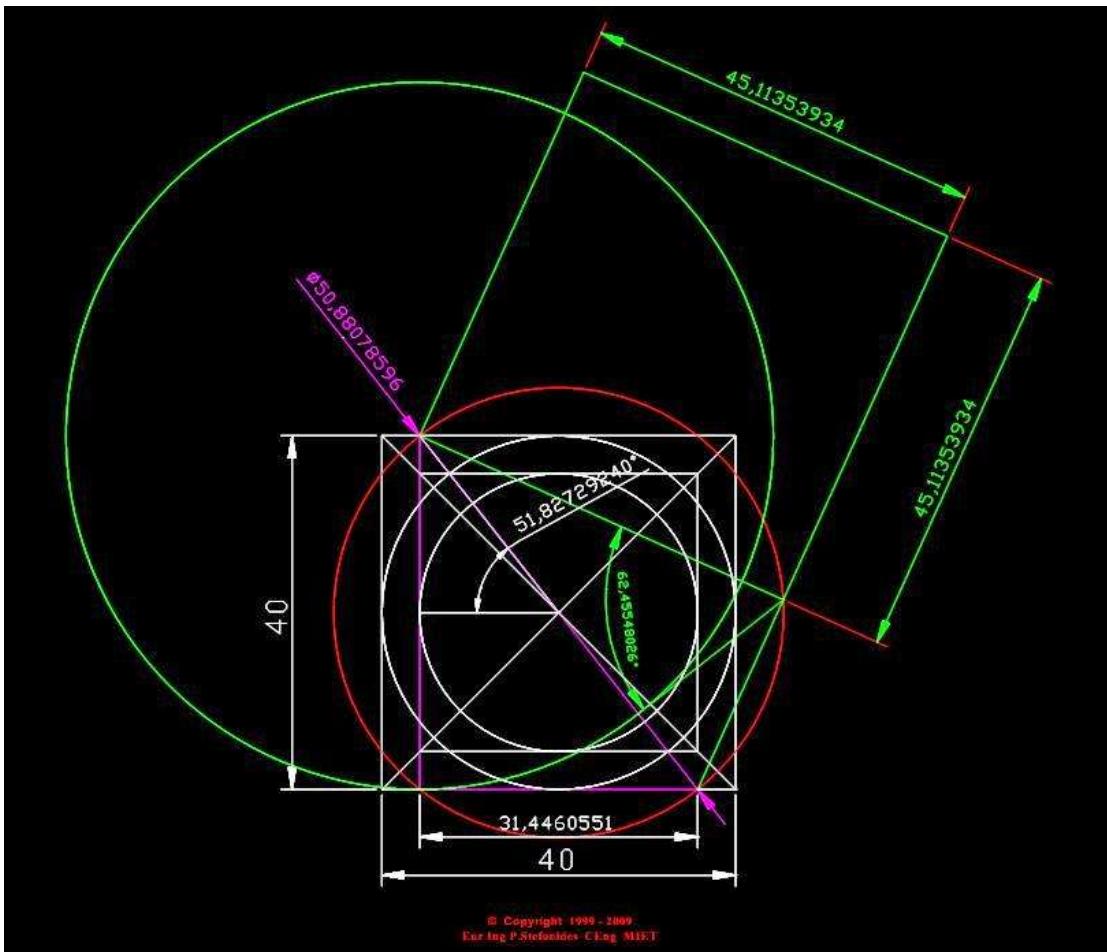
32 x 23 x 3 cm

AUTOCAD DRAWING FRAMED PHOTO, 2009

Autocad used: Geometry and Vector definition by Panagiotis Stefanides assisted for the Computerized AutoCad Drawing by Dr. Giannis Kandylas.

More information:

http://www.stefanides.gr/Html/GOLDEN_ROOT_SYMMETRIES.htm



CIRCLE'S QUADRATURE

By [Panagiotis Stefanides](#)

$$\text{For: } \pi = 4 / \sqrt{\varphi} = 3.14460551..$$

Quadrature of the Circle, Compass and Ruler - NOVEL CONCEPT - via "The Quadrature Triangle"

$$D = 40 * \sqrt{\varphi} = 50.8807859.., \quad \pi * D = 4 * 40 = 160 = \text{Square [Side 40] Perimeter} =$$

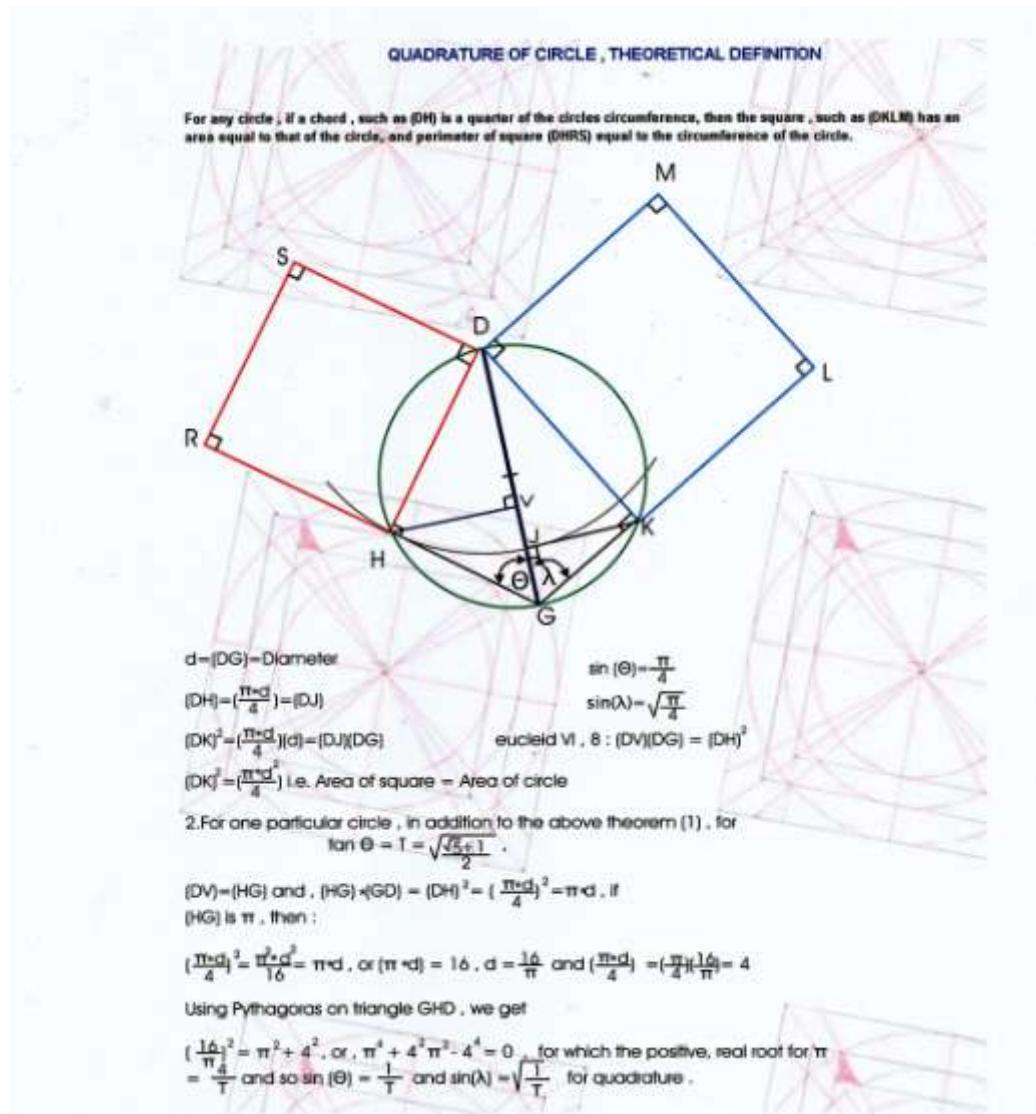
$$= \text{Circle[Red] Circumference , } [\pi/4] * D^2 = 1600 * \sqrt{\varphi} = [45.1135394..]^2 = \text{Circle[Red] Area} = \\ = \text{Square [Side 45.113539..] Area} = 2035.2314..$$

[Geometry Design and Vector Definition of Coordinates by P.Stefanides](#), <http://www.stefanides.gr>
AutoCad Computerized Drawing by Dr. J. Kandylas

© Copyright 1987 - 2014 Eur Ing Panagiotis Chr. Stefanides CEng MIET

[Bridges 2016 Exhibit](#) - Joint Mathematics Meetings

Jan 6-9 (WED-SAT),2016 - WASHINGTON STATE CONVENTION CENTER,SEATTLE, WA
The Mathematical Association of America (MAA) and the American Mathematical Society (AMS).



\

π , Irrational Positive Real Root of Fourth Order

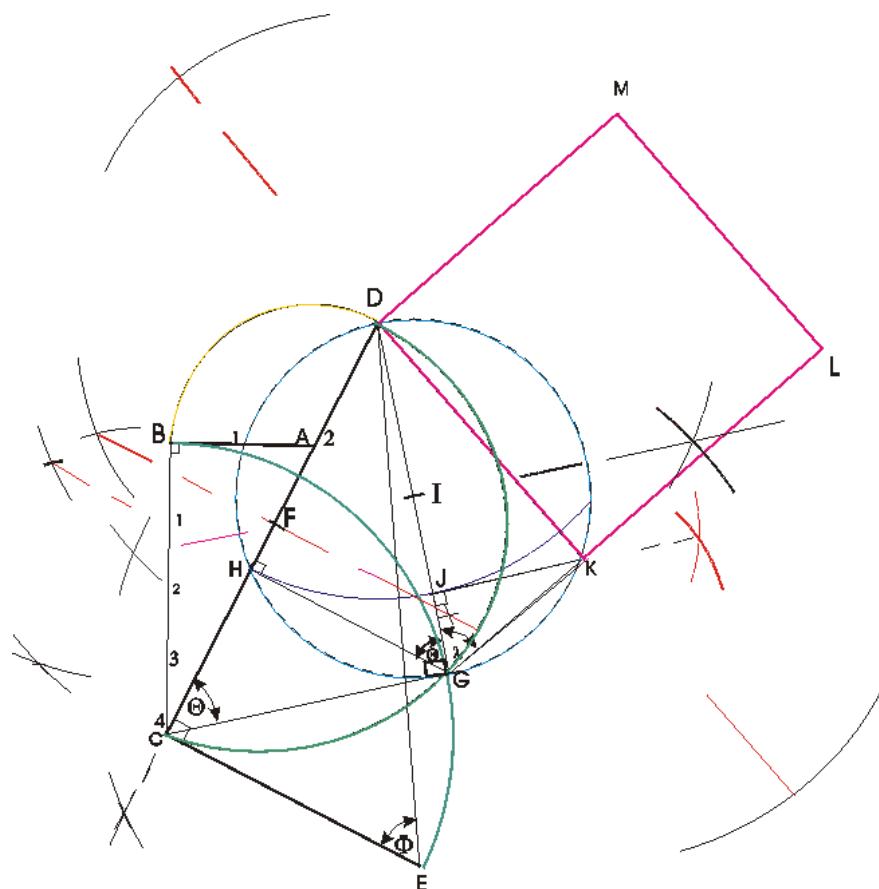
Equation

<http://www.stefanides.gr/Html/piquad.html>

For $\pi = \Pi\sigma\chi = 4/\sqrt{[\{\sqrt{5} + 1\}/2]} = 3.14460551..$ Irrational ,

Ruler and Compass

Configuration for the Circle's Quadrature.



<http://www.stefanides.gr/Html/piquad.html>

CONCLUSIONS

Under conditions described above,

**Values of Numbers and Ratios of Forms such as those
within X-Y Axial plane of **Conic Section**, defined by
extended Lines [EG] and [FH] and the whole set of Circles
Squares Triangles,**

Expanding to **Macroscopic Scales, in Powers of**

[$4/\pi$] or

Similarly, Contracting to **Microscopic Ones, in Powers of**

[$\pi/4$],

Remain **Unchangeable Unlimitedly, on the **Basis** that,**

$$\pi = 4 / \left[\sqrt{\frac{1}{2} (\sqrt{5} + 1)} \right]$$

Finally, constructing “*by compass and ruler*” a **Unit Square of side [1] or, **Perimeter** [4], defines its inscribed **Unit Circle** of Diameter [1] and **Circumference****

$$[4 / \left[\sqrt{\frac{1}{2} (\sqrt{5} + 1)} \right]].$$

Discrepancies, or not, of the value of π indicate the

relevance of the title

“HARMONY AND DISHARMONY”

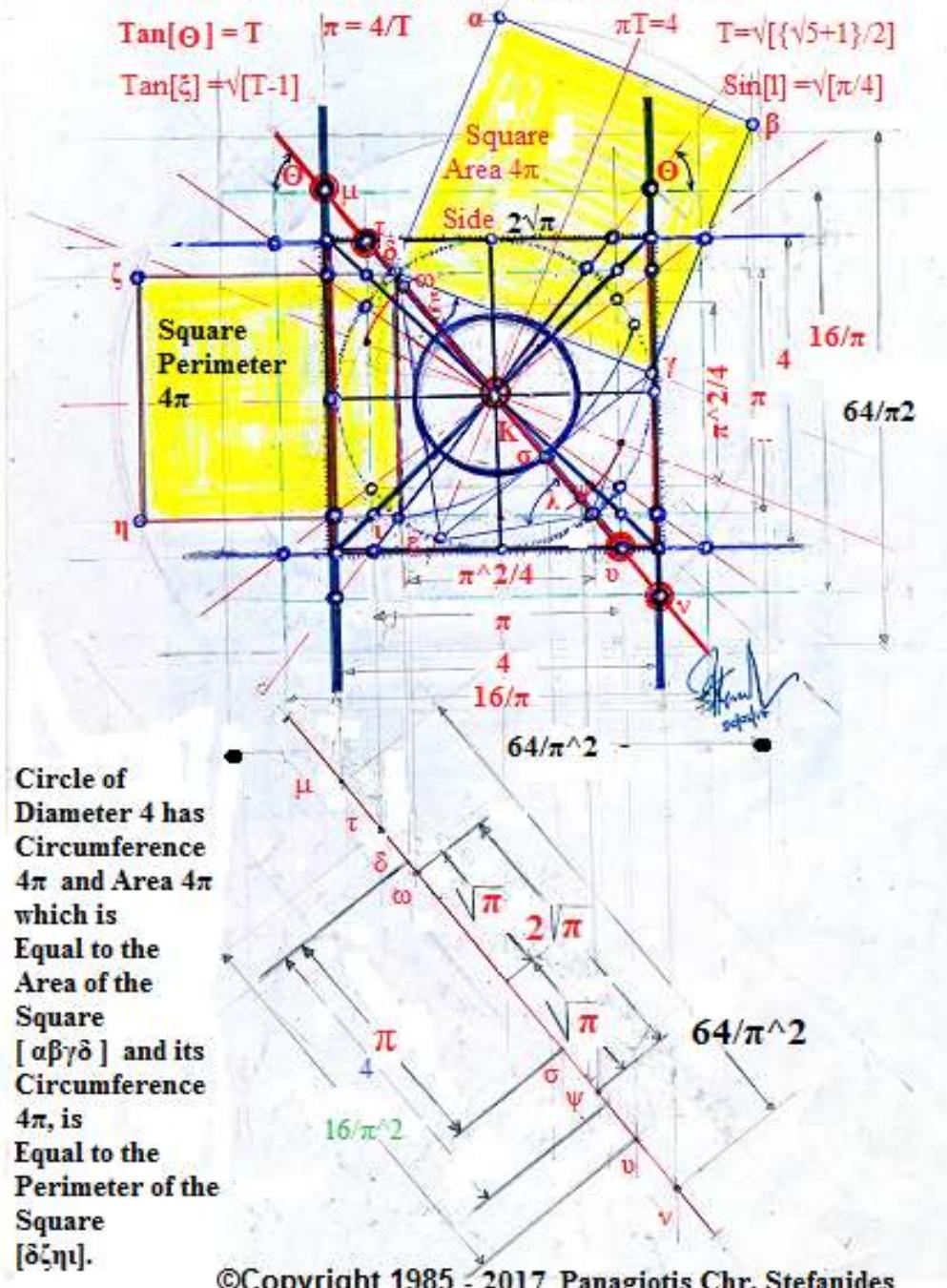
ADDENDUM 1

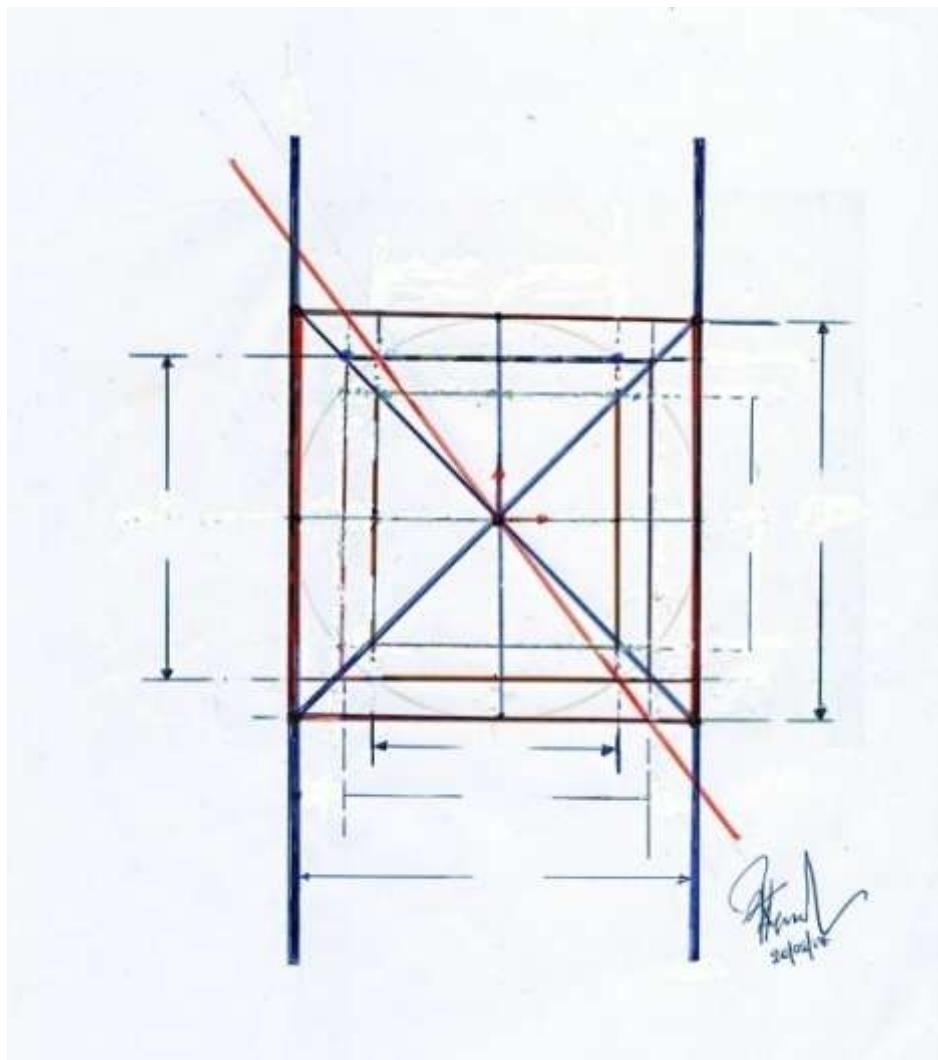


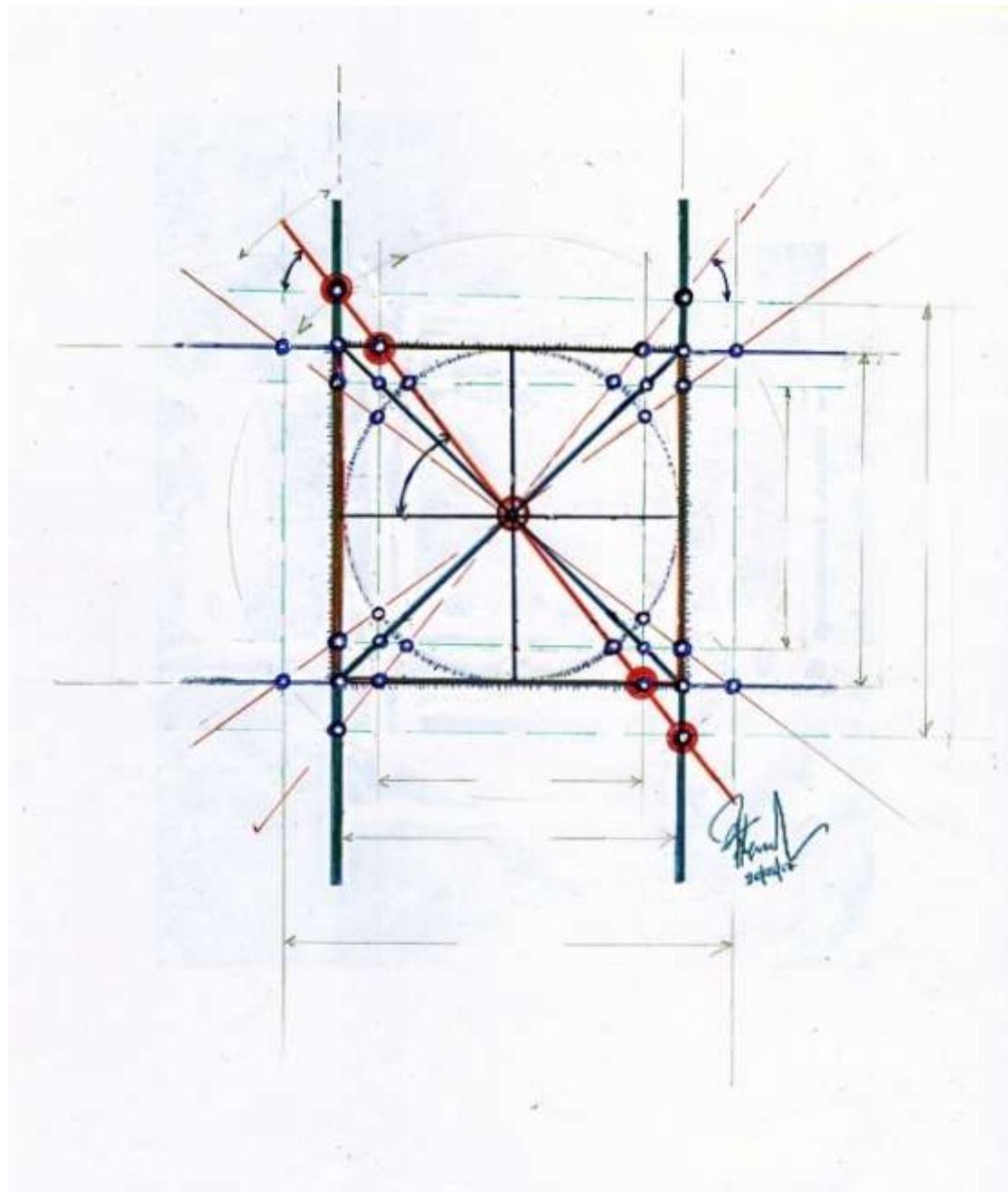
A TOOL TO DEMONSTRATE RELATIONSHIPS BETWEEN CIRCLE, SQUARE, TRIANGLE AND PARALLELOGRAMME

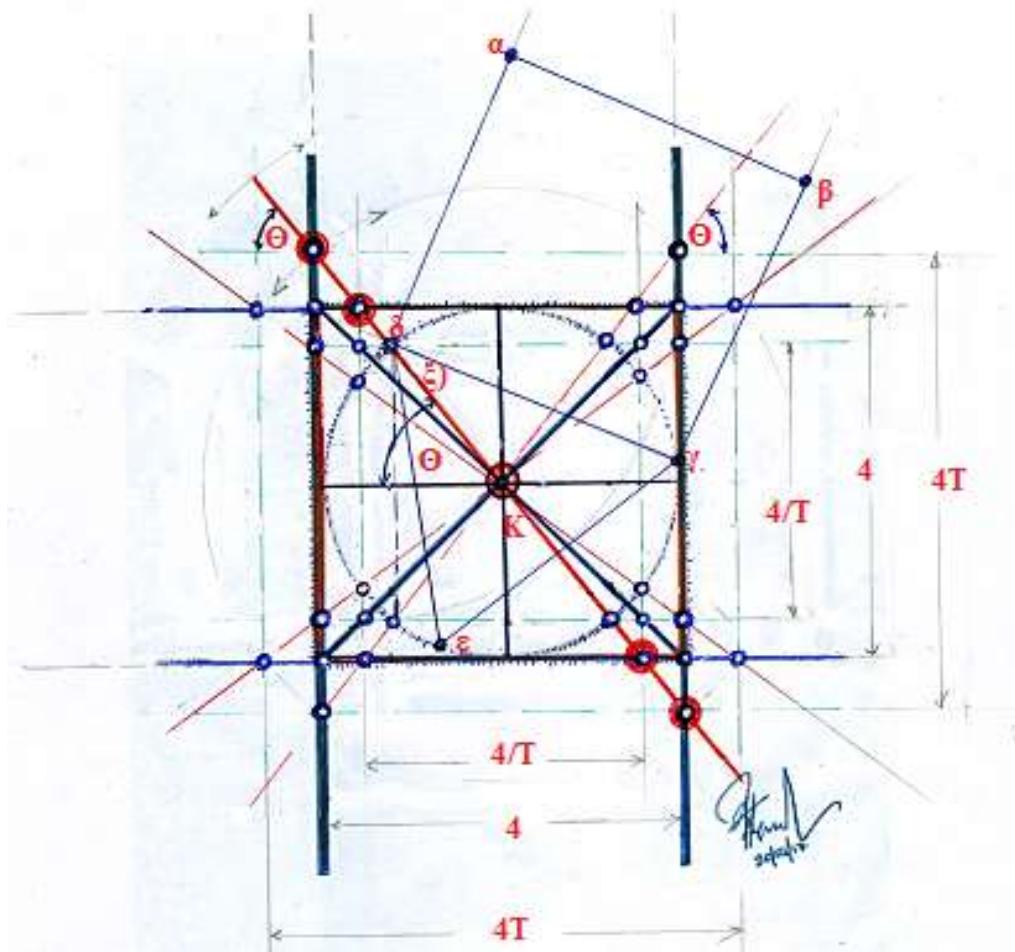
By Panagiotis Stefanides

TOOL GAUGE ROD STANDARDISATION





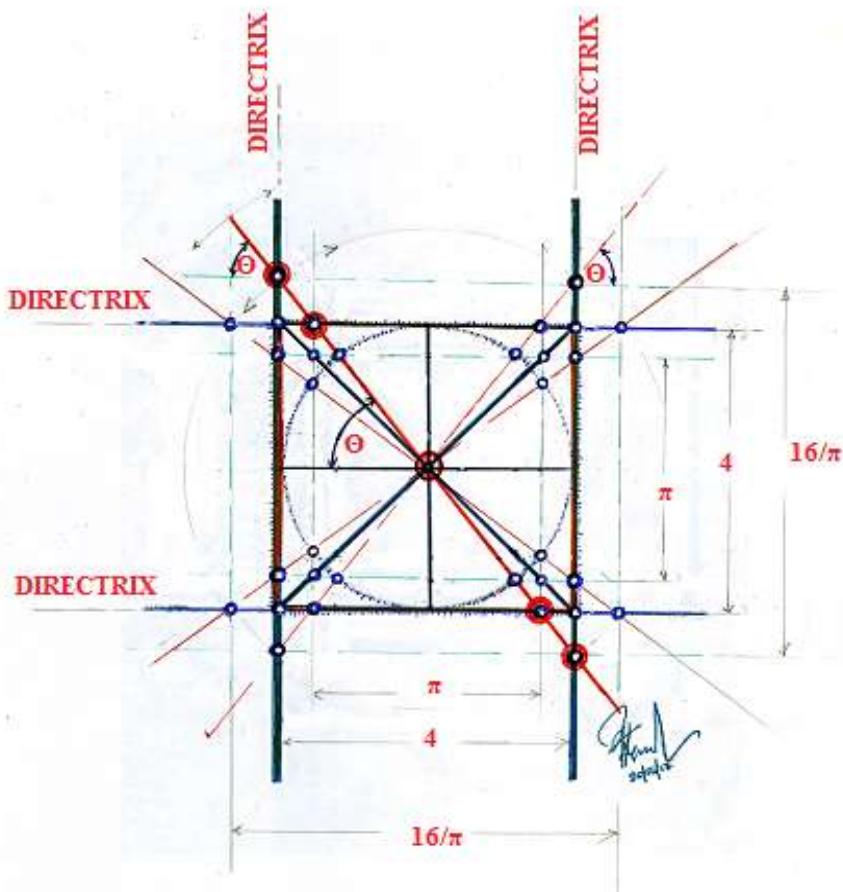




INSCRIBED CIRCLE IN SQUARE OF SIDE LENGTH 4 AND PERIMETER 16.

For $\pi=4/T$

Parallelogramme Base $4/T$ and Height 4, has Area $4[4/T]$ Equal to $16/T$, Equal to Circle's Area which is Equal to Circle's Circumference $4[4/T]$



**SQUARE SIDE 4 PERIMETER 16
INSCRIBED CIRCLE CIRCUMFERENCE 4π**

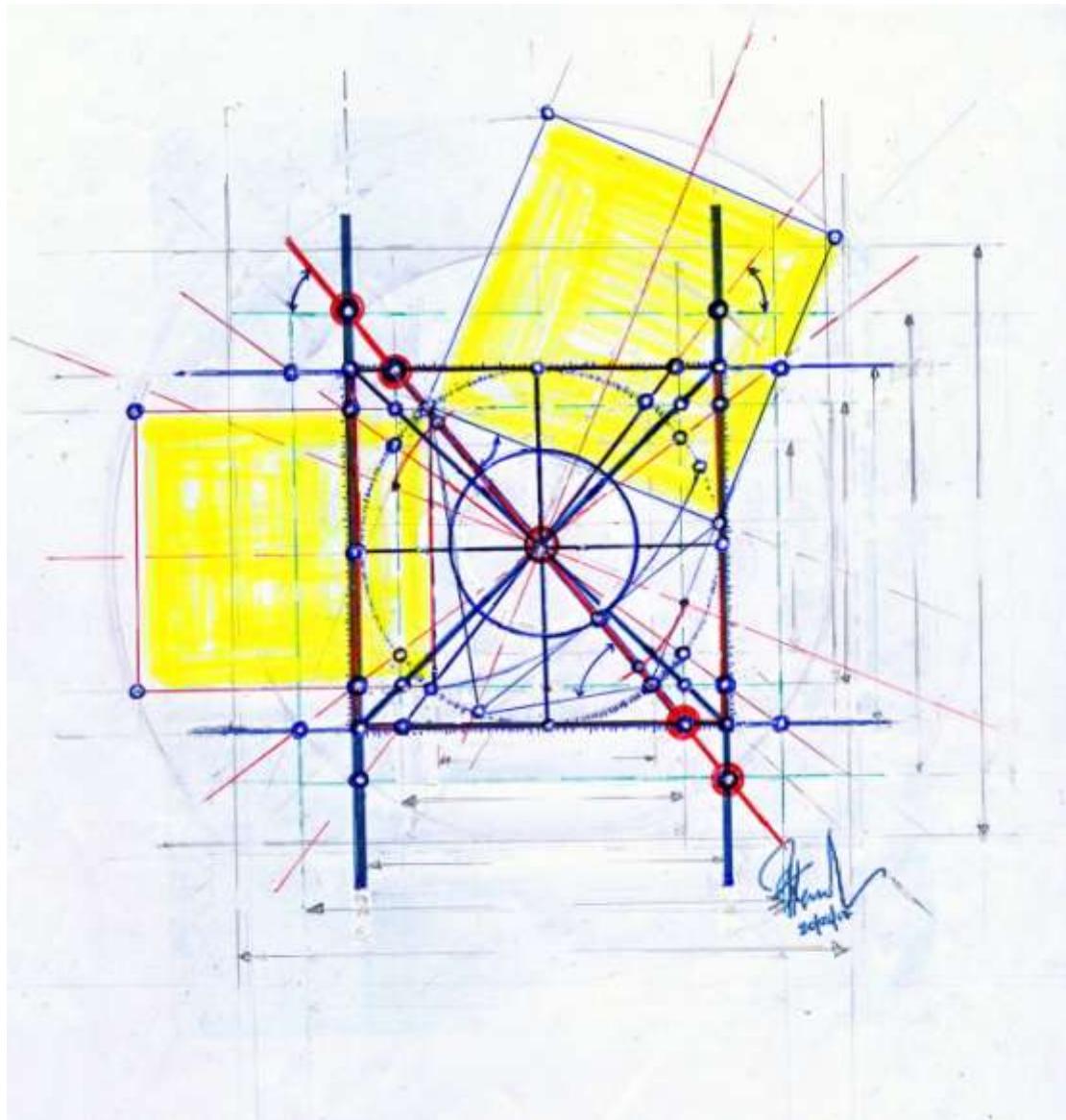
INSCRIBED CIRCLE IN SQUARE OF SIDE LENGTH 4 AND PERIMETER 16.

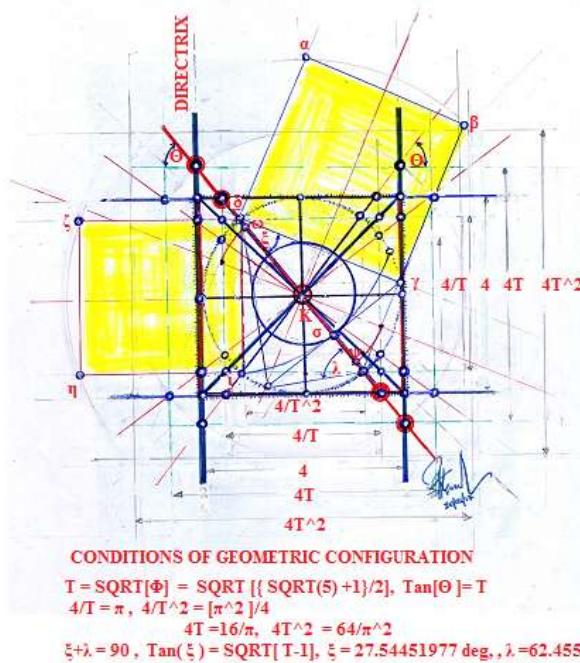
SQUARE'S PERIMETER TO CIRCLE'S CIRCUMFERENCE RATIO = $4/\pi$

Circle Area Equal 4π = Equal Circle's Circumference 4π .

SQUARE'S AREA TO CIRCLE'S AREA RATIO = $4/\pi$

Parallelogramme Base π and Height 4, has Area 4π Equal to Circle's Area 4π , which is Equal to Circle's Circumference 4π .





Angle Θ Drawn by Ruler and Compass According to:

<http://www.stefanides.gr/Html/gmr.html>

By Panagiotis Stefanides

Equation for π | Real, Irrational Roots of $\pi^4 + 16\pi^2 - 256 = 0$

For Condition that $\pi T = 4$ [$T^4 - T^2 - 1 = 0$]

Square Perimeter [$\delta\gamma\eta\tau$] = $4\pi = 4[4/T] = 16/T$

Inscribed Circle [to square side 4] has Circumference

Equal to $4\pi = 4[4/T] = 16/T$

Square [$\alpha\beta\gamma\delta$] Area = 4π [Application of Euclidean Theorem] =
 $= 4[4/T] = 16/T$
Side Length [$\gamma\delta$] = [$\alpha\beta$] = [$\beta\gamma$] = [$\alpha\delta$] = $\text{SQRT}[16/T] =$
 $= 2\{\text{SQRT}[4/T]\} = 2\{\text{SQRT}[\pi]\}$ shown on Red ROD as [$\psi\omega$] and $\pi = [\omega\sigma]$.

RED ROD ALLOWED TO ROTATE ABOUR K, IN ORDER TO ACCOMPLISH PROGRAMMED TASKS WITH RESPECT TO THIS CONFIGURATION.

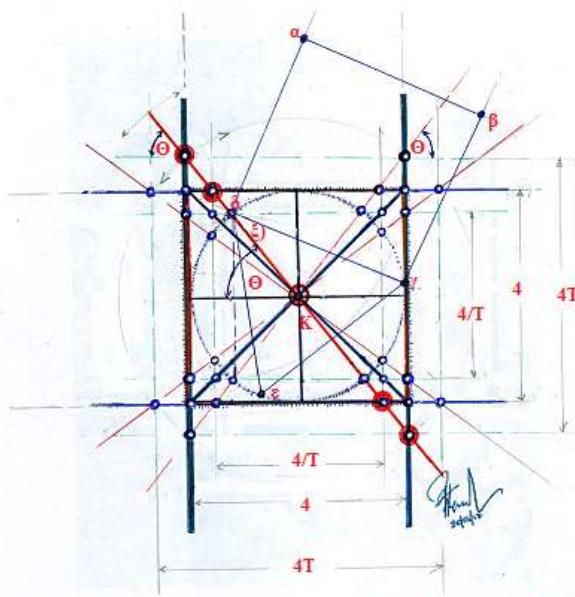
3D FLAT PRINTING IS ENVISAGED, WITH PIN HOLES, APPROPRIATELY LOCATING FOR MATCHING WITH ROD CORRESPONDING PINNING HOLES.

PINS MAY BE USED AS CONNECTING LINKS.

ROD, ACCORDINGLY PROVIDES CODIFIED INFORMATION WITH RESPECT TO LINEAR AND CIRCULAR LINEARITIES OBTAINED FROM THIS COMPOUND TOOL PACKAGE, WITH POSSIBLE USE IN EDUCATION.

SQUARES ARE IN RATIOS OF $4/\pi = 4[4/T] = T$

$\xi + \lambda = 90^\circ$, $\tan(\xi) = \text{SQRT}[T-1]$, $\xi = 27.54451977$ deg., $\lambda = 62.45548023$



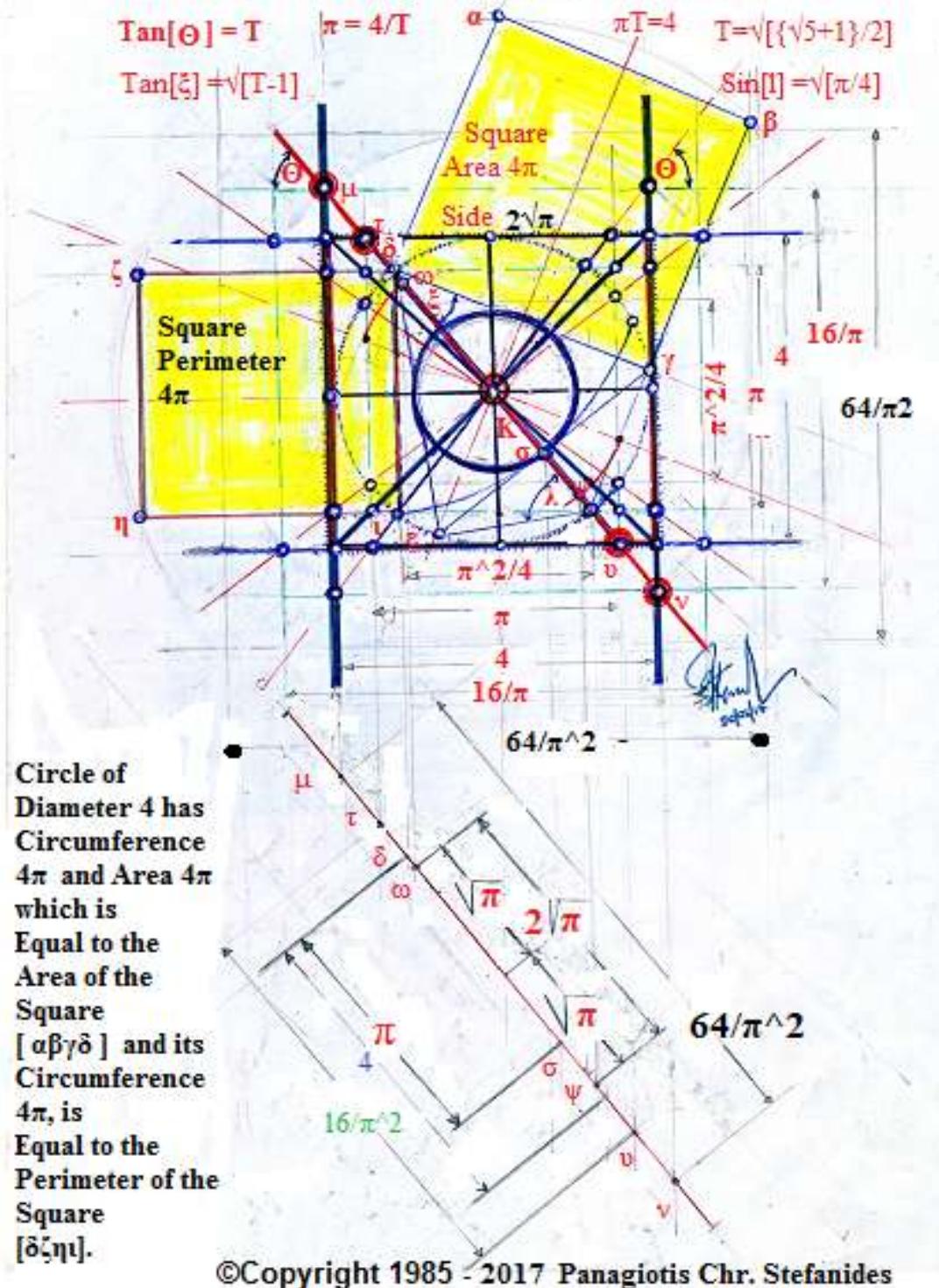
$\tan(\Theta) = T$, $\tan(\xi) = \text{SQRT}[T-1]$, $\Theta = 51.82729237$ Deg., $\xi = 27.54451975$ Deg.

CIRCLE CIRCUMFERENCE = $\pi D = 4\pi = 4[4/T] = 16/T$

for $\pi = 4/T$

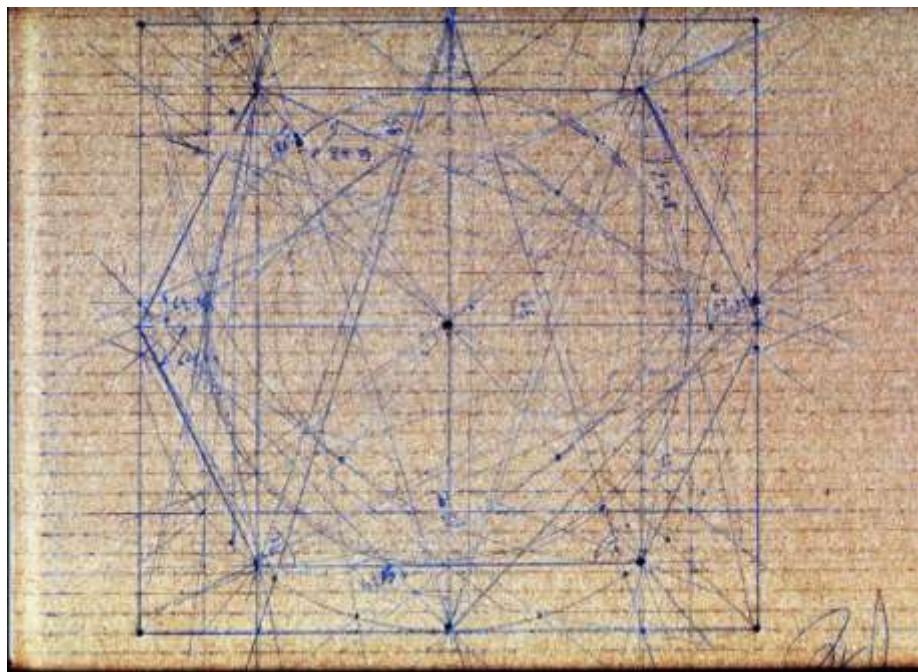
AREA OF CIRCLE = $4\pi = 16/T$ = AREA OF SQUARE [$\alpha\beta\gamma\delta$] = $[\delta\gamma]^*[\gamma\beta] = 4\pi = 4[4/T] = 16/T$, $= [\delta\gamma] = [\gamma\beta] = \text{SQRT}[16/T]$

TOOL GAUGE ROD STANDARDISATION



IMPORTANT DISCOVER

RESULTING RULER AND COMPASS CONFIGURATION, OF A VERY SPECIAL FORM, BASED ON THE SQUARE ROOT OF THE GOLDEN SECTION
By Panagiotis Stefanides:



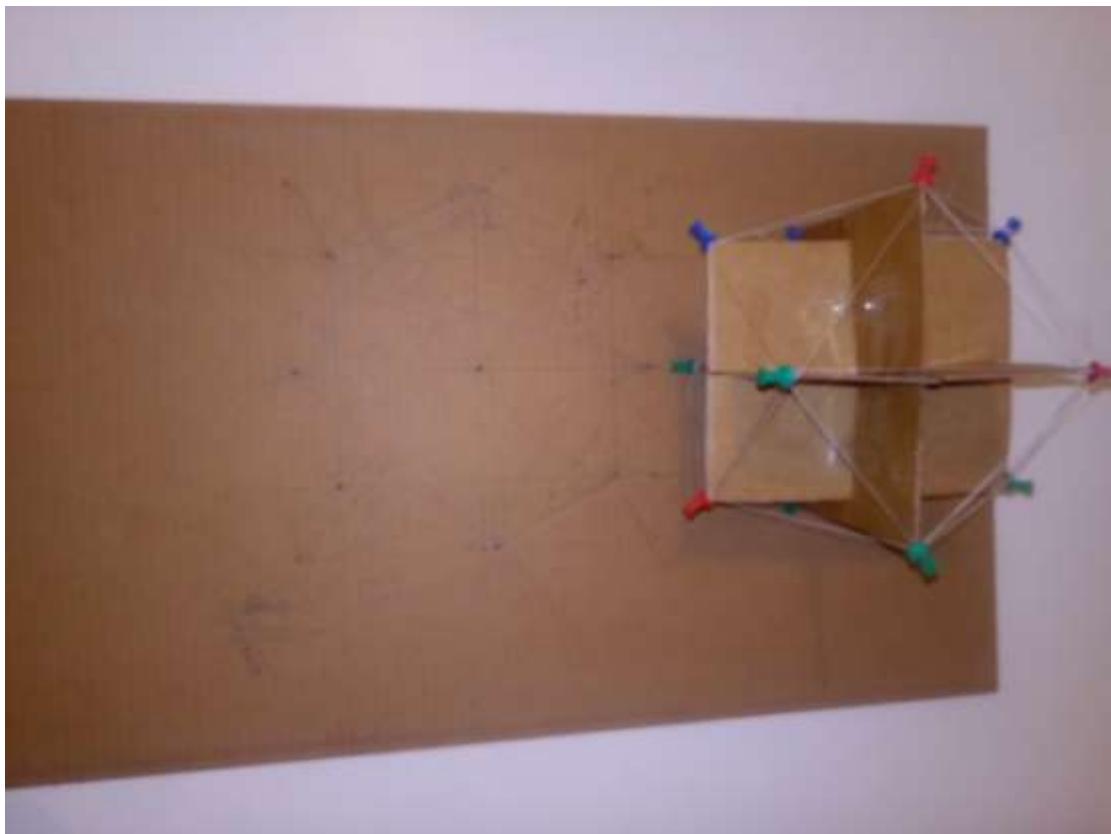
© Copyright 1985- 2017, Eur Ing Panagiotis Chr. Stefanides CEng MIET

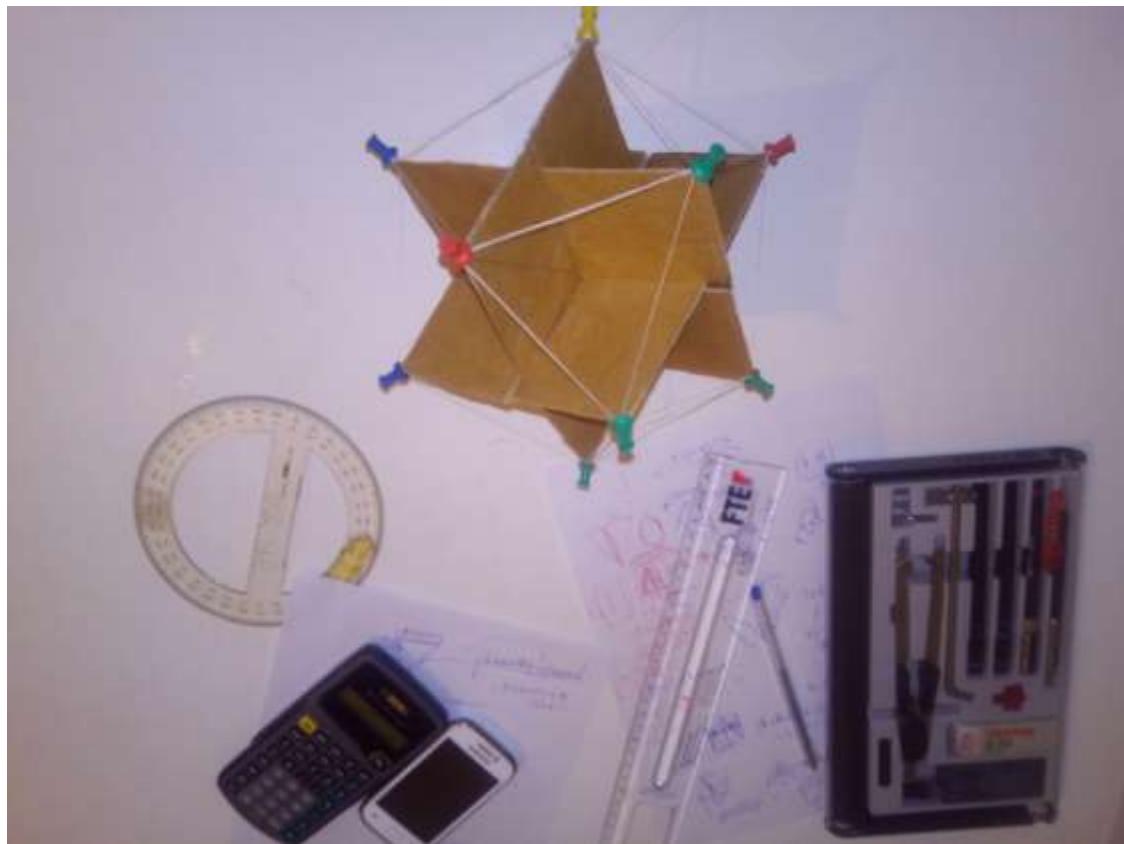


A NEW SOLID FORM CONSTRUCTED ON THE BASIS OF THE SQUARE ROOT OF THE GOLDEN SECTION By Panagiotis Stefanides

© Copyright 1985- 2017, Eur Ing Panagiotis Chr. Stefanides CEng MIET

IMPORTANT INVENTION



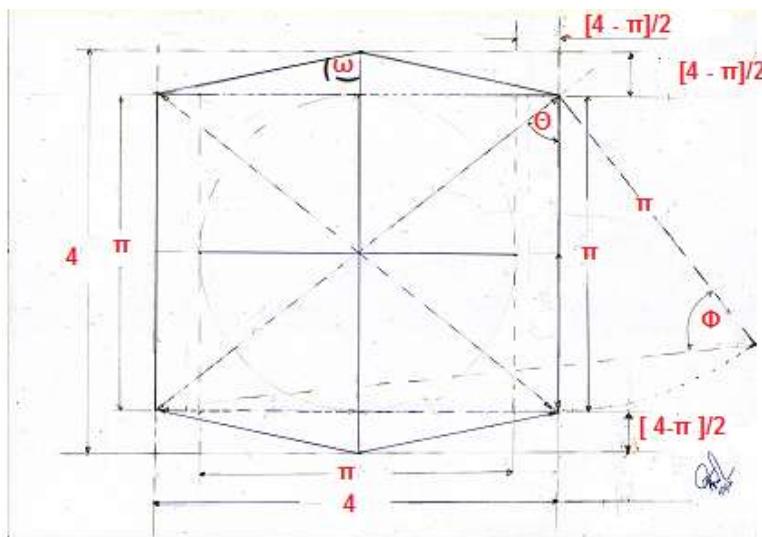


© Copyright 1985- 2017, Eur Ing Panagiotis Chr. Stefanides CEng MIET 



GENERATOR POLYHEDRON OF PLATONIC- EUCLIDEAN SOLIDS

By
Eur Ing Panagiotis Stefanides BSc(Eng)Lon(Hons)
 MSc(Eng)NTUA CEng MIET
 Chartered Engineer[UK]



**INSCRIBED TO SQUARE OF PERIMETER 4π ,
 CIRCLE WITH CIRCUMFERENCE π^2**

$$\tan[\Theta] = 4/\pi, \quad [\text{for } \pi = 4/T], \quad T = \sqrt{\{[(\sqrt{5} + 1)/2]}$$

$$\tan[\Phi] = \sqrt{4^2 + \pi^2}/\pi, \quad [\text{for } \pi = 4/T]$$

$$T = 1.27201965.., \quad \Theta = 51.82729237.. \text{ deg.}$$

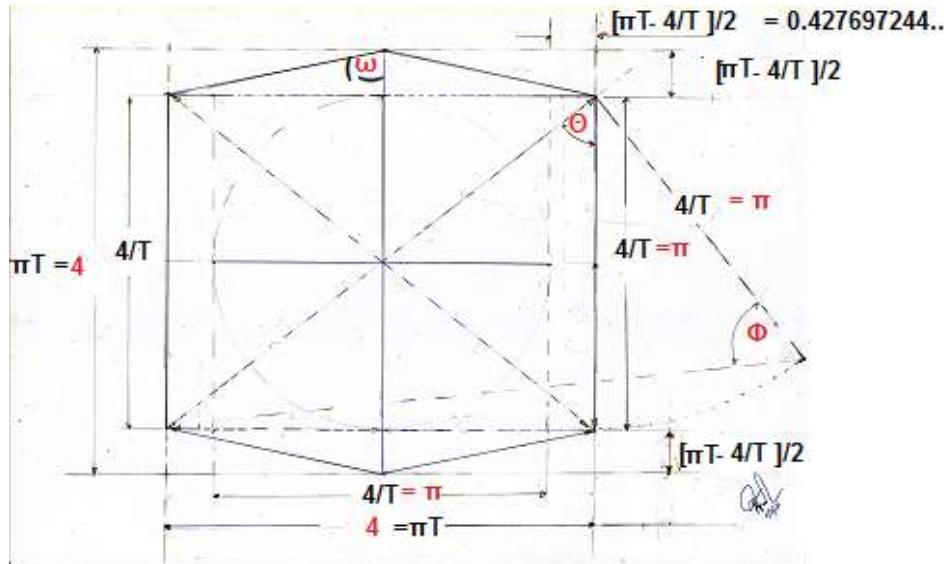
$$\pi = 3.14460551.. \quad \Phi = 58.28252559.. \text{ deg.}$$

$$[4 - \pi]/2 = 0.427697244.. \quad \text{for } \pi = 4/T$$

$$\tan[\omega] = (4/2) / [4 - \pi]/2 = 4 / [4 - \pi] = 4.676205016..$$

$$\omega = 77.92918912.. \text{ deg.}, \quad 90 - \omega = 12.07081088.. \text{ deg.}$$

$$\text{CONDITION THAT } \pi = 4 / \left[\sqrt{\frac{1}{2} (\sqrt{5} + 1)} \right] = 3.14460551$$



INSCRIBED TO SQUARE OF PERIMETER 4π , $=4[4/T] =16/T$
 CIRCLE WITH CIRCUMFERENCE π^2

$$\tan[\Theta] = 4/\pi, \quad [\text{for } \pi = 4/T], \quad T = \sqrt{\{(\sqrt{5} + 1)/2\}}$$

$$\tan[\Phi] = \sqrt{4^2 + \pi^2}/\pi, \quad [\text{for } \pi = 4/T]$$

$$T = 1.27201965.., \quad \Theta = 51.82729237.. \text{ deg.}$$

$$\pi = 3.14460551.., \quad \Phi = 58.28252559.. \text{ deg.}$$

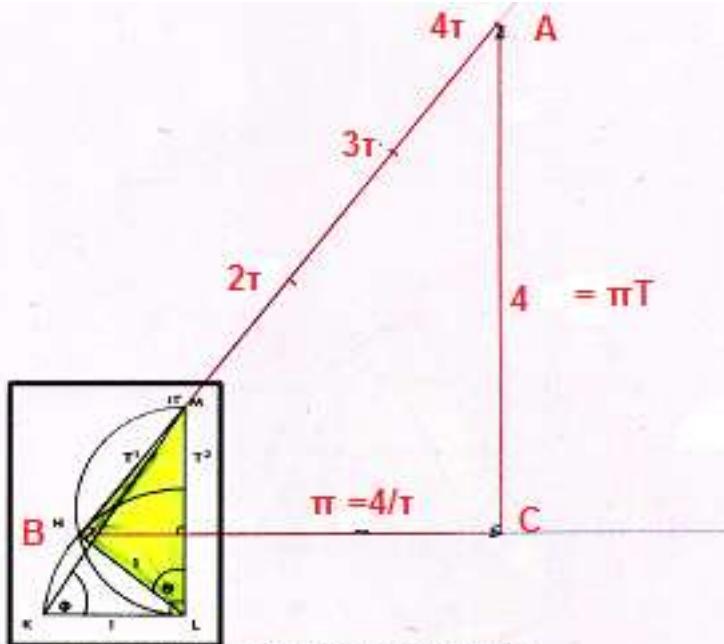
$$[4 - \pi]/2 = 0.427697244.. \quad \text{for } \pi = 4/T \quad 3.14460551..$$

$$\tan[\omega] = (4/2) / [4 - \pi]/2 = 4 / [4 - \pi] = 4.676205016..$$

$$\omega = 77.92918912.. \text{ deg.}, \quad 90 - \omega = 12.07081088.. \text{ deg.}$$

$$\text{CONDITION THAT } \pi = 4 / \left[\sqrt{\frac{1}{2} (\sqrt{5} + 1)} \right] = 3.14460551$$

© Copyright 1985- 2017, Eur Ing Panagiotis Chr.
Stefanides CEng MIET



Geometric Mean Ratio (T) by Ruler and Compass
[QUADRATURE TRIANGLE MLN]

- (1) DRAW TRIANGLE MLK (ORTHOGONAL)
- (2) DRAW SEMICIRCLE DIAMETER D = (ML) = 1.618033989
- (3) DRAW QUARTERCIRCLE RADIUS R = (KL) = 1
- (4) (NL) = (KL) = 1

$$\tan \theta = 1.618033989$$

$$\tan \theta = \sqrt{1.618033989} \\ = 1.27201965$$

$$\tan \theta = \sqrt{\tan^2 \theta}$$

$$T^2, T^2, 1 = 0$$

$$ML = 1.618033989 = T^2$$

$$(ML)^2 = 2.618033989$$

$$MN = \sqrt{2.618033989 \cdot 1}$$

$$MN = \sqrt{1.618033989} = T$$

$$T = 1.27201965$$

$$[AB] * [BC] = [AC]^2$$

$$[4T] * [4/T] = 4^2 = 16$$

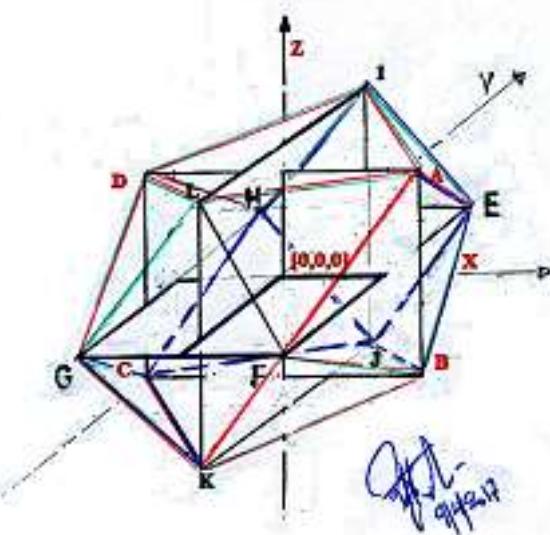
CONDITION:

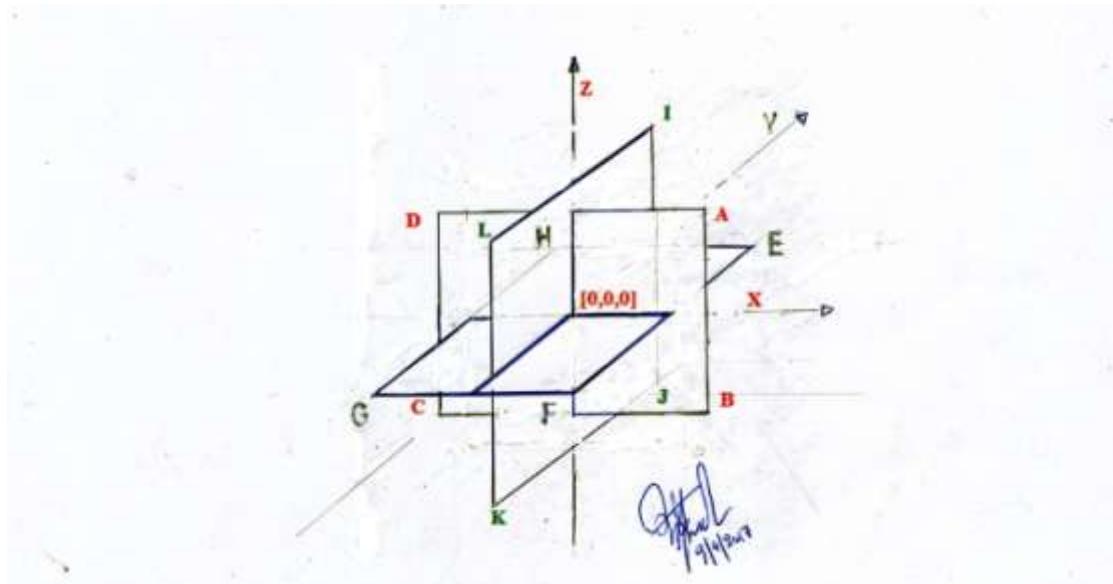
$$\pi = \sqrt{[\sqrt{5} + 1]/2}$$



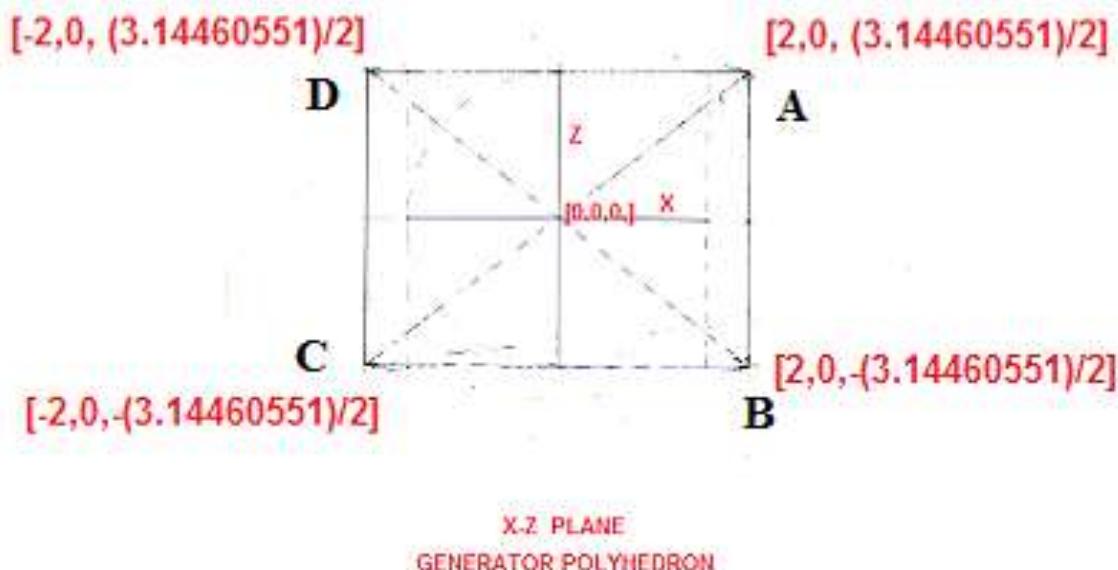
X-Y-Z COORDINATES' DEFINITION OF PLATONIC- EUCLIDEAN SOLIDS' GENERATOR POLYHEDRON

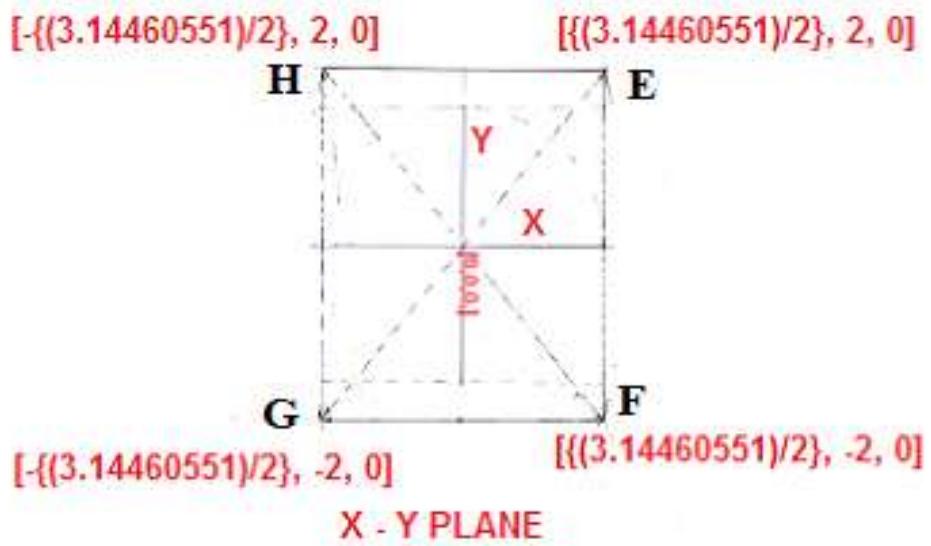
By
Eur Ing Panagiotis Stefanides BSc(Eng)Lon(Hons)
 MSc(Eng)NTUA CEng MIET
 Chartered Engineer[UK]



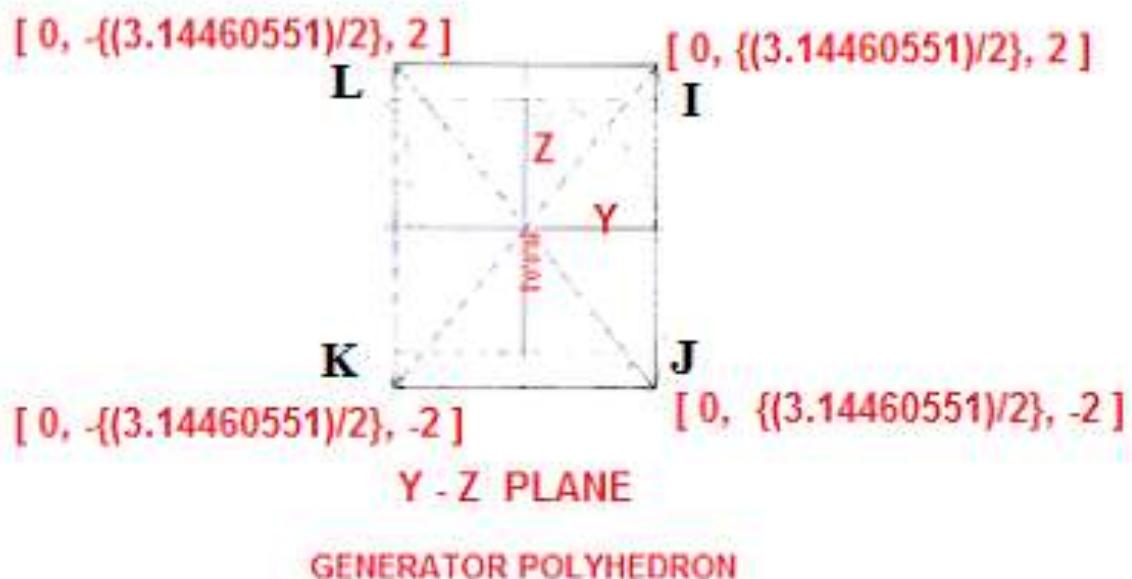


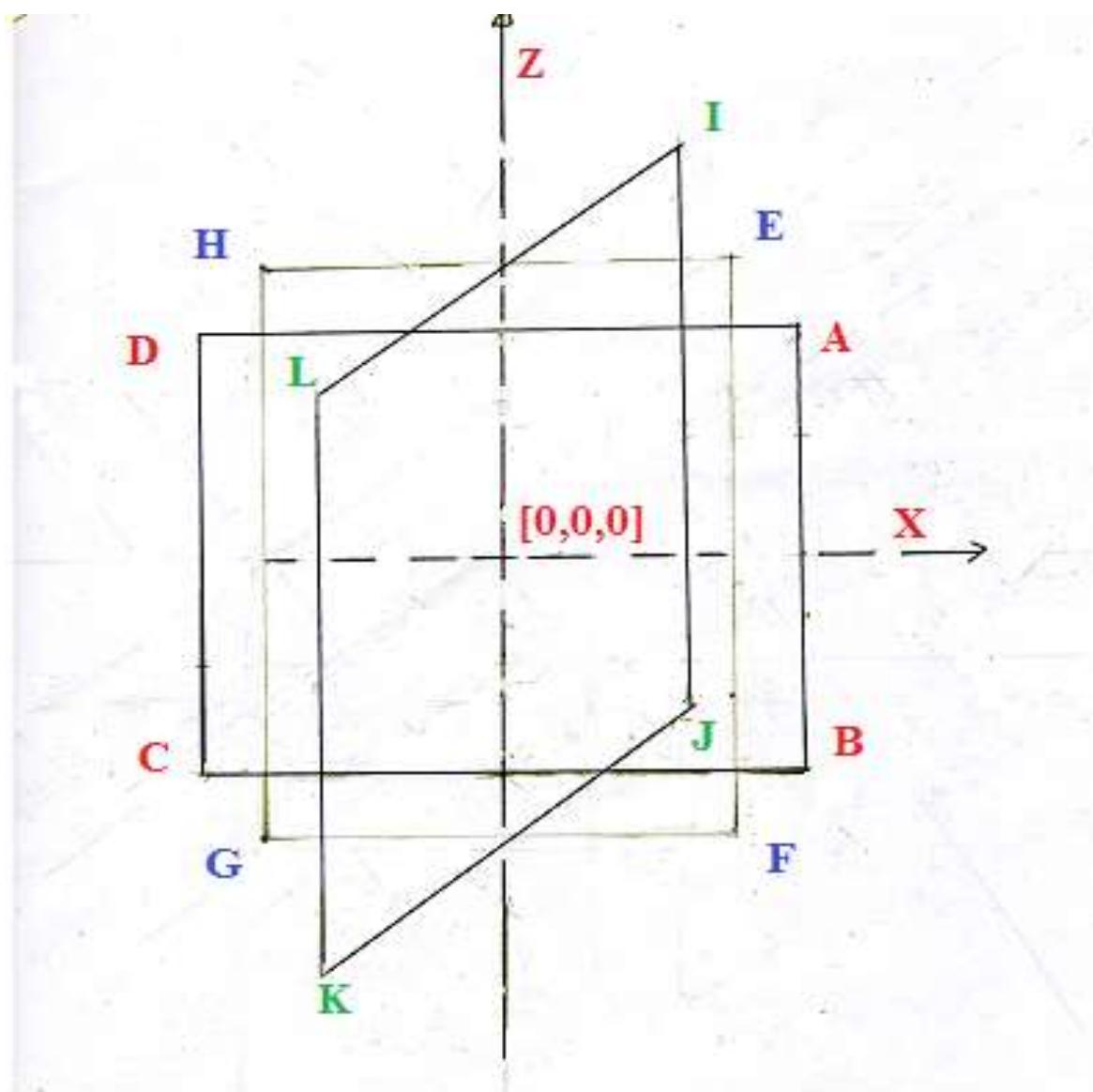
CONDITION THAT $\pi = 4 / \left[\sqrt{\frac{1}{2} (\sqrt{5} + 1)} \right] = 3.14460551$

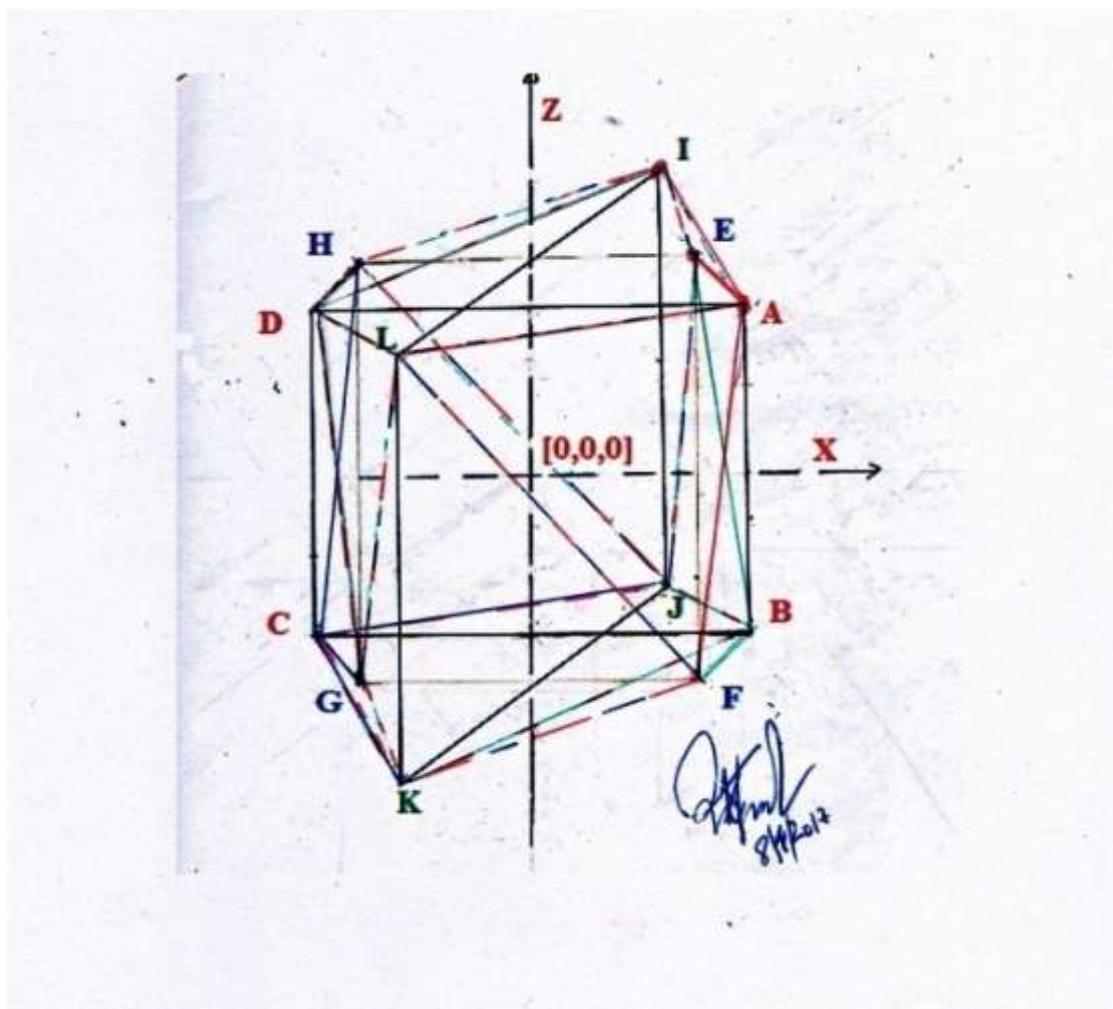


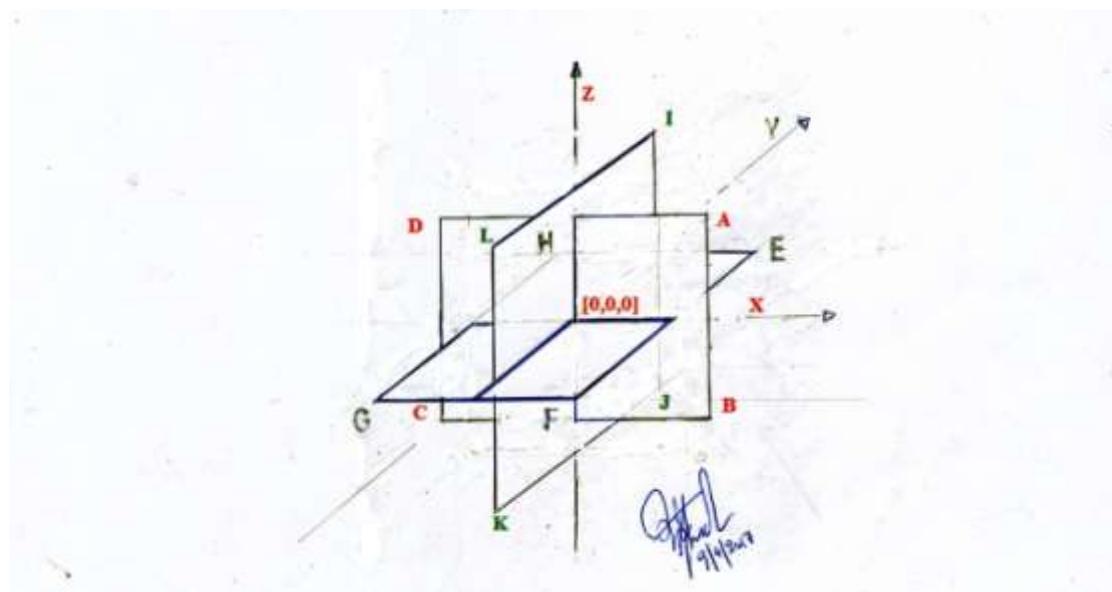


GENERATOR POLYHEDRON









PLANES' VERTICES COMBINATIONS OF CONNECTIONS

AE, AF, AI, AL

BF, BK, BE, BJ

CK, CG, CH, CJ

DI, DL, DG, DH

IA, IE, ID, IH

JE, JH, JB, JC

KB, KC, KF, KG

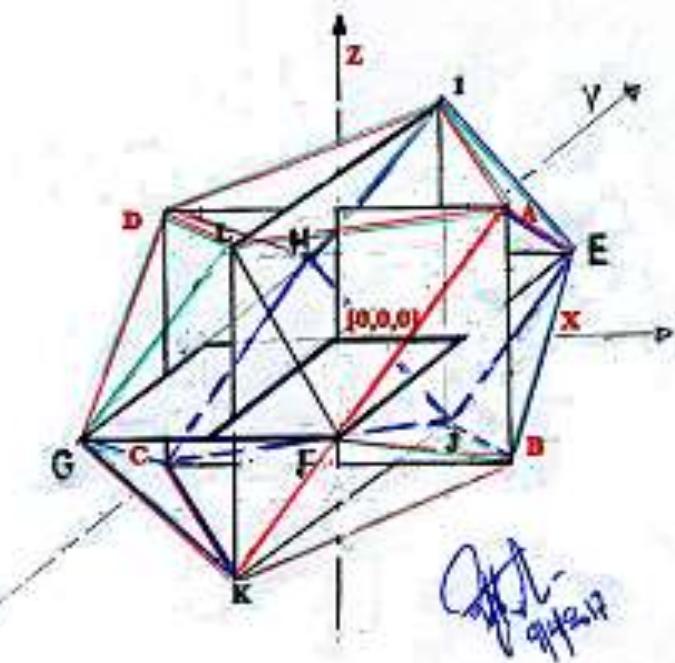
LA, LD, LF, LG

EA, EB, EI, EJ

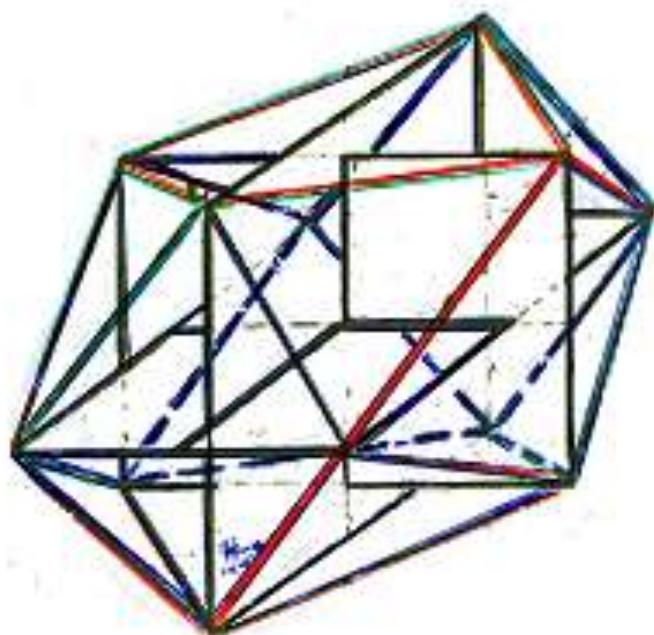
FA, FB, FK, FL

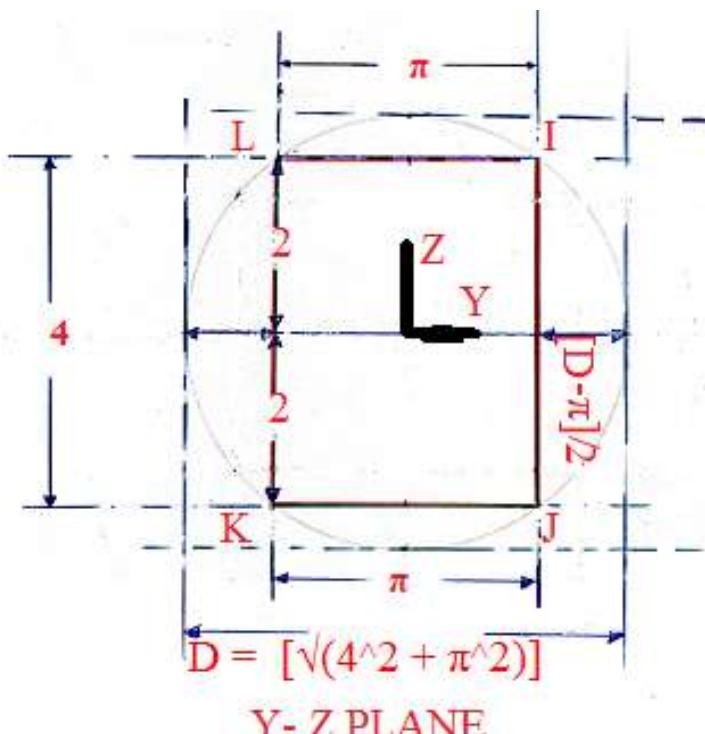
GK, GL, GC, GD

HC, HD, HI, HJ



https://www.researchgate.net/publication/315801180_GENERATOR_POLYHEDRON_OF_PLATONIC-EUCLEIDEAN_SOLIDS_By_Panagiotis_Stefanides_1A

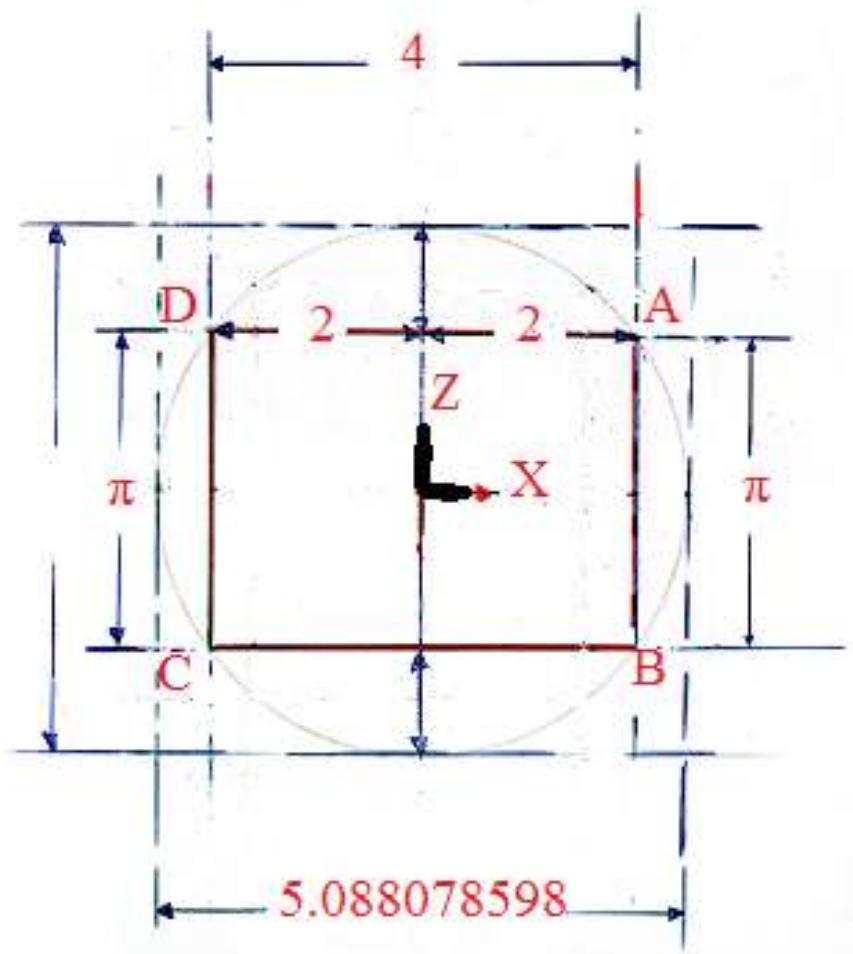


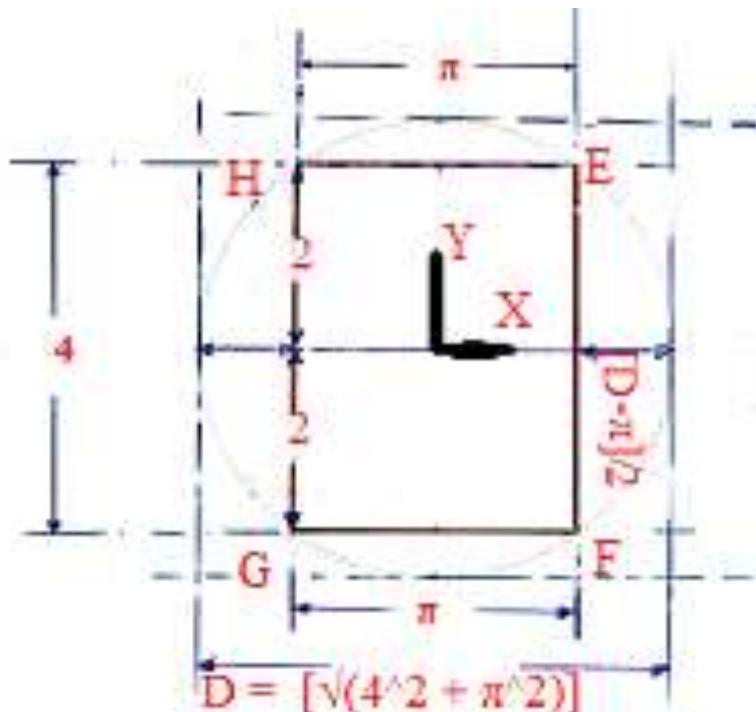


CONDITION THAT CIRCLE'S DIAMETER

$$D = [\sqrt{(4^2 + \pi^2)}] = 5.088078598, \text{ for } \pi = \\ \pi = 4 / [\sqrt{(\sqrt{5} + 1)/2}] = 3.14460551$$

$$\{[D-\pi]/2\} * [\pi + \{[D-\pi]/2\}] = 2^2 = 4$$



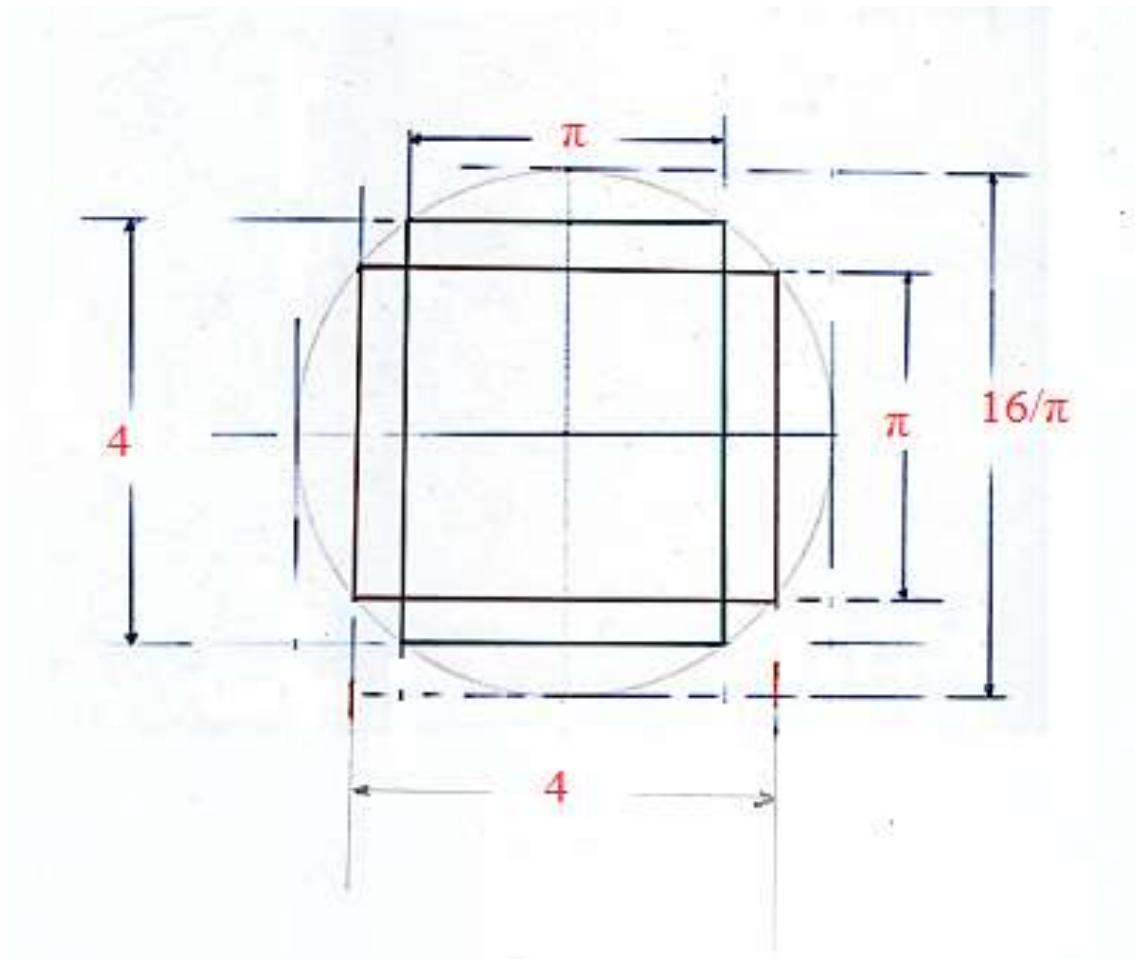


X-Y PLANE

CONDITION THAT CIRCLE'S DIAMETER

$$D = \sqrt{4^2 + \pi^2} = 5.088078598, \text{ for } \pi = \\ \pi = 4 / \sqrt{\{\sqrt{5} + 1\}/2} = 3.14460551$$

$$\{[D-\pi]/2\} * [\pi + \{[D-\pi]/2\}] = 2^2 = 4$$



CONDITION THAT $\pi = 4 / \left[\sqrt{\frac{1}{2}(\sqrt{5} + 1)} \right] = 3.14460551$

$$\alpha = \sqrt{[(4-\pi)/2]^2 + 2^2} = 2.045220021$$

$$\beta = [4-\pi]/2 = 0.427697244$$

$$\gamma = \sqrt{\alpha^2 + (\pi/2)^2} = 2.579740469$$

CONDITION

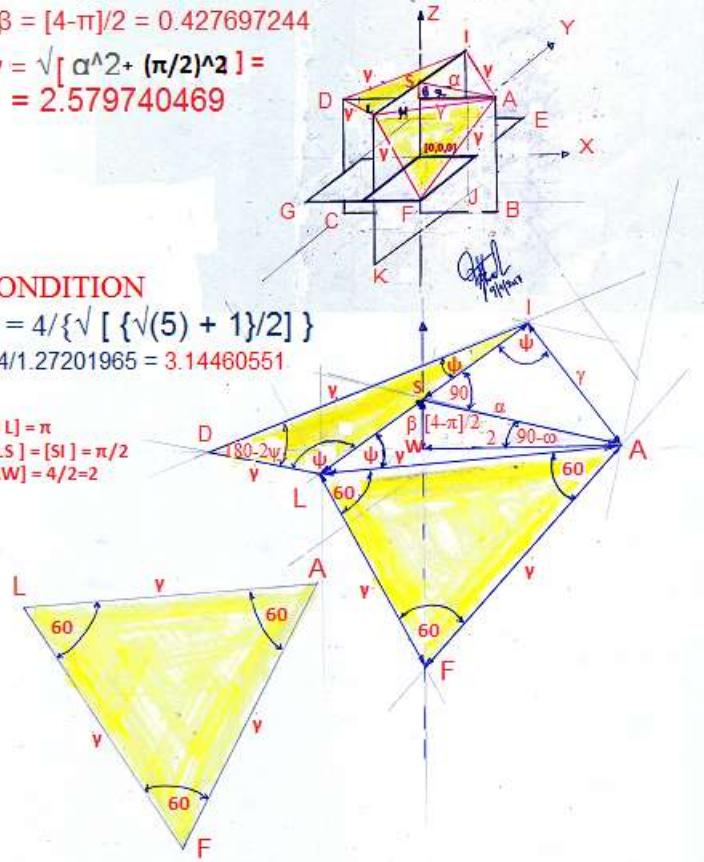
$$\pi = 4/\{\sqrt{(\sqrt{5} + 1)/2}\}$$

$$= 4/1.27201965 = 3.14460551$$

$$[IL] = \pi$$

$$[LS] = [SI] = \pi/2$$

$$[AW] = 4/2 = 2$$



$$\alpha = \sqrt{[(4-\pi)/2]^2 + 2^2} = 2.045220021$$

$$\tan[\psi] = \alpha/(\pi/2) = (2.045220021)/(1.572302757) = 1.300780027$$

$$\psi = \text{ArcTan}[1.300780027] = 52.44801593 \text{ deg.}$$

$$2\psi = 104.8960319 \text{ deg.}$$

$$[180 - 2\psi] = 75.10396814 \text{ deg.}$$

$$\tan[\omega] = 2/[(4-\pi)/2] = 4.676205016$$

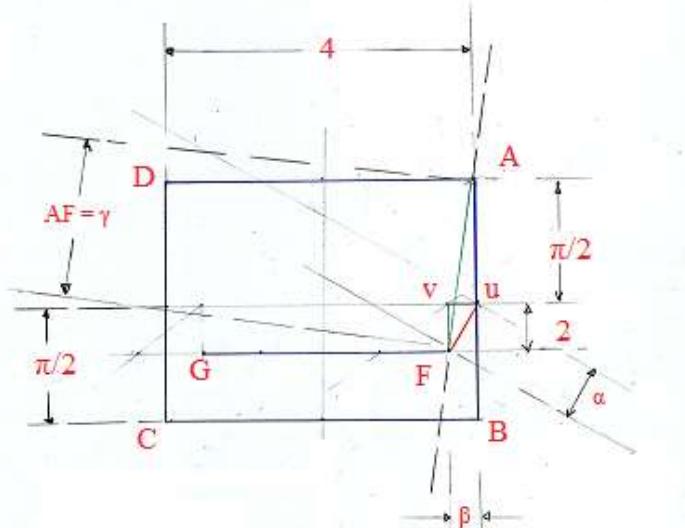
$$\omega = \text{ArcTan}[4.676205016] = 77.92918912 \text{ deg.}$$

$$[90-\omega] = [90 - 77.92918912] = 12.07081088 \text{ deg.}$$

$$2\omega = 155.8583782 \text{ deg.}$$

$$[180 - 2\omega] = 24.14162176 \text{ deg.}$$

$$\beta = [4-\pi]/2 = 0.427697244 = uv, \quad vF = 2, \quad uF = a = 2.045220021, \quad Au = \pi/2, \quad AF = 2.579740469 = \gamma$$



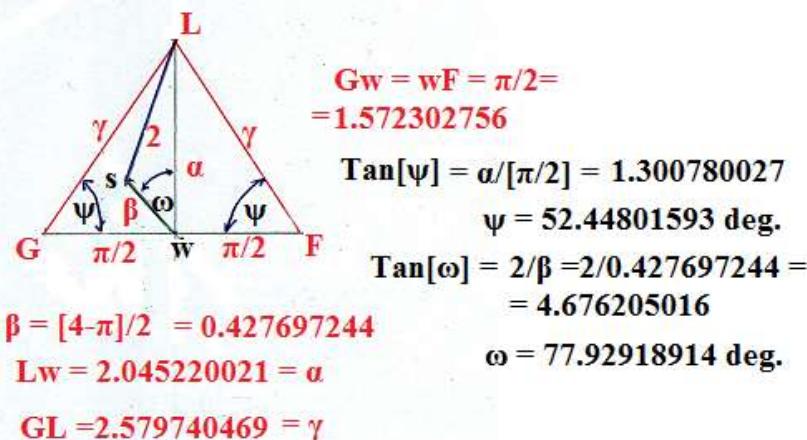
$$a^2 = [uF]^2 = [vu]^2 + 2^2 = \beta^2 + 2^2 = [(4-\pi)/2]^2 + 4 \\ a = 2.045220021$$

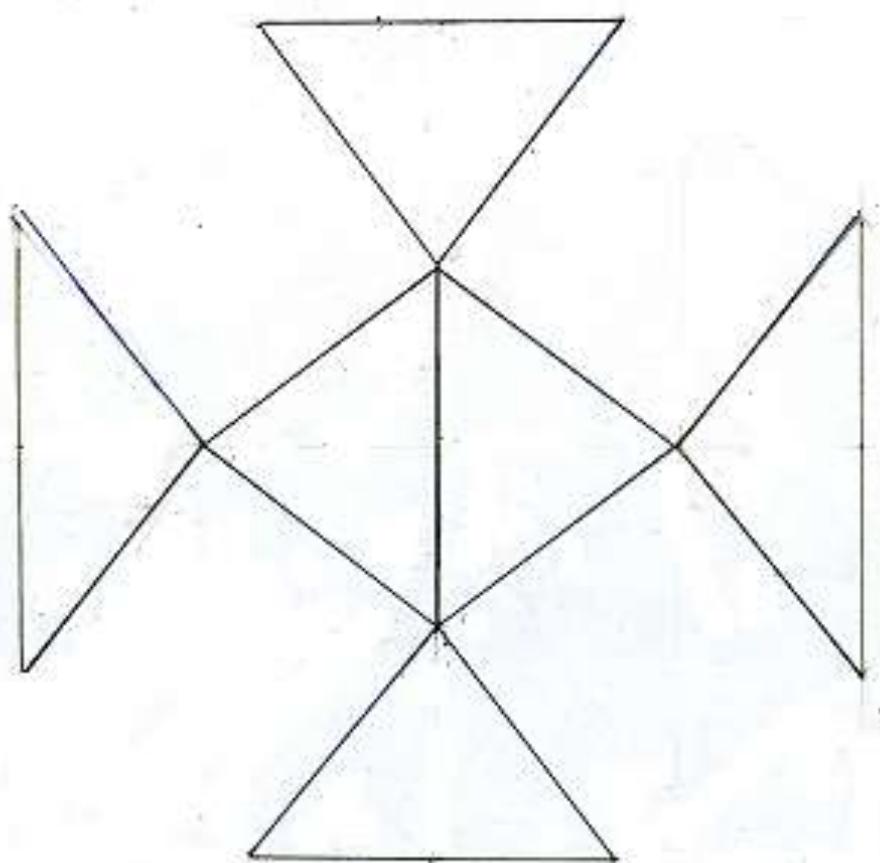
$$[AF]^2 = [Au]^2 + [uF]^2 \\ = [\pi/2]^2 + [a]^2 = 2.579740469$$

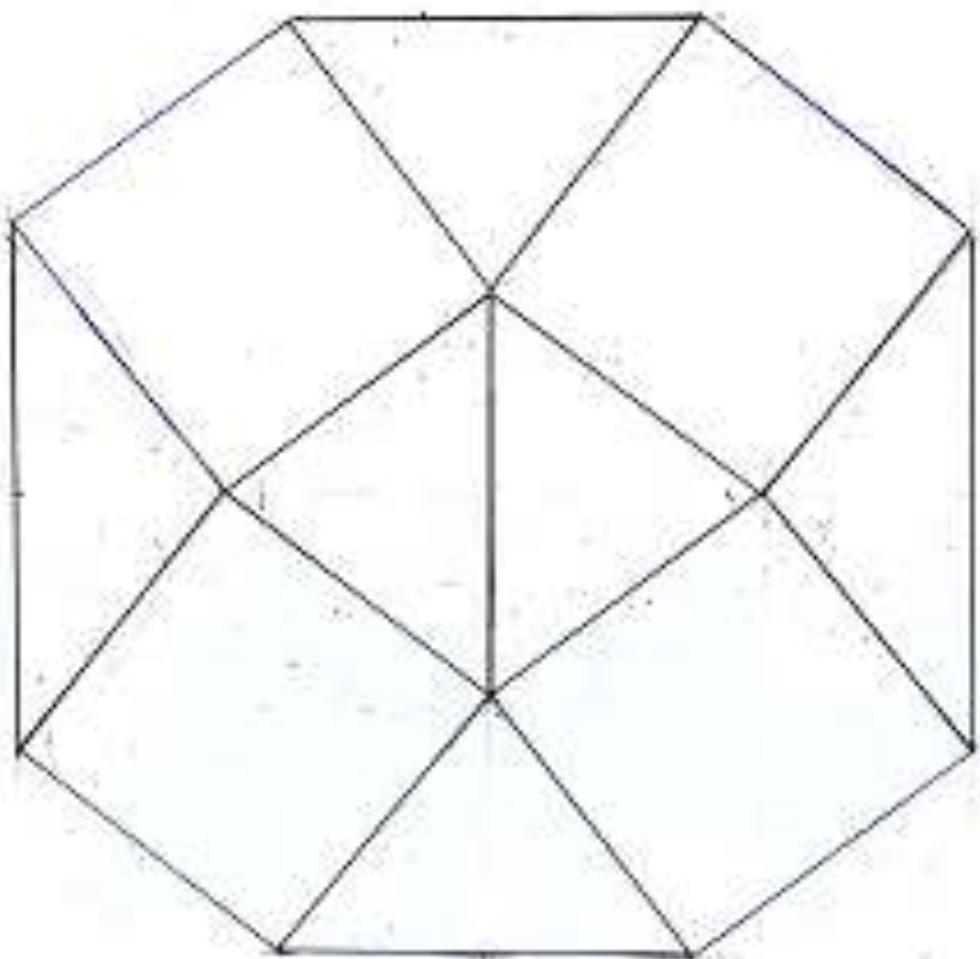
$$[vF]/[vu] = 2/\beta = 2/0.427697244 = 4.676205021 = \tan[\omega], \quad \omega = 77.92918914 \text{ deg.} \\ [Fu]/[Au] = a/\pi/2 = 2.045220021 / 1.572302756 = 1.300780027 = \tan[\psi], \quad \psi = 52.44801593 \text{ deg.}$$

© Copyright 1985- 2017, Eur Ing Panagiotis Chr. Stefanides CEng MIET

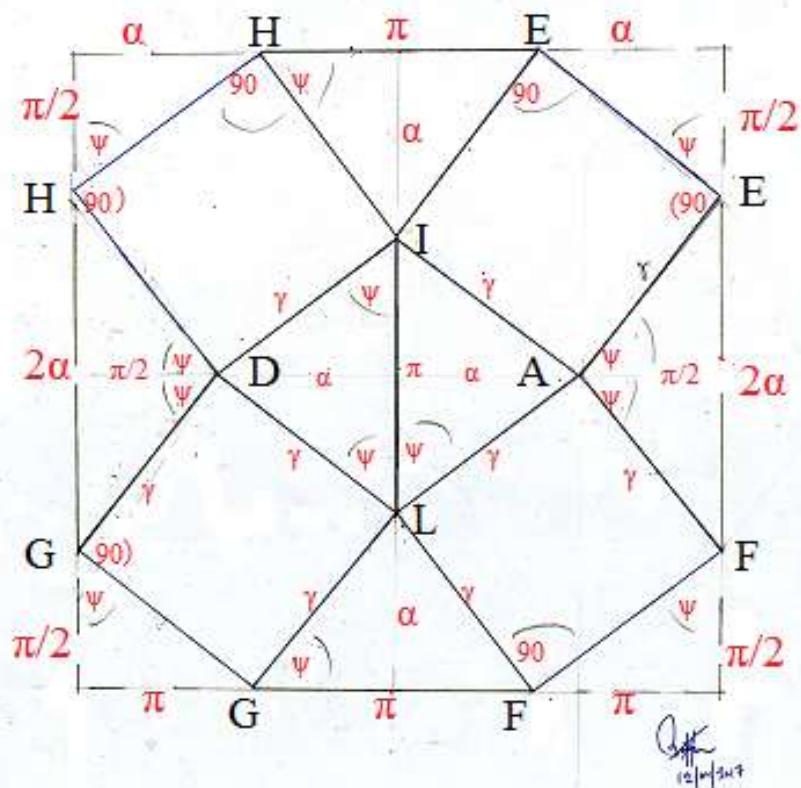
CONDITION THAT $\pi = 4 / [1.27201965] = 3.14460551$







© Copyright 1985- 2017, Eur Ing Panagiotis Chr. Stefanides CEng MIET 



© Copyright 1985- 2017, Eur Ing Panagiotis Chr.
Stefanides CEng MIET

ADDENDUM 2



Important Discovery

RULER AND COMPASS STRUCTURING OF DODECAHEDRON PENTAGON By Panagiotis Stefanides

For $\pi = 4/\text{SQRT(Golden Ratio)}$

From the geometry of the “**GENERATOR POLYHEDRON**”, we find relationships:

3 parallelogrammes vertical to each-other. Sides' lengths, of each parallelogramme, are in ratio of $4/\pi = 1.27201965$ [for $\pi = 3.14460551$ i.e. **$4/\text{SQRT(Golden Ratio)}$**].

$$[4/2]/[\pi/2] = [\pi/2]/x, \quad x = \{[\pi/2]^2\}/[4/2] = 2.472135953/2 = 1.236067977 = 1/[\text{Sin}(54)] = x$$

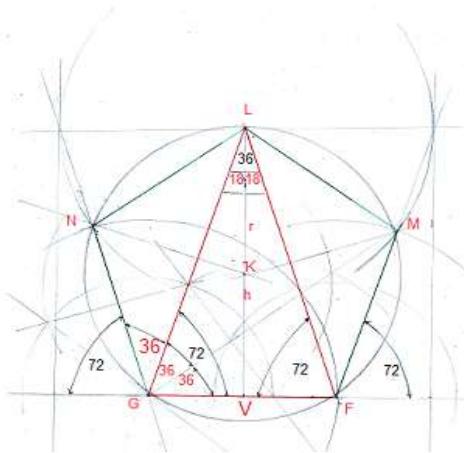
This is directly Related to the Pentagon Angle of 54 Deg:

$$1/\text{Sin}(54) = 1.236067978$$

$$r/h = \{ [1/2]/\text{Cos}(54)\} / r\text{Sin}(54) = 0.850650808 / 0.68819096 = 1.236067977$$

$$1/\text{Sin}(54) = 1.236067978$$

© Copyright 1985- 2017, Eur Ing Panagiotis Chr. Stefanides CEng MIET
 $[1/\text{sin}(54) = 1.236067978]$ $r = (1/2)/[\text{cos}(54)] = 0.850650808$ $h = r\text{sin}(54) = 0.68819096$
 $H = r+h = 1.538841768$



Sum of

angles : $36+36+36+72 = 180$ Deg.

Angle VGN = $3*36 = 108$ Deg. $108/2 = 54$ Deg

$$r = [1/2]/\text{Cos}(54) = 0.850650808, \quad h = r\text{Sin}(54) = 0.68819096$$

$$r/h = r/r\text{Sin}(54) = 1/[\text{Sin}(54)] = 1.236067978$$

$$r/h = \{ [1/2]/\cos(54)\} / r\sin(54) = 0.850650808 / 0.68819096 = 1.236067977$$

$$1/\sin(54) = 1.236067978$$

From the geometry of the “**GENERATOR POLYHEDRON**”, we find relationships:

3 parallelogrammes vertical to each-other. Sides’ lengths, of each parallelogramme, are in ratio of $4/\pi = 1.27201965$ [for $\pi = 3.14460551$ i.e. **4/SQRT(Golden Ratio)**].

$$[4/2] / [\pi/2] = [\pi/2] / x, \quad x = \{[\pi/2]^2\}/[4/2] = 2.472135953/2 = 1.236067977 = 1 / [\sin(54)] = x$$

$$[1/\cos 72] = 1 / 0.09016994 = 3.236067978, \quad [1/\cos 72] + 1 = 4.236067978 = \text{CUBE of}$$

1.618033989 [structuring the **ICOSAHEDRON** and **DODECAHEDRON**].

1.618033989 = $\sqrt{2.618033989}$ structuring the **DODECAHEDRON** and its ROOT = **1.27201965** [structuring the **GENERATOR POLYHEDRON**].

The relationships, above, demonstrate “**Roots Structuring the Platonic-Euclidean Polyhedra**”

<https://www.linkedin.com/pulse/generator-polyhedron-platonic-euclidean-solids-panagiotis-stefanides>





GENERATOR POLYHEDRON OF PLATONIC-EUCLEIDEAN SOLIDS By
Panagiotis Stefanides 1A

https://www.researchgate.net/publication/315801180_GENERATOR_POLYHEDRON_OF_PLATONIC-EUCLEIDEAN_SOLIDS_By_Panagiotis_Stefanides_1A

$$\alpha = \sqrt{[(4-\pi)/2]^2 + 2^2} = 2.045220021$$

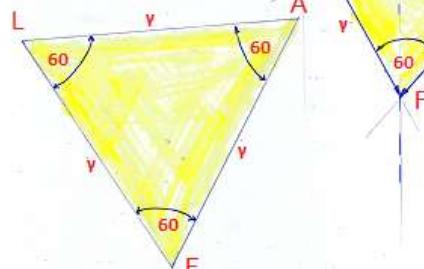
$$\beta = [4-\pi]/2 = 0.427697244$$

$$\gamma = \sqrt{\alpha^2 + (\pi/2)^2} = \\ = 2.579740469$$

CONDITION

$$\pi = 4/\{\sqrt{[\sqrt{5} + 1]/2}\} \\ = 4/1.27201965 = 3.14460551$$

$$[IL] = \pi \\ [LS] = [SI] = \pi/2 \\ [AW] = 4/2 = 2$$



$$\alpha = \sqrt{[(4-\pi)/2]^2 + 2^2} = 2.045220021$$

$$\tan[\psi] = \alpha/(\pi/2) = (2.045220021)/(1.572302757) = 1.300780027$$

$$\psi = \text{ArcTan}[1.300780027] = 52.44801593 \text{ deg.}$$

$$2\psi = 104.8960319 \text{ deg.}$$

$$[180 - 2\psi] = 75.10396814 \text{ deg.}$$

$$\tan[\omega] = 2/[(4-\pi)/2] = 4.676205016$$

$$\omega = \text{ArcTan}[4.676205016] = 77.92918912 \text{ deg.}$$

$$[90 - \omega] = [90 - 77.92918912] = 12.07081088 \text{ deg.}$$

$$2\omega = 155.8583782 \text{ deg.}$$

$$[180 - 2\omega] = 24.14162176 \text{ deg.}$$

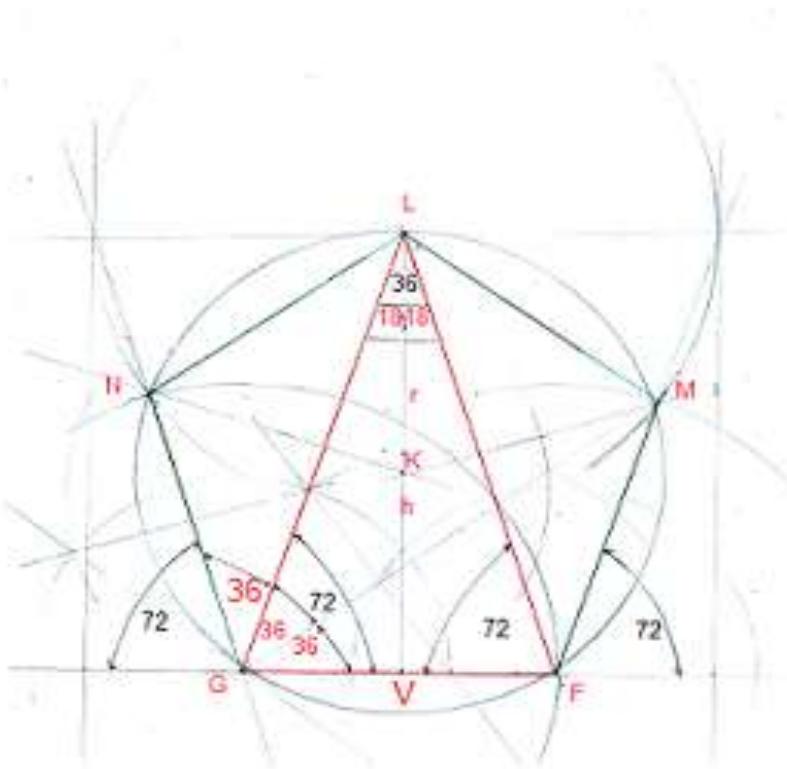
© Copyright 1985- 2017, Eur Ing Panagiotis Chr. Stefanides CEng MIET

$$\frac{1}{\sin(54)} = 1.236067978$$

$$r = (1/2)/[\cos(54)] = 0.85650808$$

$$h = r \sin(54) = 0.68819096$$

$$H = r + h = 1.538841768$$

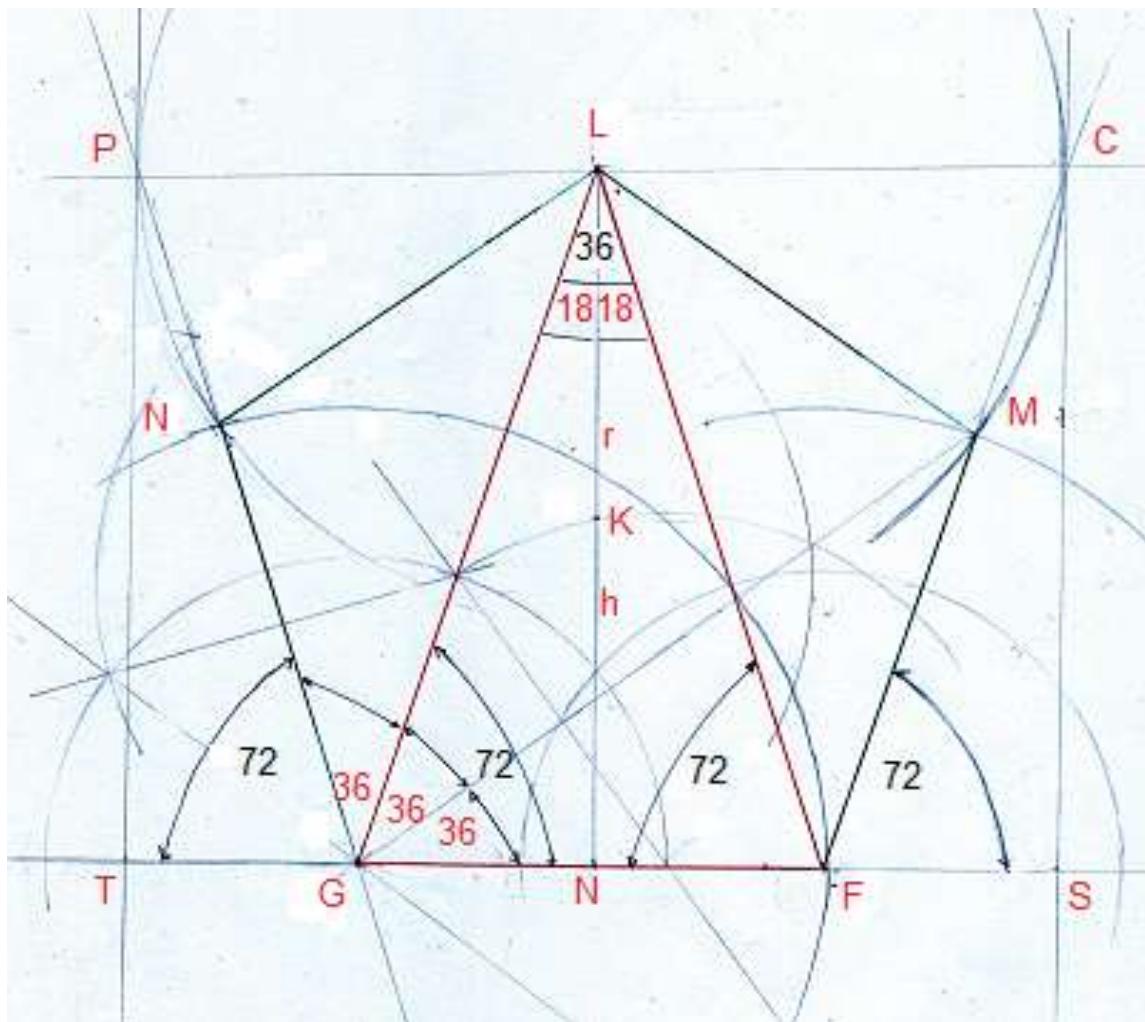


$$FG = GL = \Phi = 1.618033989, \text{ ANGLE FGN} = 108 \text{ Deg.}$$

$$108/2 = 54, [GL] \sin(72) = 1.538841768 = r+h$$

$$[GL]\cos(72) = 0.5 = [FG]/2$$

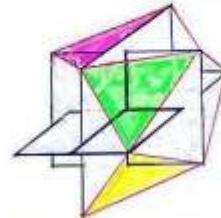
<https://www.linkedin.com/pulse/patterns-structured-matter-panagiotis-stefanides-stefanides>



<https://www.linkedin.com/pulse/x-y-z-coordinates-definition-platonic-eucleidean-stefanides>



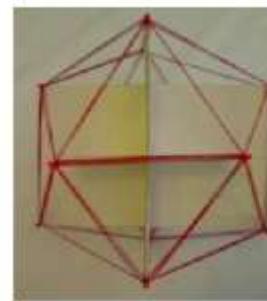
FUNDAMENTAL TETRAHEDRON
Building Polyhedra By Panagiotis Stefanides



GENERATOR POLYHEDRON
STRUCTURE
Discovery - Invention
By
Panagiotis Stefanides



DODECAHEDRON STRUCTURE By Panagiotis Stefanides



ICOSAHEDRON Structure By Panagiotis Stefanides

Important Discovery

From the geometry of the “**GENERATOR POLYHEDRON**”, we find relationships:

3 parallelogrammes vertical to each-other. Sides’ lengths, of each parallelogramme, are in ratio

of $4/\pi = 1.27201965$ [for $\pi = 3.14460551$ i.e. **4/ SQRT(Golden Ratio)].**

$$[4/2]/[\pi/2] = [\pi/2]/x, \quad x = \{[\pi/2]^2\}/[4/2] = 2.472135953/2 =$$

$$= 1.236067977 = 1/[\sin(54)] = x$$

This is directly Related to the Pentagon Angle of 54 Deg:

$$1/\sin(54) = 1.236067978$$

$$r/h = \{ [1/2]/\cos(54)\} / r\sin(54) = 0.850650808 / 0.68819096 = 1.236067977$$

$$1/\sin(54) = 1.236067978$$

Wolfram Alpha Checking Solutions

$$1/\sin(54) = 1.236067977499789696409173668731276235440618359611525724270$$

$$4/[\sqrt{[\sqrt{5} + 1]/2}] =$$

$$= 3.144605511029693144278234343371835718092488231350892950659$$

$$\{[3.144605511029693144278234343371835718092488231350892950659]^2\}/8 =$$

$$= 1.236067977499789696409173668731276235440618359611525724270$$

$$[1/8]*\{4/[\sqrt{[\sqrt{5} + 1]/2}]\}^2 = [1/\sin(54)]$$

[https://www.wolframalpha.com/input/?i=%5B1%2F8%5D*%7B4%2F%5Bsqr%7B+ %5Bsqr\(5\)+%2B1%5D%2F2%7D%5D%7D%5E2+%3D+%5B+1%2Fsin\(54\)%5D](https://www.wolframalpha.com/input/?i=%5B1%2F8%5D*%7B4%2F%5Bsqr%7B+ %5Bsqr(5)+%2B1%5D%2F2%7D%5D%7D%5E2+%3D+%5B+1%2Fsin(54)%5D)

$$[1/8]*\{4/[\sqrt{[\sqrt{5} + 1]/2}]\}^2 = [3+\sqrt{5}] / [2+\sqrt{5}]$$

[https://www.wolframalpha.com/input/?i=%5B1%2F8%5D*%7B4%2F%5Bsqr%7B+ %5Bsqr\(5\)+%2B1%5D%2F2%7D%5D%7D%5E2+%3D+%5B3%2Bsqr\(5\)%5D+%2F+%5B+2%2B+sqr\(5\)%5D](https://www.wolframalpha.com/input/?i=%5B1%2F8%5D*%7B4%2F%5Bsqr%7B+ %5Bsqr(5)+%2B1%5D%2F2%7D%5D%7D%5E2+%3D+%5B3%2Bsqr(5)%5D+%2F+%5B+2%2B+sqr(5)%5D)



Link References

<http://www.stefanides.gr>

<https://communities.theiet.org/files/13919>

https://www.researchgate.net/publication/315801180_GENERATOR_POLYHEDRON_OF_PLATONIC-EUCLEIDEAN_SOLIDS_By_Panagiotis_Stefanides_1A

https://www.researchgate.net/publication/316582864_IMPORTANT_DISCOVERY_-PENTAGON_STRUCTURE -RULER_AND_COMPASS-By_P_Stefanides

<https://www.youtube.com/watch?v=ZXKQFXIWvE0&t=4s>

https://www.youtube.com/watch?v=N_sIR0SrG-I

https://www.youtube.com/watch?v=XeOjPmKSsOI&feature=em-upload_owner

<https://www.youtube.com/watch?v=mFn5pl4krv4>

https://www.researchgate.net/publication/311440042_SQUARES%27_CIRCUMSCRIBED_CIRCLEs_By_Panagiotis_Stefanides

https://www.researchgate.net/publication/311156470_No_Detection_of_Imperfection_of_Circle_Challenges_the_Transcendence_of_p_By_Panagiotis_Stefanides

<https://www.linkedin.com/pulse/squares-circumscribed-circles-concentric-package-stefanides?trk=prof-post>

<https://www.linkedin.com/pulse/detection-imperfection-circle-challenges-%CF%80-panagiotis-stefanides?trk=prof-post>

http://www.stefanides.gr/pdf/2012_Oct/PHOTO_12.pdf

<http://contest.techbriefs.com/2015/entries/sustainable-technologies/5464>

https://www.youtube.com/watch?v=XeOjPmKSsOI&feature=em-upload_owner

http://www.stefanides.gr/pdf/DIALOGO_2014_PANAGIOTIS_STEFANIDES.pdf

<http://ireport.cnn.com/people/PCSTEFANIDES?viewingAsOthers=true>

http://www.stefanides.gr/pdf/BRIDGES_2014_PANAGIOTIS_STEFANIDES.pdf

http://www.stefanides.gr/pdf/BOOK%20_GRSOGF.pdf

http://www.stefanides.gr/pdf/BOOK_1997.pdf

<https://hydrodynamica.wordpress.com/2014/09/06/panagiotis-stefanides-from-athens-designer-of-geometry-and-drawing/>

[https://www.researchgate.net/publication/260036589_GOLDEN_ROOT_CH_\(1\)_PREPUBLICATION_SECOND_EDITION_TRANSLATION_IN_CHINESE_\(2\)?ev=prf_pub](https://www.researchgate.net/publication/260036589_GOLDEN_ROOT_CH_(1)_PREPUBLICATION_SECOND_EDITION_TRANSLATION_IN_CHINESE_(2)?ev=prf_pub)

http://www.stefanides.gr/pdf/2012_Oct/PHOTO_09_PCST_GEOMETRY.pdf

https://www.researchgate.net/publication/292775110_EXHIBITION_OF_MATHEMATICAL_ART_JMM16_by_Panagiotis_Stefanides

https://www.researchgate.net/publication/283047210_BRIDGES_RG_C

https://www.researchgate.net/publication/282945779_PANAGIOTIS_STEFANIDES_WORKS_PRESENTED_TO_A_RUSSIAN_LYCEUM_CONFERENC_BY_IRINA_PECHONKINA_1A-

<https://www.linkedin.com/pulse/data-from-conference-presentations-exhibits-panagiotis-stefanides>

http://www.stefanides.gr/Html/GOLDEN_ROOT_SYMMETRIES.html

http://herz-fischler.ca/ARTICLES/very_pleasant_theorem.pdf

https://www.google.gr/webhp?sourceid=chrome-instant&ion=1&espv=2&ie=UTF-8#q=KEPLER+MAGIRUS+TRIANGLE&*

<https://www.linkedin.com/pulse/exhibition-symmetry-festival-2006-panagiotis-stefanides>

<https://www.linkedin.com/pulse/circle-circumference-equated-naturally-square-area-pi-stefanides>

<https://www.linkedin.com/pulse/polygonal-method-compared-triangular-quadrature-panagiotis-stefanides>

C.V. RESUME

Eur Ing Panagiotis Chr. Stefanides BSc(Eng) Lon(Hons) MSc(Eng)NTUA TEE CEng



Emeritus Honoured Member of the Technical Chamber of Greece

IET Hellas Network Honorary Secretary [2010 present]

Born: 05. Jan.1945, Aigaleo, Athens.

Professional and Academic Qualifications:

- [2002] **Chartered Engineer** of the Engineering Council (**UK**),
- [2002] Member of the IEE [**IET**],
- [1997] Certified Lead Auditor [Cranfield University],
- [1977] Member of the Technical Chamber of Greece TEE,
- [1975] Electrical and Mechanical Engineer of the Technical University of Athens,
- [1974] Electrical Engineer of the University of London .

Professional Experience:

30 Jun 2010-1978 [HAI]

- Electromagnetic Compatibility,Head of Standards and Certification, **EMC Hellas** SA, Affiliate of HELLENIC AEROSPACE **HAI**,
- Research and Development,Lead Engineer, of the Electronic Systems Tests and Certification,
- Engineering Quality and Reliability Section, Lead Engineer, and HAI's Quality System Lead Auditor,
- Engines' Directorate Superintendent, Managed the Engineering Methods Division of the M53P2 Engine Nozzle Manufacturing, of the SNECMA- HAI Coproduction[Module 10] M53 P2 Programme, MANAGED the Engineering Methods Section.
- Engines' Tests and Accessories Superintendent,
- Engines' Electrical Accessories Supervisor.

1978-1974

- G.E., Athens Representatives, Sales Engineer / Assistant Manager,
- Continental Electronics Dallas Texas, and EDOK-ETER Consortium Engineer, of a 2MW Superpower Transmitters' installation Programme, in Saudi Arabia,
- Chandris Shipyards Engineer and Vessel repairs Superintendent, Salamis Island.

Training:

Public Power Corporation [GR], Sizewell Nuclear Power Station [UK], Oceangoing Steamship [S/S Chelatros] and Motor Vessels' Navigation [Celestial, Radio, Coastal] and Engines', of "Kassos" Shipping Co. Ltd. [R&K London].

Presentations, Publications, Conferences, Awards :

BOOK Published 2010 "Golden Root Symmetries of Geometric Forms"

Ref Conference: http://www.stefanides.gr/Html/GOLDEN_ROOT_SYMMETRIES.htm

Publication: "Golden Root Symmetries of Geometric Forms" The journal of the Symmetry: Culture and Science, Volume 1q7,Numbers 1-2, 2006, pp 97-111

Award: Archimedes Silver Medal for the Invention of a **Solar** Locating and **Tracking** System, by the Hellenic Society of Research and Inventions, Athens Hilton 4 Feb 1983.

[“**Heliotropio Stefanides**” Competed in Create the Future Design Contest 2011, of the NASA Tech Briefs <http://contest.techbriefs.com/sustainable-technologies-2011/1179>].

Latet paper issued in EMC to :

MEDPOWER 2008 [IET] in Thessaloniki [2-5 Nov. 2008] under the title:

“Compliance of Equipment in Accordance with an Adequate Level of Electromagnetic Compatibility”,

Eur Ing Panagiotis Chr. Stefanides, Head of Standards and Certification EMC Hellas sa,Affiliate of Hellenic Aerospace Industry sa [HAI] 2-4, Messogion Ave[Athens Tower], 11527 Athens, Greece.

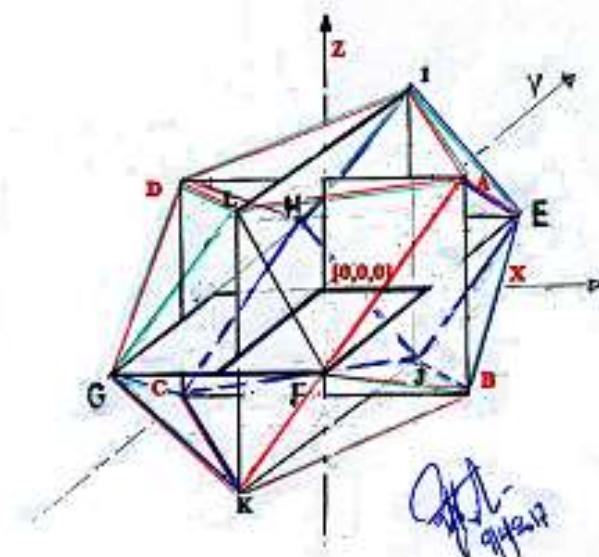
(C.V.), <http://www.stefanides.gr>



GENERATOR POLYHEDRON OF PLATONIC- EUCLIDEAN SOLIDS

By
Eur Ing Panagiotis Stefanides BSc(Eng)Lon(Hons)
 MSc(Eng)NTUA CEng MIET
 Chartered Engineer[UK]

$$[1/8] * \{4 / [\sqrt{[\sqrt{5} + 1]/2}]\}^2 = [1/\sin(54)]$$



$$[1/8] * \{4 / [\sqrt{[\sqrt{5} + 1]/2}]\}^2 = [3 + \sqrt{5}] / [2 + \sqrt{5}]$$

ISBN 978 – 618 – 83169 – 0 - 4